

**İSTANBUL TEKNİK ÜNİVERSİTESİ ★ FEN BİLİMLERİ ENSTİTÜSÜ**

**ELASTİK ZEMİNE OTURAN TIMOSHENKO KİRİŞİNİN SONLU  
ELEMANLAR YÖNTEMİYLE ELASTOPLASTİK ANALİZİ**

**YÜKSEK LİSANS TEZİ  
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**Anabilim Dalı : İnşaat Mühendisliği**

**Programı : Yapı Mühendisliği**

**Tez Danışmanı: Prof. Dr. Metin AYDOĞAN**

**HAZİRAN 2009**



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**HAZİRAN 2009**





## **ÖNSÖZ**

İstanbul Teknik Üniversitesi Fen Bilimleri Enstitüsü'ne bağlı Yapı Mühendisliği programında gerçekleştirilen bu yüksek lisans tez çalışmasında Timoshenko kırışları detaylı olarak incelenmiş, çeşitli şartlar altındaki problemlerin çözümü gerçekleştirilmiştir.

Çalışma boyunca her konuda benden yardımını esirgemeyen saygı değer hocam Prof.Dr. Metin Aydoğan başta olmak üzere bugüne kadar eğitimimde emeği geçmiş herkese teşekkürü bir borç bilirim.

Haziran 2009

Elif YAZICI

İnşaat Mühendisi



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## **ELASTİK ZEMİNE OTURAN TIMOSHENKO KİRİŞİNİN SONLU ELEMANLAR YÖNTEMİYLE ELASTOPLASTİK ANALİZİ**

### **ÖZET**

Günümüzde teknolojinin ilerlemesine paralel olarak gelişen bilgisayar programları, değişik bilim dallarına ait problemlerin çözümünde kolayca uygulanmakta, bu sayede muhtelif koşullar altında çeşitli sistemlerin davranışları önceden belirlenebilmektedir.

Bu çalışmada pek çok mühendislik probleminin çözümünde oldukça iyi bir yaklaşım sağlayan sonlu eleman yöntemi kullanılarak FORTRAN dilinde yazılan bir bilgisayar programı yardımıyla Timoshenko kırışı için muhtelif tip problemlere ait elastoplastik çözümler elde edilmiştir. Bu program yüksek lisans tezine konu olan Timoshenko kırışlarının tabakalı ve tabakasız halleri için, farklı zemin koşulları, yüklemeler ve değişik malzeme durumlarında davranışlarının incelenmesinde kullanılmıştır. Timoshenko kırışları genel kırış teorisine ilaveten enine kayma şekil değiştirmelerini de dikkate alır ve  $L/h$  (genişliğinin yüksekliğine oranı) değeri küçük olan problemlerde çok daha doğru sonuçlar verdiğiinden “Kalın Kırış” teorisi olarak da bilinir.

Çalışmanın girişten sonraki bölümünde bir boyutlu elastoplastik problemler ve çözüm yöntemlerinden bahsedilmiştir. Üçüncü bölümde Timoshenko kırışı ayrıntılı olarak irdelenerek sonlu eleman yaklaşımının bu kırışlara uygulanmasına ait esaslar verilmiştir. Dördüncü bölümde kullanılan bilgisayar programlarına ait akış diyagramları verilmiş, ana ve alt programlar ve bu programlarda kullanılan komutların işlevleri ayrıntılı olarak sunulmuştur. Beşinci bölümde Timoshenko kırışlarının elastik zemine yataklanma durumu da dahil olmak üzere tekil ve yayılı yük etkileri altında uygulamalar yapılmıştır. Aynı bölümde tabakalı hal için de çözümler bulumaktadır. Altıncı ve son bölümde önceki bölümde yapılan çözümler irdelenerek sonuçlar verilmiştir.



## **ELASTOPLASTIC FINITE ELEMENT ANALYSIS OF TIMOSHENKO BEAM ON ELASTIC FOUNDATION**

### **SUMMARY**

Nowadays computer programs has developed in parallel with technological advancement. Most of these programs could be easily applied to solution process of various problems relating to various branches of science. Thanks to these applications attitudes of different systems can be determined easily.

In this study elastoplastic solution of Timoshenko beam is achieved by using the finite element method which provides fairly well approximate solutions for many engineering problems. Mathematical calculations were carried on a computer program which taken from the literature and improved by the author of this thesis in Fortran programming language. This program is used to obtain the behaviour of the nonlayered Timoshenko beams at different foundation conditions, loading types and material properties. The layered beam case is also analyzed.

This thesis consist of six chapters. The first chapter is introduction. The second chapter is devoted to one dimensional elastoplastic problems and the summary of the general four solution methods. In the third chapter the essentials of Timoshenko beam theory is explained in detail and the principals of finite element method for Timoshenko beam is introduced. In the fourth chapter computer programs is given with flow charts. Master and subroutine programs are examined with all of their commands. In the fifth chapter Timoshenko beam applications were presented under the concentrated and uniform loading conditions including the embedment in the elastic foundation. In the same chapter some solutions for the layered case also introduced. In the last chapter the results of the numerical solutions assessed and conclusion is presented.



## **1. GİRİŞ**

### **1.1 Konu**

Kırışlar yapılarda döşeme ve duvarlardan gelen yüklerle yapının kullanım amacına göre değişen yük etkilerini düşey taşıyıcı elemanlara aktaran ve düşey taşıyıcıların bağlanarak çerçeveye sisteminin oluşturulmasını sağlayan yapı elemanlarıdır.

Uygulamada en çok kullanılan kırış teorisi Euler-Bernoulli kırış teorisidir. Bunun nedeni basitliğidir. Bu teoride şekil değiştirmeden önce ortalama düzleme dik olan kesitin şekil değişiminden sonra da dik kaldığı varsayılmıştır. Timoshenko kırış teorisinde ise enine kayma şekil değiştirmeleri de dikkate alınır. Yani şekil değiştirmeden önce ortalama düzleme dik olan kesit şekil değişiminden sonra bu düzleme bir açı yapar, ancak düzlem kesit yine düzlem kalır (Bernoulli-Navier hipotezi). Timoshenko kırış teorisi Euler-Bernoulli kırış teorisinden daha gelişmiş ve bir anlamda onun iyileştirilmiş halidir. Özellikle kısa ve yüksek kırışlar, yani açıklık/yükseklik oranı düşük olan kırışlar, için Euler-Bernoulli teorisine nazaran daha doğru sonuçlar verir.

### **1.2 Çalışmanın Amacı ve Kapsamı**

Günümüzde bilgisayar teknolojisi ve yazılımlardaki gelişmelere paralel olarak birçok bilim dalında olduğu gibi yapı mühendisliği alanında da çeşitli yapı elemanlarının farklı koşullar altındaki davranışlarını değişik yaklaşımlarla incelemek ve daha hassas sonuçlar elde etmek oldukça kolaylaşmıştır.

Bu çalışmanın amacı bir parametrel elastik zemine (Winkler zemini) oturan Timoshenko Kırışının elastoplastik davranışının sonlu eleman yaklaşımıyla incelenmesidir. Çalışmanın kapsamı içinde bir boyutlu doğrusal olmayan problemler ve çözüm yöntemleri özetlenmiş, bir boyutlu elastoplastik problemler açıklanmıştır.

Timoshenko Kirişinin sonlu elemanlar yöntemi ile elastoplastik analizi açıklanarak çözüm amacıyla kullanılan ve literatürde daha önce geliştirilmiş olan bir bilgisayar programı hakkında bilgi verilmiştir. Tez kapsamında söz konusu programda bazı iyileştirmeler yapılarak ilgili rutinler tadil edilmiştir. Keza programda elastik zemine oturma haline ait ekleni ve değişiklikler de yapılmıştır.

Önce tabakasız hale ait bilgisayar programı açıklanmış, daha sonra tabakalı hal için yapılan değişiklikler gösterilmiştir. Program FORTRAN dilinde kodlanmıştır.

Tabakasız hal için kullanılan programdaki rijitlikler yerine kayma şekil değiştirmelerini dikkate alan rijitlik matrisi konularak bulunan çözümler öncekiler ile karşılaştırılmıştır. Bu hal için ayrıca elastik zemine yataklanma durumu da incelenmiştir.

Yukarıda açıklanan problemlerle ilgili programlara ait giriş bilgileri ve çıkış düzenleri anlatılmış, sayısal uygulamalara ait sonuçlar grafikler ve çıktılar halinde verilmiştir.

## **2. BİR BOYUTLU DOĞRUSAL OLMAYAN PROBLEMLER**

Bilim ve mühendisliğin birçok dalıyla ilgili olan doğrusal olmayan pek çok problem, katsayıları ana değişkenlere bağlı fonksiyonlardan oluşan denklemlere indirgenerek çözüm yapılabilir. Bu başlık altında tez konusuna esas olan problemin çözümünde kullanılacak olan yöntemler açıklanacaktır.

### **2.1 Doğrusal Olmayan Problemler İçin Basit Sayısal Çözüm Yöntemleri**

Sonlu eleman yönteminin doğrusal olmayan problemlerin çoğunun çözümünde kullanılan denklem formu;

$$\mathbf{H}\phi + \mathbf{f} = 0 \quad (2.1)$$

şeklindedir. Bu denklemde “ $\phi$ ” temel bilinmeyenler vektörünü, “ $f$ ” yük vektörünü, “ $H$ ” rijitlik matrisini temsil etmektedir. Yapısal problemlerde “yük” ve “rijitlik” terimleri doğrudan kullanlabilirken, diğer mühendislik ve fizik problemlerinde bu terimlerin anlamları göz önüne alınan fiziksel probleme göre değişimektedir.

Bu denklemdeki  $H$  matrisi, eğer  $\phi$  bilinmeyenleri veya türevlerine bağlı ise problem doğrusal olmaz. Bu durumda (2.1) denkleminin doğrudan çözümü genellikle mümkün olmaz ve iteratif çözüm yolları kullanılır. İteratif çözüm yöntemlerinin en çok uygulananları aşağıda sıralanmıştır:

#### **2.1.1 Doğrudan iterasyon (veya ardışık yaklaşım) yöntemi**

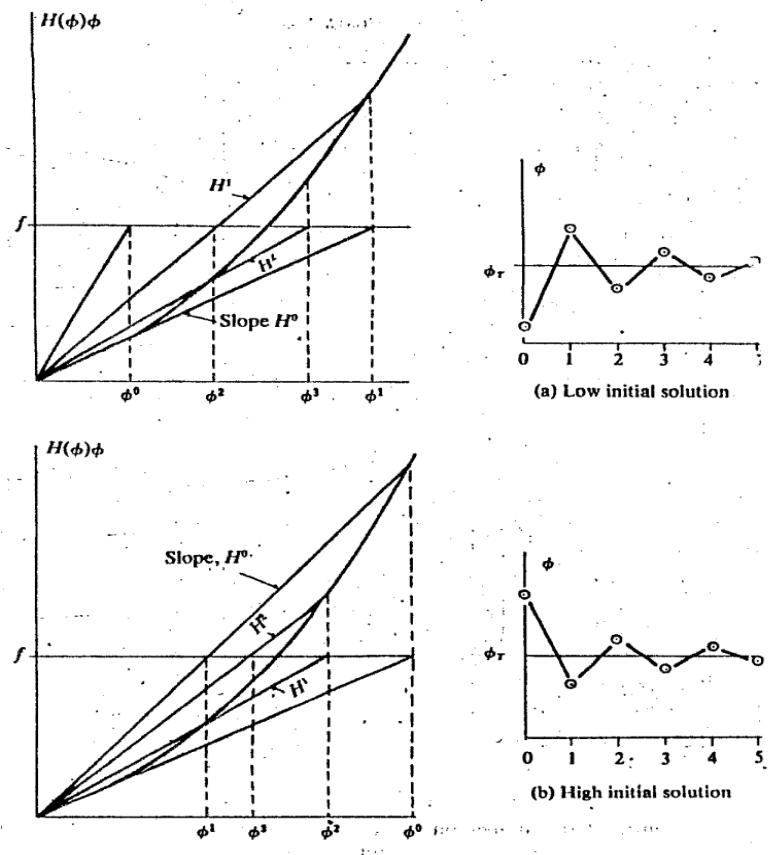
Bu yöntemde ardışık çözümler kullanılır. Her bir çözüm bir önceki çözümdeki  $\phi$  bilinmeyenlerinin  $H(\phi)$  matrisindeki değerini tahmin etmek için kullanılır.

(2.1) denklemi yeniden yazılır ve  $(r+1)$ . İterasyon için düzenlenirse

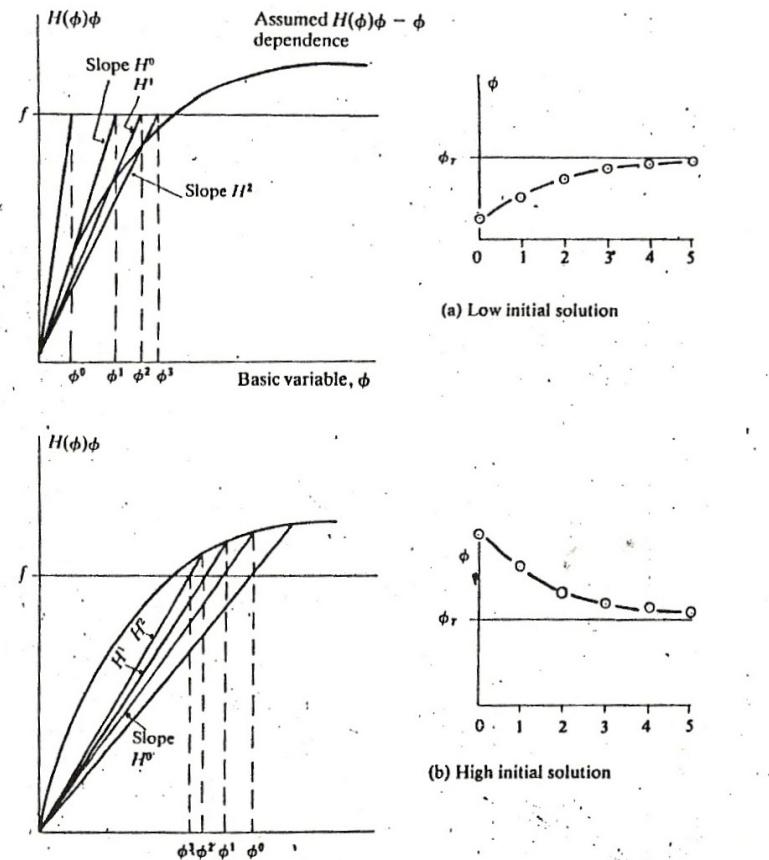
$$\varphi = -[H(\varphi)]^{-1} \cdot f \quad (2.2)$$

$$\varphi^{r+1} = -[H(\varphi^r)]^{-1} \cdot f \quad (2.3)$$

olur. Eğer çözüm yakınsiyorsa, yani  $r$  sonsuza giderken,  $\varphi$  doğru sonuca yaklaşır. (2.3) denkleminden görüldüğü gibi her iterasyon adımı için rijitlik matrisi  $H$  yeniden hesaplanmalıdır. Çözüme başlarken  $\varphi$  bilinmeyeninin tahmini başlangıç rijitlik matrisinin hesaplanabilmesi için gereklidir.



**Şekil 2.1:**Tek değişkenli problem için direkt iterasyon yöntemi-içbükey H- $\phi$  ilişkisi



**Şekil 2.2:**Tek değişkenli problem için direkt iterasyon yöntemi-dışbükey H- $\phi$  ilişkisi

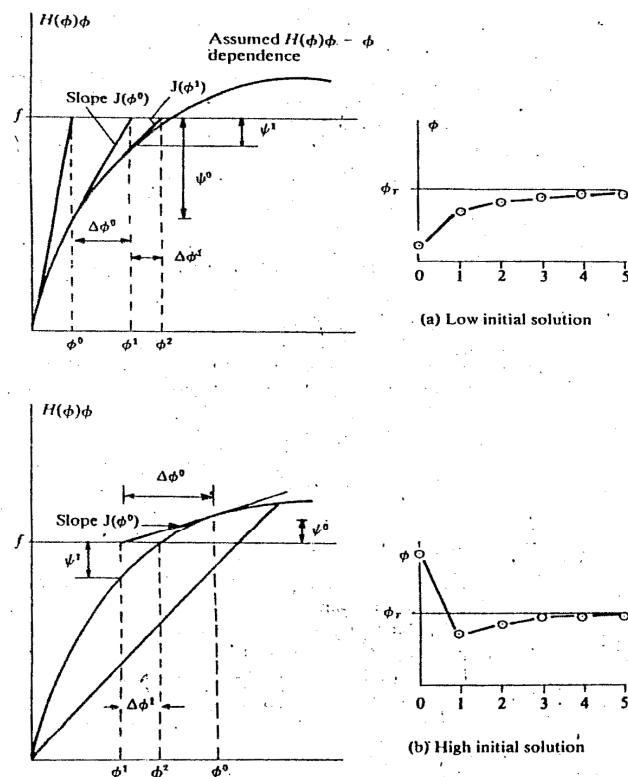
### 2.1.2 Newton- Raphson yöntemi

Doğrudan iterasyon yöntemindeki iteratif çözüm yönteminin herhangi bir aşamasında sonuca yakınsama olmadan (2.1) denklemi sağlanamaz. Newton-Raphson yönteminde artık kuvvetlerin olduğu varsayılar ve bu kuvvetlerin sistem çözümündeki varlığı aşağıdaki gibi gösterilir.

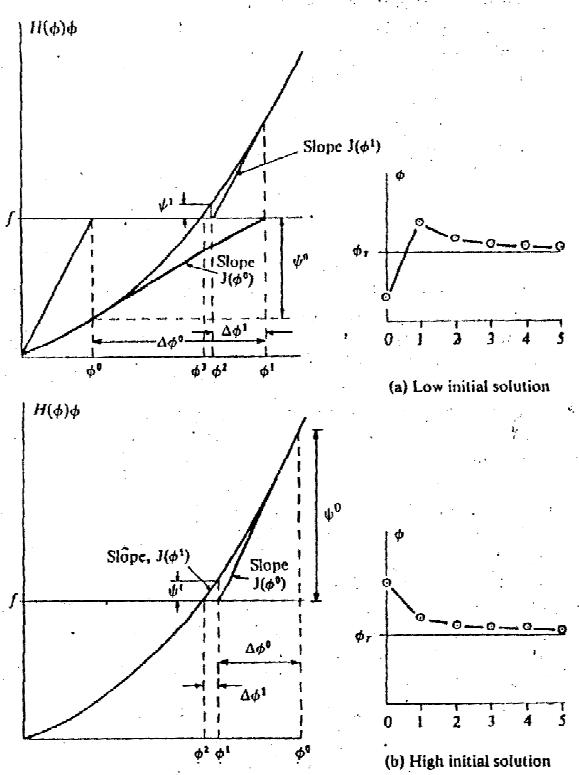
$$\psi = H\varphi + f \neq 0 \quad (2.4)$$

Bu yöntemde bir  $\varphi^0$  başlangıç değeri ile yaklaşımına başlanır. Şekil (2.4)'te görüldüğü gibi  $J(\varphi^1)$  eğrisi ile  $\varphi^0$  noktasının kesiştiği yerden  $J(\varphi^1)$ 'e çizilen teğetin yatay ekseni kestiği yer yani  $\varphi^1$  bir sonraki yaklaşımın başlangıç noktasıdır. Bu şekilde  $\varphi^1, \varphi^2, \dots, \varphi^n$  ile eğrinin teğetinin yatay ekseni kesim noktaları bulunarak köke yaklaşılır.

Newton-Raphson yönteminde eğrinin kendisi yerine teğeti kullanılarak lineerleştirme yapılır. Ardışık yaklaşım, kök değeri izin verilen en büyük hata değerinden küçük olunca sona erer.



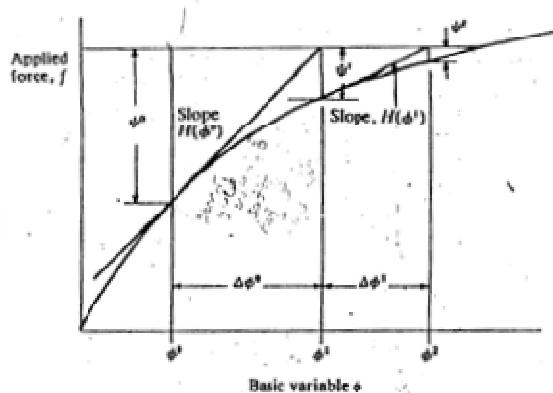
**Şekil 2.3:** Tek değişkenli problem için Newton-Raphson Metodu-dışbükey H- $\phi$  ilişkisi



**Şekil 2.4:** Tek değişkenli problem için Newton-Raphson Metodu-içbükey H- $\phi$  ilişkisi

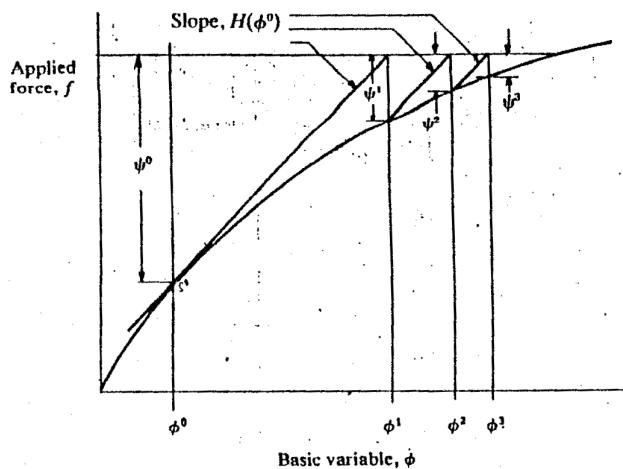
### 2.1.3 Teğetsel rıjilik yöntemi

Yapı mühendisliğinde  $H$ , yapının rıjilik matrisi olarak yorumlanabilir. Rıjilikin yer değiştirmenin derecesine bağlı olduğu doğrusal olmayan durumlarda  $H$ , yapının herhangi bir noktasındaki kuvvet-yer değiştirme ilişkisinin yerel değişimine eşittir ve bu teğetsel rıjilik olarak tanımlanır. Artımlar halinde çözüme gidilen problemlerin analizinde çözüm yapının sadece o andaki yer değiştirmelerine değil önceki yükleme geçmişine de bağlıdır. Herhangi bir yük admımda problem doğrusallaştırılabilir.



**Şekil 2.5:**Tek değişkenli problem için teğetsel rıjilik çözüm algoritması

#### 2.1.4 Başlangıç rıjılıği yöntemi



**Şekil 2.6:**Tek değişkenli problem için başlangıç rıjılıği çözüm algoritması

Yukarıda bahsedilen diğer 3 yöntemde her iterasyonda denklem takımının tekrar çözümü gereklidir. Deneme değerlerinin hesabında başlangıçtaki denemeye karşı gelen rıjilikler kullanılırsa her adımda denklem takımının tekrar çözümü gerekmez. Bu halde tüm denklem takımının çözümü yalnızca ilk iterasyonda yapılır ve bunu takip eden yaklaşımlarda rıjilik için bu değer kullanılır. Her adımda, aynı rıjilik matrisi kullanıldığından, sadece adımın sağ tarafındaki terimler indirgenir. Bu,

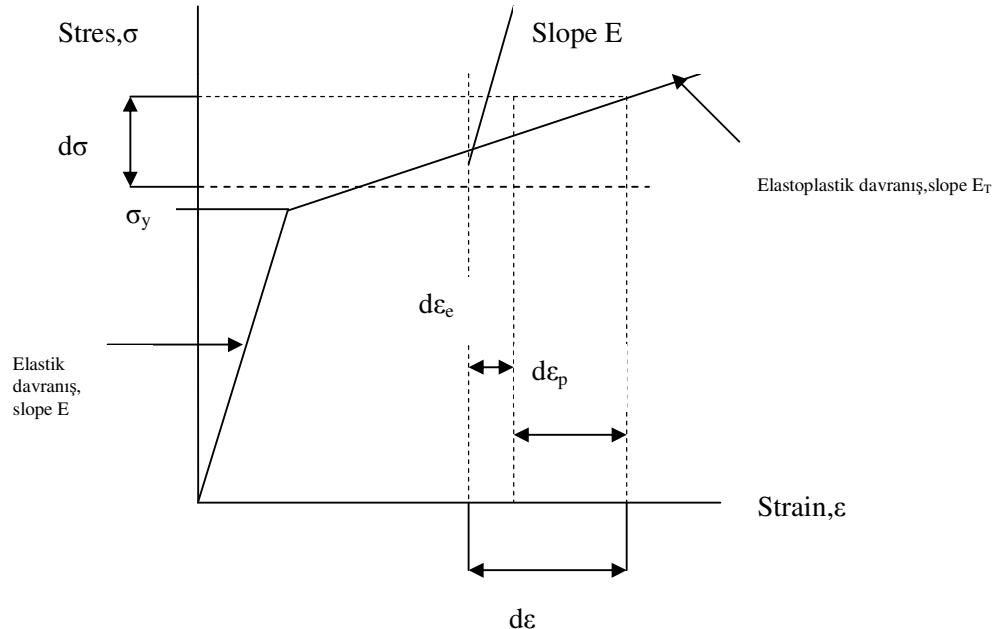
Şekil(2.6) da görüldüğü üzere çözüm süresini önemli bir oranda azaltır, ancak yakınsaklık oranını da düşürür. İterasyon algoritması teğetsel rijitlik yöntemindeki ile idantikdir. Bu yöntem koşulsuz olarak yakınsaktır ve malzemeden oluşan negatif rijitlikli hallerde de kullanılabilir. Başlangıç rijitliği ya da teğetsel rijitlik yöntemlerinden hangisinin daha ekonomik olduğu ilgilenilen probleme ait nonlineerlik derecesinin büyüklüğü ile alakalıdır. Optimum algoritma her iki yöntemin karışımı ile bulunabilir, yani seçilen iterasyon aralıkları için rijitlikler değiştirilebilir.

## **2.2 Bir Boyutlu Elastoplastik Problemler**

Elastoplastik davranış, başlangıçtan belirli bir gerilme değerine kadar elastik olan malzeme davranışının bu seviyeden sonra plastik davranışa dönüşmesi olarak tanımlanabilir.

Plastik şekil değiştirme yüklemenin kaldırılmasıyla geri çevrilemez. Plastik şekil değiştirmenin başlangıcı (veya akma) akma kriteri ile tanımlanır ve genellikle akma sonrasında pekleşme bölgesi adı verilen şekil değiştirme diliminde malzeme rijitliği önemli ölçüde azalır.

Bir boyutlu problemlerde elastoplastik davranışın tam anlamıyla tanımlanabilmesi için gerekli olan malzeme parametreleri malzemeye tek eksenli çekme testi uygulanarak elde edilir.



**Şekil 2.7:** Elastoplastik davranış

Şekil(2.3) de bir malzeme için idealleştirilmiş gerilme-şekil değiştirmeye eğrisi görülmektedir. Çekme ve basınç etkileri altında malzemenin benzer davranış gösterdiği varsayılmıştır.

Malzeme, başlangıçta gerilme tek eksenli akma gerilmesi  $\sigma_y$  değerine ulaşıncaya kadar eğimi elastisite modülüne ( $E$ ) eşit olacak şekilde doğrusal elastik şekil değiştirmeye yapar. Yükün gerilme akma sınırını aşacak şekilde artırılmasıyla malzemenin doğrusal olarak pekleştiği varsayıılır. Pekleşen kısımdaki doğrunun eğimi teğetsel elastisite modülü ( $E_T$ ) ile gösterilir ve  $E$  değerine göre oldukça yatkı olduğu görülmektedir.

Yükün akmadan sonra artmaya devam etmesi sonucu akmadan sonra bir  $d\epsilon$  artımından dolayı  $d\sigma$  gerilme artımı meydana gelsin. Şekil değiştirmenin iki ayrı bölgeye ayrılabildiği varsayılırsa

$$d\epsilon = d\epsilon_e + d\epsilon_p \quad (2.5)$$

yazılabilir.

Burada  $H'$  ile gösterilen bir pekleşme parametresi tanımlansın:

$$H' = \frac{d\sigma}{d\varepsilon_p} \quad (2.6)$$

Bu parametre gerilme-şekil değiştirmeye eğrisinin plastik kısmının elastik şekil değiştirmeye bileşenin kaldırılmasından sonraki eğimi olarak açıklanabilir.

$$H' = \frac{d\sigma}{d\varepsilon - d\varepsilon_e} = \frac{E_T}{1 - E_T/E} \quad (2.7)$$

Doğrusal yer değiştirmeye yapan tek eksenli çubuk elemanı dikkate alalım. Enkesit alanı  $A$  olan ve artan bir eksenel  $F$  kuvveti etkisinde olan bu elemanda  $\sigma = F/A$  değerinin  $\sigma_y$ 'ye eşit ya da küçük olduğu durumlarda malzeme elastiktir. Bu aralıkta çubuktaki eksenel yer değiştirmeye  $\delta$  ve malzeme davranışının elastik olduğu düşünülerek  $K_e$  rijitliği

$$K_e = \frac{F}{\delta} = \frac{E \cdot A}{L} \quad (2.8)$$

olur. Eleman rijitlik matrisi ise:

$$K_e^{(e)} = \frac{EA}{L} \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \quad (2.9)$$

dir.  $F$  kuvveti malzeme akana kadar arttırılsın. Bu noktadan sonra elemanda ilave bir uzamaya ( $d\delta$ ) neden olan bir yük artımı ( $dF$ ) olacaktır. Eleman uzunluğu  $L$  ise bu durumda aşağıdaki ifadeler yazılabilir:

$$d\delta = (d\varepsilon_e + d\varepsilon_p)L \quad (2.10)$$

$$dF = d\sigma A = AH'd\varepsilon_p \quad (2.11)$$

Bu durumda malzemenin teğetsel rijitliği ise

$$K_{ep} = \frac{dF}{d\delta} = \frac{AH' d\varepsilon_p}{L(d\sigma/E + d\varepsilon_p)} \quad (2.12)$$

veya (2.6) denklemini kullanarak

$$K_{ep} = \frac{EA}{L} \left( 1 - \frac{E}{E+H'} \right) \quad (2.13)$$

şekillerinde yazılabilir.

Sonuç olarak elastoplastik malzeme davranışları için eleman rijitlik matrisi

$$K_{ep}^{(e)} = \frac{EA}{L} \cdot \left( 1 - \frac{E}{E+H'} \right) \begin{bmatrix} 1 & -1 \\ -1 & 1 \end{bmatrix} \quad (2.14)$$

ile verilir. (2.14) denkleminde matristen önceki ilk terim (2.9) denkleminde de görülebileceği gibi elastik rijitliği, ikinci terim ise akmadan dolayı malzeme elastikliğinde meydana gelen azalmanın rijitlikteki etkisini göstermektedir.

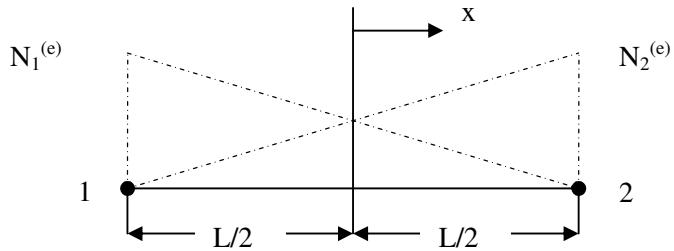
Sonlu elemanlar yönteminde eleman rijitlik matrisinin standart ifadesi aşağıdaki gibidir:

$$K_e^{(e)} = \int_V B^T D B dV = A \int_0^L B^T D B dx \quad (2.15)$$

Tek boyutlu elemanlarda  $D=E$  olmak üzere

$$B = \begin{bmatrix} \frac{dN_1^{(e)}}{dx} & \frac{dN_2^{(e)}}{dx} \end{bmatrix} = \begin{bmatrix} -1 & 1 \\ L & L \end{bmatrix} \quad (2.16)$$

yazılabilir. Burada  $N_1^{(e)}$  ve  $N_2^{(e)}$  doğrusal yer değiştirmeye karşı gelen şekil fonksiyonlarıdır.



**Şekil 2.8:** Şekil fonksiyonları

$$N_1^{(e)} = \frac{1}{2} - \frac{x}{L} \quad (2.17)$$

$$N_2^{(e)} = \frac{1}{2} + \frac{x}{L}$$

Netice olarak elastoplastik malzeme davranışları için teğetsel rijitlik matrisi  $D$  yerine  $D_{ep}$  konularak elde edilebilir:

$$D_{ep} = E \cdot \left( 1 - \frac{E}{E + H} \right) \quad (2.18)$$

Tam (perfekt) plastik malzeme halinde akmadan hemen sonra  $H' = 0$  ve (2.14) bağıntısından  $K_{ep}^{(e)} = 0$  olur. Bu durumda elastoplastik teğetsel rijitlik matrisi tekil olur ve çözüm için teğetsel rijitlik yöntemi kullanılamaz. Bu güçlük başlangıç rijitliği yöntemi ile yenilebilir, bu halde her hesap adımında elastik eleman rijitlikleri kullanılır.

### **3. ELASTOPLASTİK TIMOSHENKO KIRIŞ ANALİZİ**

Elastoplastik kiriş analizinin yapılacağı bu bölümde öncelikle kiriş analizi ile ilgili iki ana teori, Euler-Bernoulli ve Timoshenko kiriş teorileri, tanımlanacaktır:

- **Euler-Bernoulli Kiriş Teorisi:** Kübik yer değiştirmeleri esas alan deplasman yöntemi olan ve basitliği nedeniyle mühendisler tarafından en çok kullanılan teoridir. Burada kayma şekil değiştirmeleri dikkate alınmaz. Hermitian elemanla temsil edilebilen bu halde eğilme momentleri eleman boyunca lineer bir şekilde değişebilir.
- **Timoshenko Kiriş Teoremi:** Bu teori kayma gerilmelerinin etkilerini göz önüne alır. En basit Timoshenko kiriş eleman doğrusal yer değiştirmeleri esas alan Hughes elemanıdır. Bu elemanda eğilme momentleri eleman boyunca sabittir.

Euler-Bernoulli kiriş teoremi daha sık kullanılsa da, bu çalışmada elastoplastik kiriş analizinde kullanmak üzere Timoshenko kiriş teoremi ve sabit momentli sonlu elemanlar seçilmiştir.

Öncelikle Timoshenko kiriş teorisi ile ilgili temel varsayımlar özetlenmiş ve elastik hal için Hughes elemanına ait formülasyon verilmiştir.

Timoshenko kirişlerinin elastoplastik analizi için iki yaklaşım mevcuttur;

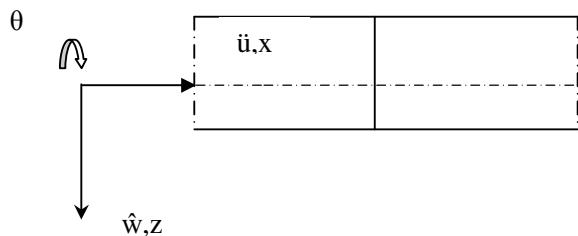
- **Tabakasız Yaklaşım:** Bu yöntemde eğilme momenti akma değerine ulaştığında tüm kiriş enkesitinin anı bir şekilde plastikleştiği varsayıılır. Başlangıçta kirişin dış lifleri plastikleşirken hızla kesitin tamamında aşamalı bir şekilde plastikleşme meydana gelir ve tüm kesit plastikleşene kadar sürer.

- **Tabakalı Yaklaşım:** Bu yaklaşımda kiriş yüksekliği boyunca her biri farklı plastikleşen tabakalarla ayrılır. Tabaka sayısı arttıkça kiriş yüksekliği boyunca plastiklikleşme kademeleri daha gerçekçi bir şekilde temsil edilir.

### 3.1 Timoshenko Kiriş Teorisinin Temel Varsayımları

Tipik bir Timoshenko kirişinde şekil değiştirmeden önce tarafsız eksene normal olan doğrular şekil değiştirmeden sonra da doğru olarak kalır, ancak tarafsız eksene normal kalmaları gerekmektedir.

Herhangi bir  $(x, z)$  noktasındaki eksenel yer değiştirme  $\bar{u}$ , normalin  $\vartheta(x)$  dönmesi cinsinden doğrudan ifade edilebilir;



**Sekil 3.1**

$$\bar{u}(x, z) = -z\vartheta(x) \quad (3.1)$$

Burada normal dönme  $\vartheta(x)$ , tarafsız eksenin eğimi ( $\frac{d\bar{w}}{dx}$ ) ile enine kayma şekil değiştirmelerinden oluşan dönmenin ( $\beta$ ) farkına eşittir. Yani

$$\vartheta(x) = \frac{d\bar{w}}{dx} - \beta \quad (3.2)$$

Herhangi bir (x,z) noktasındaki yanal yer değiştirmeye (  $\bar{w}$  ) tarafsız eksene ait yanal yer değiştirmeye eşittir.

$$\bar{w}(x, z) = w(x) \quad (3.3)$$

### 3.1.1 Gerilme-şekil değiştirme bağıntıları:

Timoshenko kırış teoresinde düzlem gerilme analizi için kullanılan elastik gerilme-şekil değiştirme bağıntıları biraz değiştirilerek kullanılır.

Kirişin x-z düzlemi boyunca yüklenmiş olduğu kabul edilerek izotrop elastik malzemeye ait gerilme-şekil değiştirme bağıntıları:

$$\begin{bmatrix} \sigma_x \\ \sigma_z \\ \tau_{xz} \end{bmatrix} = \frac{E}{1-\nu^2} \begin{bmatrix} 1 & \nu & 0 \\ \nu & 1 & 0 \\ 0 & 0 & \frac{(1-\nu)}{2} \end{bmatrix} \cdot \begin{bmatrix} \epsilon_x \\ \epsilon_z \\ \gamma_{xz} \end{bmatrix} \quad (3.4)$$

dır. Burada E elastisite modülü,  $\nu$  ise Poisson oranıdır.  $\sigma_z$  'nin sıfıra eşit olduğu kabul edilir.

$$\epsilon_z = -\nu \cdot \epsilon_x \quad (3.5)$$

ve (3.4) denkleminde  $\epsilon_z$  yerine konulursa;

$$\sigma_x = E \cdot \epsilon_x, \quad \tau_{xz} = G \cdot \gamma_{xz} \quad (3.6)$$

bağıntıları elde edilir. Burada ( $G$ ) kayma modülü izotrop malzeme için  $G = \frac{E}{2(1+\nu)}$  formülüyle bulunur.

### 3.1.2 Şekil değiştirme-yer değiştirme bağıntıları:

Genellikle küçük yer değiştirme teorisi kabul edilir ve eksenel şekil değiştirme  $\varepsilon_x$  ;

$$\varepsilon_x = \frac{\partial \bar{u}}{\partial x} \quad (3.7)$$

olur. (3.1)' deki yaklaşım ile bu şekil değiştirme

$$\varepsilon_x = -z \cdot \frac{d\theta}{dx} \quad (3.8)$$

dir. Benzer şekilde kayma gerilmesi  $\gamma_{xz}$  :

$$\gamma_{xz} = \frac{\partial \bar{u}}{\partial z} + \frac{\partial \bar{w}}{\partial x} \quad (3.9)$$

olur. Eğer (3.2) yaklaşımı benimsenir ise  $\gamma_{xz}$ :

$$\gamma_{xz} = -\vartheta + \frac{d\bar{w}}{dx} = \beta \quad (3.10)$$

olarak elde edilir.

### 3.1.3 Virtüel iş prensibi

Kalınlığı  $t$  olan ve genişliğin kalınlık boyunca tarafsız eksene göre simetrik değiştiği bir Timoshenko kirişini ele alalım. Kiriş  $q$  uniform yayılı yüküne maruz olsun.

Eğer kirişte bir grup virtüel yanal yer değiştirmeler ( $\delta w$ ), virtüel normal dönmeler ( $\delta\vartheta$ ) , bunlarla bağlantılı virtüel eğrilik  $-z \cdot [d(\delta\theta)/dx]$  ve virtüel kayma şekil değiştirmeleri  $\delta\beta$  meydana gelirse buradan virtüel iş denklemi:

$$\int_0^l \int_{-t/2}^{t/2} \int_{b(-t/2)}^{b(t/2)} \left( -z \frac{d(\delta\theta)}{dx} \sigma_x + \delta\beta \tau_{xz} \right) dy dz dx - \int_0^l \delta w q dx = 0 \quad (3.11)$$

olarak veya

$$\int_0^l \left( -\frac{d(\delta\vartheta)}{dx} M + \delta\beta Q \right) dx - \int_0^l \delta w q dx = 0$$

yazılabilir. Burada M eğilme momenti ve Q kesme kuvveti:

$$M = \int_{-t/2}^{t/2} \int_{b(-t/2)}^{b(t/2)} z \cdot \boldsymbol{\sigma}_x \cdot dy \cdot dz \quad (3.12)$$

$$Q = \int_{-t/2}^{t/2} \int_{b(-t/2)}^{b(t/2)} \boldsymbol{\tau}_{xz} \cdot dy \cdot dz \quad (3.13)$$

dir. M ve Q denklemlerinde  $\sigma_x$  ve  $\tau_{xz}$  yerine konulursa

$$M = \left( \int_{-t/2}^{t/2} \int_{b(-t/2)}^{b(t/2)} z^2 E dy dz \right) \left( -\frac{d\theta}{dx} \right) = EI \left( -\frac{d\theta}{dx} \right) \quad (3.14)$$

$$Q = \left( \int_{-t/2}^{t/2} \int_{b(-t/2)}^{b(t/2)} G dy dz \right) \beta = GA\beta \quad (3.15)$$

bağıntıları elde edilir. Burada EI eğilme rijitliği, GA: kayma rijitliği olup kesit çarpılmasını göz önünde bulunduran  $\alpha$  düzeltme çarpanını dikkate almak üzere  $\hat{GA}$  ile değiştirilir ( $\hat{A} = A/\alpha$ ). Örneğin dikdörtgen kesit için  $\alpha = 1.5$  alınır.

(3.13) ve (3.14) eşitliklerindeki M ve Q değerleri yukarıdaki değişikliğe göre yeniden düzenlenirse (3.11) denklemi aşağıdaki gibi yazılabilir:

$$\int_0^L \left( \frac{d(\delta\theta)}{dx} EI \frac{d\theta}{dx} + \delta\beta G A \beta - \delta w q \right) dx = 0 \quad (3.16)$$

### 3.1.4 Kiriş yaklaşımlarının karşılaştırılması:

Bu karşılaştırma için düzgün yayılı  $q$  yükü etkisindeki dikdörtgen kesitli basit bir kiriş ele alalım.  $EI$  eğilme rijitliği,  $\nu$  Poisson oranı,  $t$  kalınlık,  $L$  kiriş uzunluğu olmak üzere elastik bölge içindeki yanal yer değiştirmeler;

- Düzlem gerilme halinde;

$$w = \frac{q \cdot L^4}{24EI} \left[ \left( \frac{x}{L} \right)^4 - \frac{3}{2} \cdot \left( \frac{x}{L} \right)^2 + \frac{5}{16} \right] + \left( \frac{t}{L} \right)^2 \cdot \left[ \frac{12}{5} + \frac{3\nu}{2} \right] \cdot \left[ \frac{1}{4} - \left( \frac{x}{L} \right)^2 \right] \quad (3.17a)$$

- Timoshenko kirişi halinde;

$$w = \frac{q \cdot L^4}{24EI} \left[ \left( \frac{x}{L} \right)^4 - \frac{3}{2} \cdot \left( \frac{x}{L} \right)^2 + \frac{5}{16} \right] + \left( \frac{t}{L} \right)^2 \cdot [2\alpha \cdot (1+\nu)] \cdot \left[ \frac{1}{4} - \left( \frac{x}{L} \right)^2 \right] \quad (3.17b)$$

- Euler-Bernoulli kirişi halinde;

$$w = \frac{q \cdot L^4}{24EI} \left[ \left( \frac{x}{L} \right)^4 - \frac{3}{2} \cdot \left( \frac{x}{L} \right)^2 + \frac{5}{16} \right] \quad (3.17c)$$

olarak elde edilir. Yaklaşımlar karşılaştırıldığında ( $t / L$ ) oranının küçük olduğu uzun ve narin kirişlerde Euler-Bernoulli teoreminin uygun sonuçlar verdiği, Timoshenko yaklaşımının tüm boyutlardaki kirişlerde yeterli ve doğru bir teori olduğu görülmektedir.

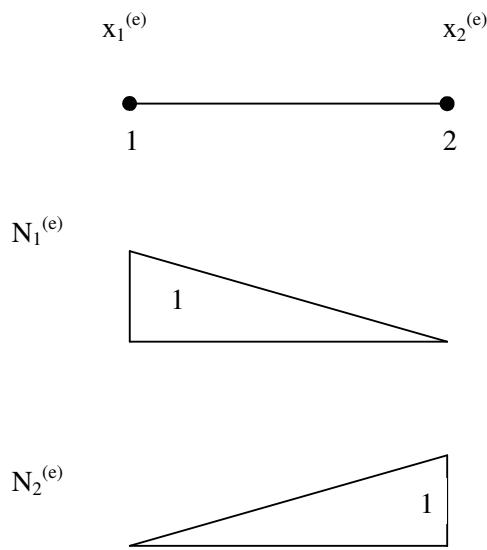
### 3.2 Doğrusal Elastik Timoshenko Kırışı için Sonlu Eleman Yaklaşımı

#### 3.2.1 Yer değiştirme ve şekil değiştirme

Hughes elemanında yanal yer değiştirme ( $w$ ):

$$w^{(e)} = N_1^{(e)} \cdot w_1^{(e)} + N_2^{(e)} \cdot w_2^{(e)} \quad (3.18)$$

olup burada  $w_1^{(e)}$  ve  $w_2^{(e)}$  Şekil(3.2)' de gösterilen elemanın 1 ve 2 düğüm noktalarındaki yanal yer değiştirmeleri göstermektedir.



**Şekil 3.2**

$x_1^{(e)}$  ve  $x_2^{(e)}$ : local düğüm noktaları 1 ve 2'nin x koordinatları,  $l^{(e)}$ : eleman uzunluğu,  
 $x^{(e)}$ : eleman üzerindeki bir noktanın x koordinatı olmak üzere,

$N_1^{(e)} = \frac{(x_2^{(e)} - x^{(e)})}{l^{(e)}}$  ve  $N_2^{(e)} = \frac{(x^{(e)} - x_1^{(e)})}{l^{(e)}}$  olarak yazılır. Benzer şekilde eleman içinde herhangi bir noktadaki  $\vartheta^{(e)}$  normal dönmesi

$$\vartheta^{(e)} = N_1^{(e)} \cdot \vartheta_1^{(e)} + N_2^{(e)} \cdot \vartheta_2^{(e)} \quad (3.19)$$

İle verilir. Burada  $\vartheta_1$  ve  $\vartheta_2$  1 ve 2 düğüm noktalarındaki normal dönmeleri gösterir. Eğrilik-yer değiştirmeye bağıntıları:

$$-\left(\frac{d\vartheta}{dx}\right)^{(e)} = -\left(\frac{dN_1}{dx}\right)^{(e)} \vartheta_1^{(e)} - \left(\frac{dN_2}{dx}\right)^{(e)} \vartheta_2^{(e)} \quad (3.20)$$

veya

$$\mathcal{E}_f^{(e)} = \begin{bmatrix} 0 & \frac{1}{l^{(e)}} & 0 & -\frac{1}{l^{(e)}} \end{bmatrix} \cdot \begin{bmatrix} w_1^{(e)} \\ \theta_1^{(e)} \\ w_2^{(e)} \\ \theta_2^{(e)} \end{bmatrix} = B_f^{(e)} \cdot \varphi^{(e)} \quad \text{şeklinde} \quad \text{yazılabilir. Burada}$$

$B_f^{(e)}$  eğrilik-yer değiştirmeye matrisidir. Kayma şekil değiştirmesi-yer değiştirmeye ilişkisi ise

$$\left(\frac{dw}{dx} - \vartheta\right)^{(e)} = \left(\frac{dN_1}{dx}\right)^{(e)} \cdot w_1^{(e)} - N_1^{(e)} \cdot \vartheta_1^{(e)} + \left(\frac{dN_2}{dx}\right)^{(e)} \cdot w_2^{(e)} - N_2^{(e)} \cdot \vartheta_2^{(e)} \quad (3.21)$$

veya

$$\mathcal{E}_s^{(e)} = \begin{bmatrix} -\frac{1}{l^{(e)}} & -\frac{(x_2^{(e)} - x^{(e)})}{l^{(e)}} & \frac{1}{l^{(e)}} & -\frac{(x^{(e)} - x_1^{(e)})}{l^{(e)}} \end{bmatrix} \cdot \begin{bmatrix} w_1^{(e)} \\ \vartheta_1^{(e)} \\ w_2^{(e)} \\ \vartheta_2^{(e)} \end{bmatrix} = B_s^{(e)} \cdot \varphi^{(e)}$$

olarak yazılabilir. Burada da  $B_s^{(e)}$  kayma şekil değiştirmesi-yer değiştirmeye matrisidir.

### 3.2.2 Rijitlik matrisinin teşkili

Önceki bölümde verilen eleman gerilme-şekil değiştirme ilişkilerini ve virtüel iş yaklaşımını kullanarak hakim denklem aşağıdaki gibi yazılabilir:

$$[K_f + K_s] \cdot \varphi - f = 0 \quad (3.22)$$

Burada (e) elemanı için  $K_f$ ,  $K_s$  v alt matrisleri ile f alt vektörü aşağıda verilmiştir:

$$\begin{aligned} K_f^{(e)} &= \int_{x_1^{(e)}}^{x_2^{(e)}} [B_f^{(e)}]^T \cdot (EI)^{(e)} \cdot B_f^{(e)} \cdot dx \\ K_s^{(e)} &= \int_{x_1^{(e)}}^{x_2^{(e)}} [B_s^{(e)}]^T \cdot (G\hat{A})^{(e)} \cdot B_s^{(e)} \cdot dx \\ f^{(e)} &= \int_{x_1^{(e)}}^{x_2^{(e)}} [N_1^{(e)} \quad 0 \quad N_2^{(e)} \quad 0]^T \cdot q \cdot dx \end{aligned} \quad (3.23)$$

Eğilme elemanına ait rijitlik matrisi bir boyutlu Gauss-Legendre Kuralı kullanılarak aşağıdaki gibi yazılabilir:

$$K_f^{(e)} = \left( \frac{EI}{l} \right)^{(e)} \cdot \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 0 & 0 \\ 0 & -1 & 0 & 1 \end{bmatrix} \quad (3.24)$$

$K_s$ 'yi de iki boyutlu Gauss-Legendre kuralına göre yazarsak;

$$K_s^{(e)} = \left( \frac{G\tilde{A}}{l} \right)^{(e)} \cdot \begin{bmatrix} 1 & \frac{l}{2} & -1 & \frac{l}{2} \\ \frac{l}{2} & \frac{l^2}{3} & -\frac{l}{2} & \frac{l^2}{6} \\ -1 & -\frac{l}{2} & l & -\frac{l}{2} \\ \frac{l}{2} & \frac{l^2}{6} & -\frac{l}{2} & \frac{l^2}{3} \end{bmatrix} \quad (3.25)$$

olur.

Bu formülasyonla fazla rijit sonuçlar elde edildiği gösterilebilir. Kilitlenme adı verilen bu sorun  $K_s^{(e)}$ ,yi bir boyutlu Gauss-Legendre kuralı ile elde ederek çözülmekte ve doğru sonuçlar elde edilebilmektedir:

$$K_s^{(e)} = \left( \frac{G\hat{A}}{l} \right)^{(e)} \begin{bmatrix} 1 & \frac{l}{2} & -1 & \frac{l}{2} \\ \frac{l}{2} & \frac{l^2}{4} & -\frac{l}{2} & \frac{l^2}{4} \\ -1 & -\frac{l}{2} & 1 & -\frac{l}{2} \\ \frac{l}{2} & \frac{l^2}{4} & -\frac{l}{2} & \frac{l^2}{4} \end{bmatrix} \quad (3.26)$$

Eşdeğer düğüm noktası kuvvet vektörü:

$$f^{(e)} = \begin{bmatrix} \frac{(ql)^{(e)}}{2} & 0 & \frac{(ql)^{(e)}}{2} & 0 \end{bmatrix} \quad (3.27)$$

dır. Burada Euler-Bernoulli kübik Hermitian elemanın aksine sadece yanal düğüm noktası kuvvetleri mevcuttur.

Tabakasız elastoplastik Timoshenko kırışının sonlu elemanlar yöntemiyle analizinde kiriş eğilme momenti plastikleşme momenti ( $M_0$ ) ‘a ulaştığında bütün sistem plastik hale gelir. Böyle durumlarda eğilme rijitliği  $EI$ , elastoplastik eğilme rijitliği  $(EI)_{ep}$  ile değiştirilir. Kesme rijitliği  $G\hat{A}$ ’nın ise değişmediği kabul edilir.

### 3.2.2.1 Kayma şekil değiştirmelerini dikkate alan çubuk rijitlik matrisi

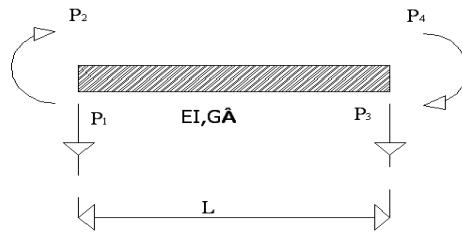
Bizim problemimize konu olan elastik zemine oturan tabakasız Timoshenko kirişinin çözümü için kullandığımız kayma şekil değiştirmelerini hesaba katan çubuk rijitlik matrisi aşağıdaki gibidir.

$$K_{e,k} = \begin{bmatrix} \frac{12EI}{l^3(1+\beta)} & \frac{6EI}{l^2(1+\beta)} & -\frac{12EI}{l^3(1+\beta)} & \frac{6EI}{l^2(1+\beta)} \\ \frac{6EI}{l^2(1+\beta)} & \frac{4EI(1+0.25\beta)}{l(1+\beta)} & -\frac{6EI}{l^2(1+\beta)} & \frac{2EI}{l} \cdot \frac{(1-0.5\beta)}{(1+\beta)} \\ -\frac{12EI}{l^3(1+\beta)} & -\frac{6EI}{l^2(1+\beta)} & \frac{12EI}{l^3(1+\beta)} & -\frac{6EI}{l^2(1+\beta)} \\ \frac{6EI}{l^2(1+\beta)} & \frac{2EI}{l} \cdot \frac{(1-0.5\beta)}{(1+\beta)} & -\frac{6EI}{l^2(1+\beta)} & \frac{4EI}{l} \cdot \frac{(1+0.25\beta)}{(1+\beta)} \end{bmatrix} \quad (3.27)$$

Burada  $\beta = \frac{12EI}{G\hat{A}l^2}$  dır. Elastik zemin etkilerini içeren rijitlik matrisi ise;

$$K_{el,ze\ min} = \begin{bmatrix} \frac{13}{35} \cdot K \cdot l & \frac{11}{210} \cdot K \cdot l^2 & \frac{9}{70} \cdot K \cdot l & -\frac{13}{420} \cdot K \cdot l^2 \\ \frac{11}{210} \cdot K \cdot l^2 & \frac{Kl^3}{105} & \frac{13}{420} \cdot K \cdot l^2 & -\frac{Kl^3}{140} \\ \frac{9}{70} \cdot K \cdot l & \frac{13}{420} \cdot K \cdot l^2 & \frac{13}{35} \cdot K \cdot l & -\frac{11}{210} \cdot K \cdot l^2 \\ -\frac{13}{420} \cdot K \cdot l^2 & -\frac{Kl^3}{140} & -\frac{11}{210} \cdot K \cdot l^2 & \frac{K \cdot l^3}{105} \end{bmatrix} \quad (3.28)$$

$$K = k_0(\text{yatık katsayı}) t/m^3 * b(\text{kiriş genişliği})$$



**Sekil 3.3**

Elastik zemin halinde iki matrisin toplamı kullanılacaktır.  $K=0$  halinde elastik yataklanmanın olmadığı açıkları.

### 3.2.3 Eleman iç kuvvetleri

(3.14) ve (3.15) denklemleri yardımıyla her bir eleman için eğilme momentini ve kesme kuvvetlerini hesaplayabileceğimiz ifadeleri elde edebiliriz.

Her eleman için sabit olan eğilme momenti

$$M^{(e)} = (EI)^{(e)} \cdot B_f^{(e)} \cdot \varphi^{(e)} = (EI)^{(e)} \cdot \begin{bmatrix} 0 & \frac{1}{l^{(e)}} & 0 & -\frac{1}{l^{(e)}} \end{bmatrix} \cdot \begin{bmatrix} w_1^{(e)} \\ v_1^{(e)} \\ w_2^{(e)} \\ v_2^{(e)} \end{bmatrix} = \left(\frac{EI}{l}\right)^{(e)} \cdot (v_1^{(e)} - v_2^{(e)}) \quad (3.29)$$

İfadesi ile bulunur. Kesme kuvveti her elemanda doğrusal olarak değişir, fakat bir yaklaşım olarak kesme kuvvetinin eleman ortasındaki ( $x = \frac{x_1^{(e)} + x_2^{(e)}}{2}$ ) değeri alınıp kesme kuvvetinin eleman boyunca bu değere eşit olduğu varsayılmaktır. Kesme kuvveti aşağıdaki bağıntı ile elde edilir:

$$Q^{(e)} = (G\hat{A})^{(e)} \cdot B_s^{(e)} \cdot \varphi^{(e)} = (G\hat{A})^{(e)} \cdot \begin{bmatrix} -\frac{1}{l^{(e)}} & -\frac{1}{2} & \frac{1}{l^{(e)}} & -\frac{1}{2} \end{bmatrix} \cdot \begin{bmatrix} w_1^{(e)} \\ v_1^{(e)} \\ w_2^{(e)} \\ v_2^{(e)} \end{bmatrix} \quad (3.30)$$

$$= (G\hat{A})^{(e)} \cdot \left\{ \left( \frac{w_2^{(e)} - w_1^{(e)}}{l^{(e)}} \right) - \left( \frac{v_1^{(e)} + v_2^{(e)}}{2} \right) \right\}$$

### 3.3 Elastoplastik Timoshenko Kırışları

#### 3.3.1 Akma momenti

Eğilme momenti etkisinde bir Timoshenko kırışını göz önüne alalım. Timoshenko yaklaşımına göre eksenel gerilme ve eksenel şekil değiştirme kesitin derinliği boyunca doğrusal olarak değişir. Eğilme momentinin artmasıyla beraber kesitin alt ve üst başlıklarındaki liflerde plastikleşme meydana gelir ve yükün biraz daha artmasıyla beraber plastikleşme tüm kesit plastikleşene kadar kesitin diğer kısımlarına da yayılmaya başlar. Sonunda en kesit tam plastik hale gelir.  $\sigma_x$  ve  $\tau_{xz}$ 'in etkileşimi kesitin akması boyunca ihmal edilmiştir. Bu ihmal doğru olmamakla beraber özellikle ince kırışlerde fark çok azdır.

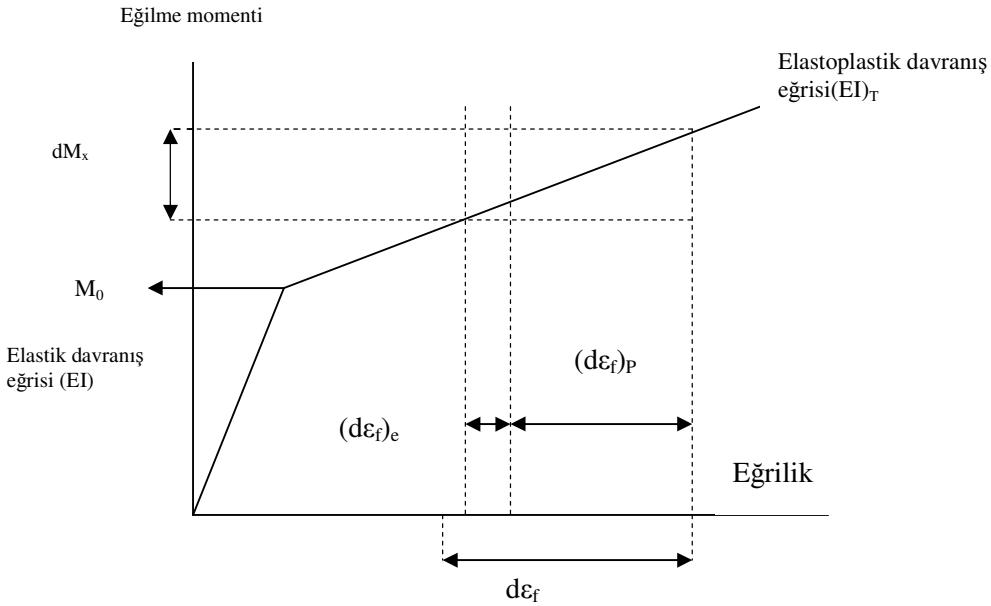
Tamamıyla plastikleşmiş kesitte meydana gelen limit momentin değeri, akma gerilmesi  $\sigma_0$  cinsinden hesaplanabilir:

$$M_0 = \int_{b(-t/2)}^{b(t/2)} \int_{-t/2}^{t/2} z \sigma_0 dz dy \quad (3.31)$$

Bu değer genişliği b olan bir dikdörtgen kırış için  $M_0 = \sigma_0 \cdot \left( bt^2 / 4 \right)$  dir.

#### 3.3.2 Elastoplastik eğilme

Önceki bölümlerde belirtildiği gibi elastoplastik davranış, başlangıçta elastik davranış gösteren malzemenin artan gerilme ile eğilme momenti akma momenti değerini geçtiğinde oluşan plastik şekil değiştirmeler ile tanımlanır. Plastik şekil değiştirme yüklemenin kaldırılmasıyla geri dönmez ve plastik şekil değiştirmenin başlaması akma kriteri ile belirlenir. Pekleşme anında malzeme rıjitiğinde ciddi bir azalma görülür.



**Şekil 3.4:** Elastoplastik davranış

Elastoplastik malzemeli bir Timoshenko kırışı için moment-eğrilik ilişkisi yukarıda Şekil(3.4)'te görülmektedir. Kırış başlangıçta eğilme rijitliğine ( $EI$ ) bağlı olarak elastik bir şekilde şekil değiştirir. Bu deformasyon eğilme momentinin tüm kesitin plastikleştiği aşamadaki değerine gelmesine kadar sürer.

Yükün biraz daha arttırılmasıyla malzemenin teğetsel eğilme rijitliği ( $EI_T$ ) ile tanımlanan doğrusal plastik davranış gözlenir. Akma sınırı geçildikten sonra ilave bir yük artımı olduğunda bu artış eğilme momentinde eğriliğin değişimiyle sonuçlanan bir artış ( $d\epsilon_f$ ) meydana getirir. Eğriliği elastik ve plastik olmak üzere ikiye ayırsak;

$$d\epsilon_f = (d\epsilon_f)_e + (d\epsilon_f)_p \quad (3.32)$$

Bu durumda pekleşme parametresi  $H' = \frac{dM}{(d\epsilon_f)_p}$  olarak tanımlanabilir. Bu

parametrenin değeri elastik eğrilik kısmının çıkarılmasından sonra moment-eğrilik grafiğinin plastik kısmının eğimi olarak tanımlanabilir.

$$H' = \frac{dM}{d\epsilon_f - (d\epsilon_f)_e} = \frac{(EI)_T}{1 - \left[ \frac{(EI)_T}{EI} \right]} \quad (3.33)$$

(3.31) bağıntısı biraz daha düzenlenirse

$$d\epsilon_f = \frac{dM}{EI} + \frac{dM}{H'} = \frac{dM(H' + EI)}{EI \cdot H'} \quad (3.34)$$

ve artımsal moment-eğilme ilişkisi aşağıdaki gibi yazılabilir:

$$dM = \frac{EI \cdot H'}{(EI + H')} \cdot d\epsilon_f \quad (3.35)$$

Akma esnasında artımsal gerilme-şekil değiştirme bağıntısı

$$dM = EI \left( 1 - \frac{EI}{EI + H'} \right) \cdot d\epsilon_f \quad (3.36)$$

$$dQ = G\hat{A} \cdot d\epsilon_s$$

olur. Moment-eğrilik ilişkisinin elastoplastik olmasına karşılık kesme kuvveti-kayma gerilmesi ilişkisi her zaman elastiktir. Akmadan sonra eğilme rijitliği aşağıdaki değerle değiştirilecektir.

$$EI \left( 1 - \frac{EI}{EI + H'} \right)$$

Pekleşme parametresi  $H'$  malzeme davranışını perfekt elastoplastik olduğunda sıfır eşit olur. Bu durumda elastoplastik çubuk eleman teğetsel rijitlik matrisi tekil olur. Bu güçlük başlangıç rijitlik yöntemi kullanılarak yenilir.

### 3.3.3 Lineer olmayan denklemlerin çözümü

Elemana ait yanal yer değiştirmeleri, dönme, eğrilik ve kayma şekil değiştirmelerini bulabilmek için doğrusal olmayan denge denklemleri virtüel iş prensibi yardımıyla genelleştirilebilir. Sonlu eleman ağının herhangi bir noktasındaki yanal yer değiştirme ve dönmeler aşağıdaki ifade ile elde edilebilir:

$$\begin{bmatrix} w \\ \vartheta \end{bmatrix} = N \cdot \varphi \quad (3.37)$$

Buradaki şekil fonksiyonu matrisi N,

$$N = \begin{bmatrix} N_1, 0, N_2, 0, \dots, N_n, 0 \\ 0, N_1, 0, N_2, \dots, 0, N_n \end{bmatrix} \quad (3.38)$$

ve düğüm noktası yer değiştirmeleri vektörü  $\varphi$ ,

$$\varphi = [w_1, \theta_1, w_2, \theta_2, \dots, w_n, \theta_n]^T \quad (3.39)$$

Yukarıdaki denklemlerde  $w$  yanal yer değiştirmeyi,  $\theta$  dönmeyi,  $N_i$  herhangi bir düğüm noktasına ait global şekil fonksiyonunu temsil etmektedir. Sonlu eleman sisteminin tamamı için herhangi bir noktadaki eğrilik ve kayma şekil değiştirmesi ise

$$-\frac{d\theta}{dx} = B_f \cdot \varphi \quad \text{ve} \quad \frac{dw}{dx} - \theta = B_s \cdot \varphi \quad (3.40)$$

olarak gösterilebilir. Burada

$$B_f = \left[ 0, -\frac{dN_1}{dx}, 0, -\frac{dN_2}{dx}, \dots, 0, -\frac{dN_n}{dx} \right] \quad (3.41)$$

$$B_s = \left[ \frac{dN_1}{dx}, -N_1, \frac{dN_2}{dx}, -N_2, \dots, \frac{dN_n}{dx}, -N_n \right] \quad (3.42)$$

Virtüel eğrilikler ve kayma şekil değiştirmeleri sırasıyla aşağıdaki gibidir.

$$-\frac{d(\delta\theta)}{dx} = B_f \cdot \delta\varphi \quad \text{ve} \quad \frac{d(\delta w)}{dx} - \delta\theta = B_s \cdot \delta\varphi \quad (3.43)$$

Düğüm noktası virtüel yer değiştirmeleri vektörü de

$$\delta\varphi = [\delta w_1, \delta\theta_1, \delta w_2, \delta\theta_2, \dots, \delta w_n, \delta\theta_n]^T \quad (3.44)$$

olarak yazılır. Virtüel iş prensibi kullanılarak

$$\int_0^l [\delta\varphi]^T \cdot [B_f]^T \cdot M \cdot dx + \int_0^l [\delta\varphi]^T \cdot [B_s]^T \cdot Q \cdot dx - \int_0^l [\delta\varphi]^T \cdot [\bar{N}]^T \cdot q \cdot dx = 0 \quad (3.45)$$

olur. Burada  $\bar{N}$  ;

$$\bar{N} = [N_1, 0, N_2, 0, \dots, N_n, 0] \quad (3.46)$$

dir. (3.45) eşitliği virtüel yer değiştirmelerin ( $\delta\varphi$ ) her bir değeri için doğru olmalıdır. Bunun sonucunda denklem aşağıdaki hali alır:

$$\left\{ \int_0^l [B_f]^T \cdot M \cdot dx + \int_0^l [B_s]^T \cdot Q \cdot dx \right\} - \int_0^l [\bar{N}]^T \cdot q \cdot dx = 0 \quad (3.47)$$

Veya  $p - f = 0$  olarak da yazılabilir. Bu eşitlik aslında plastikliğin söz konusu olmadığı (3.22) eşitliğine özdeştir.

Elastoplastik problemlerde  $M$  doğrusal olmayan bir fonksiyondur ve genellikle  $p$  vektörü ancak yaklaşık olarak bulunur. Bu yüzden (3.47) eşitliği doğrusal olmadığından ve  $p$  yaklaşık olarak bilinebildiğinden ( $p-f$ ) değeri artık bir  $\psi(\varphi)$  değerine eşit olacaktır.

Bir e elemanın  $p$ 'ye yaptığı katkıyı genel biçimde gösterirsek,

$$\begin{aligned}
 p^{(e)} &= \int_{x_1^{(e)}}^{x_2^{(e)}} \begin{bmatrix} 0 \\ \frac{1}{l^{(e)}} \\ 0 \\ -\frac{1}{l^{(e)}} \end{bmatrix} \cdot M^{(e)} \cdot dx + \int_{x_1^{(e)}}^{x_2^{(e)}} \begin{bmatrix} -\frac{1}{l^{(e)}} \\ \frac{x^{(e)} - x_2^{(e)}}{l^{(e)}} \\ \frac{1}{l^{(e)}} \\ \frac{x_1^{(e)} - x^{(e)}}{l^{(e)}} \end{bmatrix} \cdot Q^{(e)} \cdot dx \\
 &= \left[ -Q^{(e)}, M^{(e)} - \frac{(Ql)^{(e)}}{2}, Q^{(e)}, -M^{(e)} - \frac{(Ql)^{(e)}}{2} \right]^T
 \end{aligned} \tag{3.48}$$

### 3.4 Elastoplastik Tabakalı Timoshenko Kırışları

#### 3.4.1 Tabakalı kırışlerde akma

Tabakalı yaklaşımda kırış yüksekliği boyunca seçilen bir tabaka sayısına bölünür. Sonlu eleman yaklaşımında dıştaki tabakaların ortasındaki gerilme akma değerine ulaşır ulaşmaz bu tabaka plastikleşir, kesitin geri kalan kısmı elastiktir. Yük arttıkça plastikleşme iç tabakalara doğru devam eder ve tüm kesit plastikleşene kadar devam eder.

#### 3.4.2 Tabakalı kırış için rijitlik matrisinin oluşturulması

Tabakalı yaklaşımda, tabakasız yaklaşımda olduğu gibi iç kuvvetler cinsinden değil gerilmeler cinsinden çalışılır. Bir tabakanın ortasındaki gerilme değeri o tabakanın tamamı için mukayese gerilmesi olarak varsayılar. İç kuvvetlerin ( $M$  ve  $Q$ ) katkıları, her tabaka için tabakanın kalınlığı üzerinde integrasyon yapılarak ayrı ayrı bulunur. Daha sonra her tabakaya ait katkılar eklenerek kırışın tamamına ait eğilme momentleri ve kesme kuvvetleri elde edilir.

Yer değiştirme alanı, gerilme-şekil değiştirme ilişkisi ve şekil değiştirme-yer değiştirme ilişkisi bu bölümün başında (3.1)-(3.10) bağıntıları ile verilmiştir.

**(3.11)** denkleminde verilen virtüel iş prensibinden, orta nokta kuralı kullanılarak eğilme momenti ( $M$ ) ve kesme kuvveti ( $Q$ ) değerleri bulunur:

$$M = EI \left( -\frac{d\theta}{dx} \right) \quad \text{ve} \quad Q = G\hat{A} \cdot \varepsilon_s \quad (3.49)$$

Burada;

$$EI = \sum_i E_i \cdot b_i \cdot z_i^2 \cdot t_i \quad (3.50)$$

ve

$$G\hat{A} = \sum_i G_i \cdot b_i \cdot t_i \quad (3.51)$$

Yukarıdaki ifadelerde;

$b_i$ : tabaka genişliği

$t_i$ : tabaka kalınlığı

$z_i$ : tabakanın orta noktasına ait z koordinatı

$E_i$ : tabaka malzemesinin elastisite modülü

$G_i$ : tabaka malzemesinin kayma modülünü göstermektedir.

Eğer tabakanın ortasındaki gerilme değeri tabaka malzemesinin tek eksenli akma gerilmesi değerine ulaşırsa bütün tabakanın plastikleştiği kabul edilir ve  $E_i$  değeri aşağıdaki gibi değiştirilir:

$$E_i \left( 1 - \frac{E_i}{E_i + H'} \right)$$

### 3.4.3 Lineer olmayan denklemlerin çözümü

**(3.11)** eşitliği tekrar yazılırsa

$$\int_0^l \int_{-t/2}^{t/2} \int_{b(-t/2)}^{b(t/2)} \left( -z \cdot \frac{d(\delta\theta)}{dx} \cdot \sigma_x + \delta\beta \cdot \tau_{xz} \right) \cdot dy \cdot dz \cdot dx - \int_0^l \delta W \cdot q \cdot dx = 0 \quad (3.52)$$

olur. İlk iki integralin elde edilebilmesi için orta nokta kuralı kullanılırsa

$$[\delta\varphi]^T \cdot [P_f + P_s] - [\delta\varphi]^T \cdot f = 0 \quad (3.53)$$

yazılır. Burada  $P_f$  ve  $P_s$  ifadeleri aşağıda verilmiştir.

$$P_f = \int_0^l [B_f]^T \cdot \bar{M} \cdot dx \quad \text{ve} \quad P_s = \int_0^l [B_s]^T \cdot \bar{Q} \cdot dx$$

Burada  $B_f$ ,  $B_s$  ve  $\delta\varphi$  sırasıyla (3.41), (3.43) ve (3.44) denklemlerinde gösterilmiştir.

$$\bar{M} \text{ ve } \bar{Q}$$

$$\bar{M} = \sum_i b_i \cdot \sigma_{xi} \cdot z_i \cdot t_i \quad (3.54)$$

$$\bar{Q} = \sum_i b_i \cdot \tau_{xzi} \cdot t_i \quad (3.55)$$

dir. (3.52) eşitliği virtüel yer değiştirmelerin herhangi bir durumu için doğru olduğundan

$$p_f + p_s - f = 0 \quad (3.56)$$

yazılabilir. Her bir elemanın  $p_f$  ve  $p_s$  'e olan katkıları ayrı ayrı aşağıda gösterildiği gibi elde edilebilir:

$$p_f^{(e)} = \int_{x_1^{(e)}}^{x_2^{(e)}} [Bf^{(e)}]^T \cdot \bar{M}^{(e)} \cdot dx = \int_{x_1^{(e)}}^{x_2^{(e)}} \left[ 0 \quad \left( \frac{\bar{M}}{l} \right)^{(e)} \quad 0 \quad -\left( \frac{\bar{M}}{l} \right)^{(e)} \right]^T dx = \begin{bmatrix} 0 & \bar{M}^{(e)} & 0 & -\bar{M}^{(e)} \end{bmatrix}^T$$

(3.57)

$$\begin{aligned}
 p_s^{(e)} &= \int_{x_1^{(e)}}^{x_2^{(e)}} [B_s^{(e)}]^T \cdot \bar{Q}^{(e)} \cdot dx = \int_{x_1^{(e)}}^{x_2^{(e)}} \begin{bmatrix} -\frac{1}{l^{(e)}} & -\frac{1}{2} & \frac{1}{l^{(e)}} & -\frac{1}{2} \end{bmatrix}^T \cdot \bar{Q}^{(e)} \cdot dx \\
 &= \begin{bmatrix} -\bar{Q}^{(e)} & -\frac{(\bar{Q}l)^{(e)}}{2} & \bar{Q}^{(e)} & -\frac{(\bar{Q}l)^{(e)}}{2} \end{bmatrix}^T
 \end{aligned}$$

(3.58)



## **4. PROBLEMLERİN ÇÖZÜMÜNDE KULLANILAN BİLGİSAYAR PROGRAMLARINA AİT BİLGİLER**

Timoshenko kırışlerinin elastoplastik analizi için tabakalı ve tabakasız olmak üzere iki yaklaşım mevcuttur. Problemlerin iki yaklaşım için farklı çözümlerini kolaylaştmak üzere tabakalı yaklaşım için TIMLAY ve tabakasız yaklaşım için TIMOSH başlıklar altında düzenlenmiş FORTRAN programları kullanılmıştır. Bizim problemimizin çözümü için tabakasız yaklaşım durumuna elastik zemin özelliklerini de hesaba katan ilaveler yapılmıştır. Bu kısımlar koyu font ile ayrılmıştır. Gerekli olan yerlerde programların özgün halleri bölüm sonunda verilmiştir.

### **4.1 Tabakasız Kırış Programı (TIMOSH)**

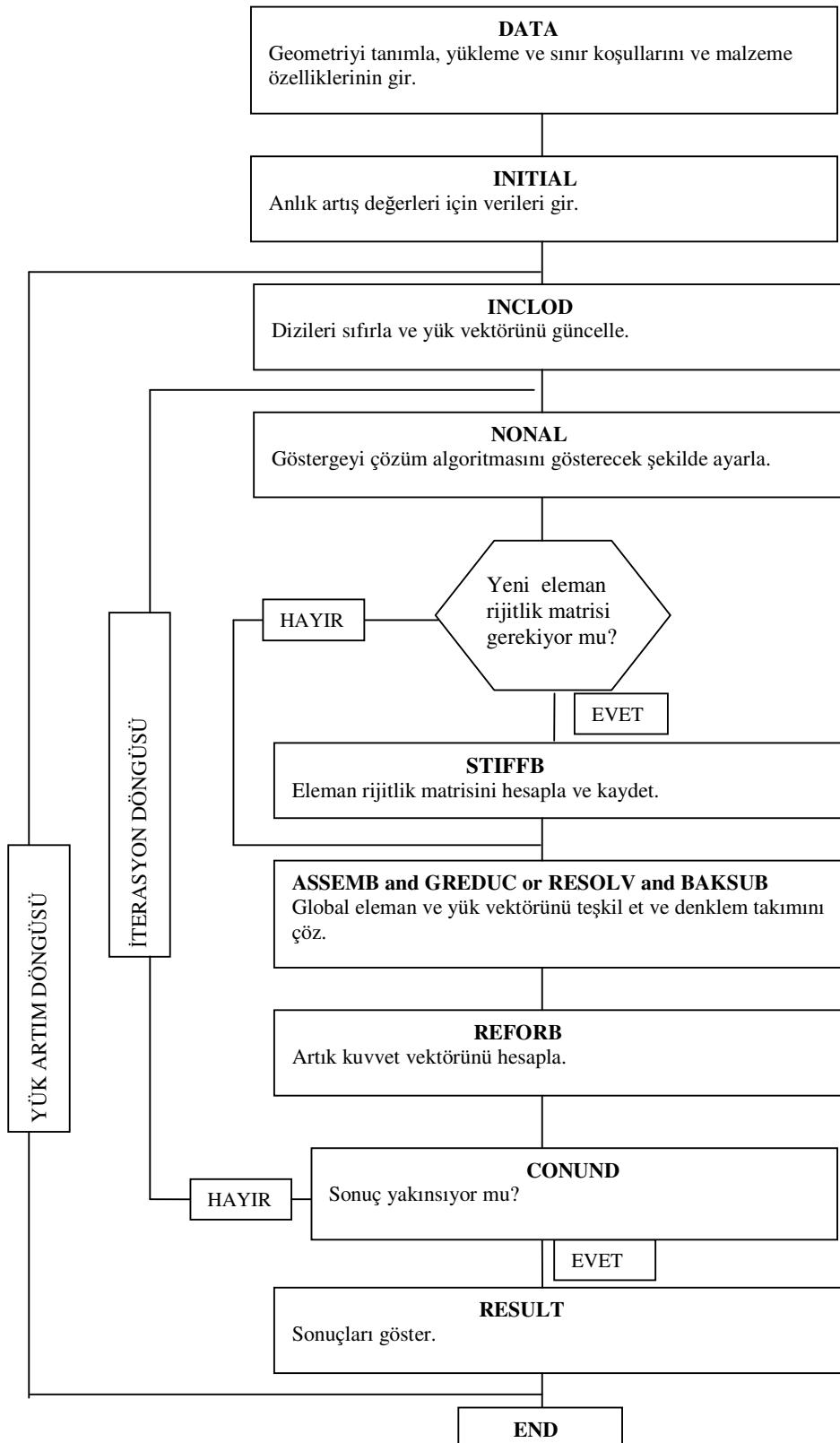
Tabakasız yaklaşım için kullanılmış olan ana program MASTER BEAM aşağıdaki gibidir.

#### **PROGRAM MASTER BEAM**

```
C*****
C   ELASTOPLASTIC NONLAYERED TIMOSHENKO BEAM PROGRAM WITH ELASTIC
C   FOUNDATION
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
.           KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
.           NITER,NOUTP,FACTO,PVALU,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
.           FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
.           MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
.           TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
.           REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
CALL DATA
CALL INITIAL
DO 30 IINCS=1,NINCS
CALL INCLOD
DO 10 IITER=1,NITER
```

```
CALL NONAL
IF(KRESL.EQ.1) CALL STIFFB
CALL ASSEMB
IF(KRESL.EQ.1)CALL GREUDC
IF(KRESL.EQ.2)CALL RESOLV
CALL BAKSUB
CALL REFORB
CALL CONUND
IF(NCHEK.EQ.0) GOTO 20
IF(IITER.EQ.1.AND.NOUTP.EQ.1) CALL RESULT
IF(NOUTP.EQ.2) CALL RESULT
10  CONTINUE
      WRITE(6,900)
900  FORMAT(1H0,5X,"SOLUTION NOT CONVERGED")
      STOP
20  CALL RESULT
30  CONTINUE
      STOP
      END
```

TIMOSH programının yapısı bir akış diyagramıyla gösterilecek olursa;



**Şekil 4.1:** TIMOSH programı akış diyagramı.

Şekil (4.1)'de görüldüğü gibi ana programın çalıştırılması için Data, Initial, Increm, Nonal, StiffB, Assemb, Greduc, Resolv, Baksub, Reforb, Conund ve Result alt programları kullanılmıştır. Sırasıyla işlevleri ve detaylı yapıları gösterilecek olursa;

#### 4.1.1 Subroutine DATA

```
C*****
C
C      INPUTS DATA DEFINING GEOMETRY LOADING BOUNDARY CONDITIONS ETC
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
.          KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
.          NITER,NOUTP,FACTO,PVALU,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
.          FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
.          MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
.          TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
.          REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
DIMENSION ICODE(2),VALUE(2),TITLE(18)
READ(5,965)TITLE
WRITE(6,965)TITLE
965  FORMAT(18A4)
READ(5,900)NPOIN,NELEM,NBOUN,NMATS,NPROP,NNODE,NINCS,NALGO,
.          NDOFN
900  FORMAT(9I5)
WRITE(6,905)NPOIN,NELEM,NBOUN,NMATS,NPROP,NNODE,NINCS,NALGO,
.          NDOFN
905  FORMAT(1X,"NPOIN=",I5,3X,"NELEM=",I5,3X,"NBOUN=",I5,3X,
.          "NMATS=",I5//1X,"NPROP=",I5,3X,"NNODE=",I5,3X,
.          "NINCS=",I5,3X,"NALGO=",I5//1X,"NDOFN=",I5)
NEVAB=NDOFN*NNODE
NSVAB=NDOFN*NPOIN
WRITE(6,910)
910  FORMAT(1H0,5X,'MATERIAL PROPERTIES')
DO 10 IMATS=1,NMATS
READ(5,915) JMATS,(PROPS(JMATS,IPROP),IPROP=1,NPROP)
10   WRITE(6,915) JMATS,(PROPS(JMATS,IPROP),IPROP=1,NPROP)
915  FORMAT(I10,4F15.5)
WRITE(6,920)
920  FORMAT(1H0,3X,"EL NODES MAT.")
DO 20 IELEM=1,NELEM
READ(5,925) JELEM,(LNODS(JELEM,INODE),INODE=1,NNODE),MATNO(JELEM)
20   WRITE(6,925) JELEM,(LNODS(JELEM,INODE),INODE=1,NNODE),MATNO(JELEM)
925  FORMAT(4I5)
WRITE(6,930)
930  FORMAT(1H0,5X,"NODE",5X,"COORD.")
DO 30 IPOIN=1,NPOIN
READ(5,935) JPOIN,COORD(JPOIN)
30   WRITE(6,935) JPOIN,COORD(JPOIN)
935  FORMAT(I10,F15.5)
DO 40 ISVAB=1,NSVAB
IFPRE(ISVAB)=0
40   PEFIX(ISVAB)=0.0
IF(NDOFN.EQ.1) WRITE(6,940)
940  FORMAT(1H0,1X,"RES.NODE",2X,"CODE",3X,"PRES.VALUES")
```

```

IF(NDOFN.EQ.2) WRITE(6,945)
945  FORMAT(1H0,1X,"RES.NODE",2X,"CODE",3X,"PRES.VALUES",2X,
         ."CODE",3X,"PRES.VALUES")
         DO 50 IBOUN=1,NBOUN
         READ(5,950) NODFX,(ICODE(IDOFN),VALUE(IDOFN),IDOFN=1,NDOFN)
         WRITE(6,950) NODFX,(ICODE(IDOFN),VALUE(IDOFN),IDOFN=1,NDOFN)
950  FORMAT( I10,2(I5,F15.5))
         NPOSN=(NODFX-1)*NDOFN
         DO 50 IDOFN=1,NDOFN
         NPOSN=NPOSN+1
         IFPRE(NPOSN)=ICODE(IDOFN)
50    PEFIX(NPOSN)=VALUE(IDOFN)
         WRITE(6,955)
955  FORMAT(1H0,2X,"ELEMENT",10X,"NODAL LOADS")
         DO 60 IELEM=1,NELEM
         DO 60 IEVAB=1,NEVAB
60    RLOAD(IELEM,IEVAB)=0.0
70    READ(5,960)JELEM,(RLOAD(JELEM,IEVAB),IEVAB=1,NEVAB)
         IF(JELEM.NE.NELEM) GO TO 70
         DO 80 IELEM=1,NELEM
80    WRITE(6,960) IELEM,(RLOAD(IELEM,IEVAB),IEVAB=1,NEVAB)
         READ(5,970) EZK
970  FORMAT(E15.6)
         WRITE(6,971) EZK
971  FORMAT(" ELASTIC SOIL COEFFICIENT= ",E15.6)
960  FORMAT(I10,5F15.5)
         RETURN
         END

```

Herhangi bir sonlu eleman analizinde veri girişi 3 ana gruba bölünebilir. Birinci olarak yapının geometrisi ve mesnetlenme durumu veri olarak girilmeli, ikinci olarak malzeme özellikleri tanımlanmalı, üçüncü ve son olarak da yükleme durumlarını veren veri girişi sağlanmalıdır.

Veri girişi için kullanılan Subroutine Data alt programındaki kontrol parametrelerini kısaca açıklayacak olursak;

**NPOIN:** Yapıdaki toplam düğüm noktası sayısı,

**NELEM:** Yapıdaki toplam eleman sayısı,

**NBOUN:** Sınır koşullarının sayısı,

**NMATS:** Yapıdaki farklı malzemelerin toplam sayısı,

**NPROP:** Malzeme karakteristiğini tam olarak belirleyebilmek için gereken malzeme parametresine ait numara.

4-Elastoplastik problemler için

2-Diğer tüm uygulamalar için kullanılacak değer.

**NNODE:** Her bir eleman için düğüm sayısı,

**NINCS:** Tüm yükleme boyunca yapılan yük artımlarının sayısı,

**NALGO:** Problemin çözümü için kullanılacak çözüm algoritmasını tanımlayan gösterge.

- 1- Doğrudan iterasyon yöntemi
- 2- Newton-Raphson yöntemi (Quasiharmonik problemler için.)  
Teğetsel rijitlik yöntemi (Lineer olmayan elastik ve elastoplastik problemler için.)
- 3-Başlangıç rijitliği yöntemi.
- 4-Sadece bir yük artımı için ilk iterasyonda rijitliğin yeniden hesaplandığı durumlar için başlangıç rijitliği ve teğetsel rijitlik yöntemlerinin kombinasyonunun kullanıldığı durumlar.
- 5-Rijitliğin ikinci iterasyonda yeniden hesaplandığı durumlar için başlangıç ve teğetsel rijitlik yöntemlerinin kombinasyonunun kullanıldığı durumlar.

**NDOFN:** Her bir düğüm noktası için serbestlik derecelerinin değeri.

- 1-Tek eksenli problemler için.
- 2-Timoshenko kirişleri için.

**COORD(IPOIN):** Her bir düğüm noktasının koordinatı referans eksen takımına göre tanımlanmalıdır. COORD ile koordinat, IPOIN ile düğüm noktalarının sayısı tanımlanır.

**LNODS(NUME, INODE):** Her bir elemanın geometrisini düğüm noktası sayısına bağlı tanımlamak için kullanılır. Burada NUMEL göz önüne alınan eleman sayısını belirtir. INODE ise 1'den NNODE(toplam düğüm noktası sayısı)'na kadar değişir.

**MATNO(NUMEL):** Her eleman malzeme özellikleri bakımından farklı olabileceğine için bu farklılıklarını tanımlayıcı olarak kullanılır. Burada eleman numarasını NUMEL

temsil eder ve MATNO(NUMEL) belirtilen numaralı elemanın farklı bir malzeme özelliğine sahip olduğunu gösterir.

**PROPS(NUMAT, IPROP):** Çözüm için gerekli olan malzeme özellikleri farklı uygulamalarda değişiklik gösterir. Burada NUMAT malzeme numarasını ve IPROP o malzemenin özelliklerini belirtir. Elastoplastik problemler için;

PROPS(NUMAT,1)-Malzemenin elastisite modülünü,

PROPS(NUMAT,2)-Elemanın kesit alanını,

PROPS(NUMAT,3)-Malzemenin tek eksenli akma gerilmesini,

PROPS(NUMAT,4)-Malzeme için lineer pekleşme parametresini ( $H'$ ) temsil etmektedir.

**ICODE(IDOFN):** İlgili düğüm noktasında hangi dereceden serbestlik değerinin atanacağını belirlemek için kullanılır.

**VALUE(IDOFN):** Serbestlik derecesinin değerini tanımlar.

**RLOAD(IELEM, IEVAB):** Yapıya ve dolayısıyla elemanlara uygulanan yükleri tanımlamak için kullanılır.

**EZK( $t/m^2$ ):** Elastik zemin katsayısı. Yatak katsayısı ( $k_0$ ) ile kiriş genişliğinin ( $b$ ) çarpımına eşit olan katsayı ( $K$ ).

#### 4.1.2 Subroutine INITIAL

```
C*****
C
C           INITIALIZES TO ZERO ALL ACCUMULATIVE ARRAYS
C
C*****
COMMON/UNIM1/NPOIN, NELEM, NBOUN, NLOAD, NPROP, NNODE, IINCS, IIITER,
.          KRESL, NCHEK, TOLER, NALGO, NSVAB, NDOFN, NINCS, NEVAB,
.          NITER, NOUTP, FACTO, PVALU, EZK
COMMON/UNIM2/PROPS(5,4), COORD(26), LNODS(25,2), IFPRE(52),
.          FIXED(52), TLOAD(25,4), RLOAD(25,4), ELOAD(25,4),
.          MATNO(25), STRES(25,2), PLAST(25), XDISP(52),
.          TDISP(26,2), TREAC(26,2), ASTIF(52,52), ASLOD(52),
.          REACT(52), FRESV(1352), PEFIG(52), ESTIF(4,4)
DO 20 IELEM=1,NELEM
PLAST(IELEM)=0.0
DO 10 IDOFN=1,NDOFN
```

```

10   STRES(IELEM,IDOFN)=0.0
    DO 20 IEVAB=1,NEVAB
      ELOAD(IELEM,IEVAB)=0.0
20   TLOAD(IELEM,IEVAB)=0.0
    DO 30 IPOIN=1,NPOIN
      DO 30 IDOFN=1,NDOFN
        TDISP(IPOIN,IDOFN)=0.0
30   TREAC(IPOIN,IDOFN)=0.0
    RETURN
    END

```

INITIAL yardımcı programının fonksiyonu diğer yardımcı programlar tarafından da kullanılan bazı dizilerin değerini sıfırlamaktır.

#### 4.1.3 Subroutine INCLOD

```

C*****
C
C     INPUTS DATA FOR CURRENT INCREMENT AND UPDATES LOAD VECTOR
C
C*****
COMMON/UNIM1/NPOIN, NELEM, NLOAD, NPROP, NNODE, IINCS, IITER,
       KRESL, NCHEK, TOLER, NALGO, NSVAB, NDOFN, NINCS, NEVAB,
       NITER, NOUTP, FACTO, PVALU, EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
       FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
       MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
       TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
       REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
READ(5,900) NITER, NOUTP, FACTO, TOLER
900 FORMAT(2I5,2F15.5)
      WRITE(6,905) IINCS, NITER, NOUTP, FACTO, TOLER
905 FORMAT(1H0,5X,"IINCS=",I5,3X,"NITER=",I5,3X,"NOUTP=",I5,
       3X,"FACTO=",E14.6,3X,"TOLER=",E14.6)
      DO 10 IELEM=1,NELEM
      DO 10 IEVAB=1,NEVAB
        ELOAD(IELEM, IEVAB)=ELOAD(IELEM, IEVAB)+RLOAD(IELEM, IEVAB)*FACTO
        TLOAD(IELEM, IEVAB)=TLOAD(IELEM, IEVAB)+RLOAD(IELEM, IEVAB)*FACTO
10   CONTINUE
      RETURN
      END

```

INCLOD yapıya uygulanan yüklerin artımını kontrol eden alt programdır. Her yük artımında iterasyonun üst limitlerine göre bu veri kontrol edilir. Çıktı sıklığı, yük artımının miktarı ve tolerans limitine yakınsama değerlendirme kriterleridir. Bu görevleri programa yaptıran terimler;

**NITER:** İzin verilebilir en fazla iterasyon sayısı. Bu çözüm süreci yakınsamadığında problemin çözümü açısından koruyucu bir önlemidir. Niter iterasyon döngüsü tamamlandıktan sonra program sona erer.

**NOUTP:** Çıktı sonuçlarının sıklığını kontrol eden parametredir. Kullanıcının çıktı almak istediği aşamalara göre değişir;

- 0- Her yük artımında ancak lineer olmayan çözüm için yakınsama olduğunda sonuçları bas.
- 1- İlk iterasyondan sonra ve her yük artımı için yakınsama olduğunda sonuçları bas.
- 2- Her yük artımında ve her iterasyondan sonra sonuçları bas.

**FACTO:** Yük artımının büyüklüğünü kontrol eden parametredir.

**TOLER:** Yakınsama için izin verilen toleransı kontrol eden parametredir.

#### 4.1.4 Subroutine NONAL

```
C*****
C
C      SETS INDICATOR TO IDENTIFY_TYPE OF SOLUTION ALGORITHM
C
C*****
COMMON/UNIM1/NPOIN, NELEM, NBOUN, NLOAD, NPROP, NNODE, IINCS, IIITER,
.           KRESL, NCHEK, TOLER, NALGO, NSVAB, NDOFN, NINCS, NEVAB,
.           NITER, NOUTP, FACTO, PVALU, EZK
COMMON/UNIM2/PROPS(5,4), COORD(26), LNODS(25,2), IFPRE(52),
.           FIXED(52), TLOAD(25,4), RLOAD(25,4), ELOAD(25,4),
.           MATNO(25), STRES(25,2), PLAST(25), XDISP(52),
.           TDISP(26,2), TREAC(26,2), ASTIF(52,52), ASLOD(52),
.           REACT(52), FRESV(1352), PEFIX(52), ESTIF(4,4)
KRESL=2
IF(NALGO.EQ.1)KRESL=1
IF(NALGO.EQ.2)KRESL=1
IF(NALGO.EQ.3.AND.IINCS.EQ.1.AND.IITER.EQ.1)KRESL=1
IF(NALGO.EQ.4.AND.IITER.EQ.1)KRESL=1
IF(NALGO.EQ.5.AND.IINCS.EQ.1.AND.IITER.EQ.1)KRESL=1
IF(NALGO.EQ.5.AND.IITER.EQ.2)KRESL=1
IF(IITER.EQ.1.OR.NALGO.EQ.1) GOTO 20
DO 10 ISVAB=1,NSVAB
10   FIXED(ISVAB)=0.0
      RETURN
20   DO 30 ISVAB=1,NSVAB
30   FIXED(ISVAB)=PEFIX(ISVAB)*FACTO
      RETURN
      END
```

NONAL alt programının temel görevi çözüm yöntemi parametresinin(NALGO) değerine göre çözüm yöntemini kontrol etmektir. KRESL göstergesinin NALGO'ya,

iterasyon numarası IITER'e ve artım numarası IINCS'e bağlı olarak değerini (1 ya da 2) ayarlamaktır. Doğrudan İterasyon ve Newton-Raphson yöntemlerinin her aşaması için KRESL=1 iken, Başlangıç Rijitliği yönteminde yük artımının ilk iterasyonu için KRESL=1'dir ve bundan sonra 2 olarak alınır. Başlangıç Rijitliği ve Teğetsel Rijitlik yöntemlerinin birleşiminde de aynı şekilde ilk iterasyon için 1 ve diğer aşamalar için 2 alınır.

NONAL yardımcı programının diğer rolü de bilinmeyenlerin önceden tahmin edilmiş değerlerini gerçek değerleriyle değiştirmektir.

#### 4.1.5 Subroutine STIFFB

```
C*****
C
C          CALCULATES ELEMENT STIFFNESS MATRICES
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
.           KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
.           NITER,NOUTP,FACTO,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
.           FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
.           MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
.           TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
.           REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
REWIND 1
DO 20 IELEM=1,NELEM
LPROP=MATNO(IELEM)
EIVAL=PROPS(LPROP,1)
SVALU=PROPS(LPROP,2)
HARDS=PROPS(LPROP,4)
NODE1=LNODS(IELEM,1)
NODE2=LNODS(IELEM,2)
ELENG=ABS(COORD(NODE2)-COORD(NODE1))
IF(PLAST(IELEM).NE.0.0) EIVAL=EIVAL*(1.0-EIVAL/(EIVAL+HARDS))
beta=12.*EIVAL/SVALU/ELENG**2
VALU1=12.*EIVAL/ELENG**3/(1.+BETA)
VALU2=6.*EIVAL/ELENG**2/(1.+BETA)
VALU3=4.*EIVAL*(1.+0.25*BETA)/ELENG/(1.+BETA)
VALU4=2.*EIVAL*(1.-0.5*BETA)/ELENG/(1.+BETA)
ESTIF(1,1)=VALU1+(13./35.)*ezk*eleng
ESTIF(1,2)=VALU2+(11./210.)*ezk*eleng**2
ESTIF(1,3)=-VALU1+(9./70.)*ezk*eleng
ESTIF(1,4)=VALU2-(13./420.)*ezk*eleng**2
ESTIF(2,2)=VALU3+(1./105.)*ezk*eleng**3
ESTIF(2,3)=-ESTIF(1,4)
ESTIF(2,4)= VALU4-(1./140.)*ezk*eleng**3
ESTIF(3,3)=ESTIF(1,1)
ESTIF(3,4)=-ESTIF(1,2)
ESTIF(4,4)=ESTIF(2,2)
DO 10 ISTIF=1,4
DO 10 JSTIF=ISTIF,4
10    ESTIF(JSTIF,ISTIF)=ESTIF(ISTIF,JSTIF)
```

```

20    WRITE(1) ESTIF
      CONTINUE
      RETURN
      END

```

Bu yardımcı programın temel amacı eleman rijitlik matrislerinin elde edilmesi ve denklem çözüm rutinlerinde kullanılmak üzere kaydedilmesidir.

Bu yardımcı programın orijinal hali aşağıdaki gibidir (Owen-Hinton).

### SUBROUTINE STIFFB

```

C*****CALCULATES ELEMENT STIFFNESS MATRICES*****
C
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
       .           KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
       .           NITER,NOUTP,FACTO
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
       .           FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
       .           MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
       .           TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
       .           REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
REWIND 1
DO 20 IELEM=1,NELEM
LPROP=MATNO(IELEM)
EIVAL=PROPS(LPROP,1)
SVALU=PROPS(LPROP,2)
HARDS=PROPS(LPROP,4)
NODE1=LNODS(IELEM,1)
NODE2=LNODS(IELEM,2)
ELENG=ABS(COORD(NODE2)-COORD(NODE1))
IF(PLAST(IELEM).NE.0.0) EIVAL=EIVAL*(1.0-EIVAL/(EIVAL+HARDS))
VALU1=0.5*SVALU
VALU2=SVALU/ELENG
VALU3=EIVAL/ELENG
VALU4=0.25*SVALU*ELENG
ESTIF(1,1)=VALU2
ESTIF(1,2)=VALU1
ESTIF(1,3)=-VALU2
ESTIF(1,4)=VALU1
ESTIF(2,2)=VALU3+VALU4
ESTIF(2,3)=-VALU1
ESTIF(2,4)=-VALU3+VALU4
ESTIF(3,3)=VALU2
ESTIF(3,4)=-VALU1
ESTIF(4,4)=VALU3+VALU4
DO 10 ISTIF=1,4
DO 10 JSTIF=ISTIF,4
10  ESTIF(JSTIF,ISTIF)=ESTIF(ISTIF,JSTIF)
      WRITE(1) ESTIF
20    CONTINUE
      RETURN
      END

```

#### 4.1.6 Subroutine ASSEMB

```

C*****
C
C          ELEMENT ASSEMBLY ROUTINE
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
.           KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
.           NITER,NOUTP,FACTO,PVALU,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
.           FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
.           MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
.           TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
.           REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
C
C          ELEMENT ASSEMBLY ROUTINE
C
REWIND 1
DO 10 ISVAB=1,NSVAB
10  ASLOD(ISVAB)=0.0
    IF(KRESL.EQ.2) GOTO 30
    DO 20 ISVAB=1,NSVAB
    DO 20 JSVAB=1,NSVAB
20  ASTIF(ISVAB,JSVAB)=0.0
30  CONTINUE

C
C          ASSEMBLE THE ELEMENT LOADS
C
DO 50 IELEM=1,NELEM
C      read(1,'(4f15.6')' ((ESTIF(i,j),j=1,4),i=1,4)
C      READ(1,'(4E15.7')' ((ESTIF(i,j),j=1,4),i=1,4)
      DO 40 INODE=1,NNODE
      NODEI=LNODS(IELEM,INODE)
      DO 40 IDOFN=1,NDOFN
      NROWS=(NODEI-1)*NDOFN+IDOFN
      NROWE=(INODE-1)*NDOFN+IDOFN
      ASLOD(NROWS)=ASLOD(NROWS)+ELOAD(IELEM,NROWE)

C
C          ASSEMBLE THE ELEMENT STIFFNESS MATRICES
C
      IF(KRESL.EQ.2)GOTO 40
      DO 40 JNODE=1,NNODE
      NODEJ=LNODS(IELEM,JNODE)
      DO 40 JDOFN=1,NDOFN
      NCOLS=(NODEJ-1)*NDOFN+JDOFN
      NCOLE=(JNODE-1)*NDOFN+JDOFN
      ASTIF(NROWS,NCOLS)=ASTIF(NROWS,NCOLS)+ESTIF(NROWE,NCOLE)
40  CONTINUE
50  CONTINUE
      RETURN
      END

```

Bu alt programın görevi eleman düğüm noktasını yüklerini toplayarak global yük vektörünü oluşturmaktır. Ayrıca her elemanın katkısını global rijitlik matrisinde bir araya getirir.

Bu alt programa özgü komutlar;

**ASLOD(MSVAB):** Birleşmiş yük vektörü.

**ASTIF(MSVAB, MSVAB):** Birleşmiş global rijitlik matrisi.

**RLOAD(MEVAB):** Eleman yük vektörü.

**ESTIF(MEVAB, MEVAB):** Eleman rijitlik matrisi.

**IELEM, NELEM, MELEM:** Sırasıyla bir elemana ait içerik, numara, maksimum değer.

**IFILE:** Dosya girişi.

**IDOFN, JDOFN:** Her bir düğüm noktası için serbestlik derecesi değeri.

**NDOFN:** Her bir düğüm noktası için serbestlik derecesi numarası.

**INODE, JNODE:** Her bir eleman için düğüm noktası içeriği.

**NNODE:** Her eleman için düğüm noktası numarası.

**MNODE:** Her eleman düğüm noktası için maksimum değer.

**ISVAB, JSVAB:** Global yapısal değişken endeksi.

**MSVAB:** Maksimum global yapısal değişken değeri.

**NSVAB:** Global yapısal değişken numarası.

**JFILE:** Dosya çıktısı.

**KRESL:** Denklem ayırma parametresi.

**LNODS(MELEM, MNODE):** Her eleman için listelenmiş düğüm noktası numarası.

**NODE I:** Düğüm noktası I

**NODE J:** Düğüm noktası J

**NCOLS:** Yapısal global rijitlik matrisindeki sütun sayısı.

**NROWS:** Yapısal global rijitlik matrisindeki ve yük vektöründeki satır sayısı.

**NCOLE:** Eleman rijitlik matrisindeki kolon sayısı.

**NROWE:** Eleman rijitlik matrisindeki ve yük vektöründeki satır sayısı.

**MEVAB:** Eleman değişkenlerinin maksimum değeri.

Bu programın ASSEMBLE THE ELEMENT LOADS kısmının orijinal hali (Owen-Hinton):

```
C
C          ASSEMBLE THE ELEMENT LOADS
C
DO 50 IELEM=1,NELEM
READ(1) ESTIF
DO 40 INODE=1,NNODE
NODEI=LNODS(IELEM,INODE)
DO 40 IDOFN=1,NDOFN
NROWS=(NODEI-1)*NDOFN+IDOFN
NROWE=(INODE-1)*NDOFN+IDOFN
ASLOD(NROWS)=ASLOD(NROWS)+ELOAD(IELEM,NROWE)
```

#### 4.1.7 Subroutine GREDUC

```
C*****
C
C          GAUSSIAN REDUCTION ROUTINE
C
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
NITER,NOUTP,FACTO,PVALU,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)

C
C          GAUSSIAN REDUCTION ROUTINE
C

KOUNT=0
NEQNS=NSVAB
DO 70 IEQNS=1,NEQNS
IF(IFPRE(IEQNS).EQ.1) GOTO 40

C
C          REDUCE EQUATIONS
C

PIVOT=ASTIF(IEQNS,IEQNS)
IF(ABS(PIVOT).LT.1.0E-10) GOTO 60
IF(IEQNS.EQ.NEQNS) GOTO 70
IEQN1=IEQNS+1
DO 30 IROWS=IEQN1,NEQNS
KOUNT=KOUNT+1
FACTR=ASTIF(IROWS,IEQNS)/PIVOT
FRESV(KOUNT)=FACTR
IF(FACTR.EQ.0.0) GOTO 30
DO 10 ICOLS=IEQNS,NEQNS
ASTIF(IROWS,ICOLS)=ASTIF(IROWS,ICOLS)-FACTR*ASTIF(IEQNS,ICOLS)
10    CONTINUE
```

```

ASLOD(IROWS)=ASLOD(IROWS)-FACTR*ASLOD(IEQNS)
30  CONTINUE
    GOTO 70
C
C          ADJUST RHS(LOADS) FOR PRESCRIBED DISPLACEMENTS
C
40  DO 50 IROWS=IEQNS,NEQNS
    ASLOD(IROWS)=ASLOD(IROWS)-ASTIF(IROWS,IEQNS)*FIXED(IEQNS)
50  CONTINUE
    GOTO 70
60  WRITE(6,900)
900 FORMAT(5X,15HINCORRECT PIVOT)
    STOP
70  CONTINUE
    RETURN
    END

```

Bu program Gaussian indirgeme yöntemiyle çözülen denklemlerde denklem giderme işlemini yapan alt programdır. Farklı değişkenlerin isimleri ve görevleri;

**ASLOD(MEQNS):** Birleşmiş yük vektörü.

**ASTIF(MEQNS, MEQNS):** Birleşmiş global rijitlik matrisi.

**IEQNS, NEQNS, MEQNS:** Sırasıyla denklemlerin içeriği, numarası ve maksimum değeri.

**IFPRE(MEQNS):** Bir düğüm noktasının bağıllık(mesnetlenme biçimini) durumunu tanımlayan vektör.

0-Serbest

1-Bağılı

**FIXED(MEQNS):** Öngörülmüş yer değiştirmelerin vektörü ( eğer önceden bir değer Verilmemişse 0 alınır.)

**ICOLS:** Yapısal rijitlik matrisindeki kolonların içeriği.

**IROWS:** Yapısal rijitlik matrisindeki satırların içeriği.

**FACTR:** Gaussian indirgeme faktörü.

**FRESV( ):** Kaydedilmiş Gaussian indirgeme faktörleri.

**PIVOT:** Silinmiş değişkenin köşegen terimi.

#### 4.1.8 Subroutine RESOLV

```
C*****
C
C          RESOLVING GAUSSIANREDUCTION ROUTINE
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINC$S,IITER,
.           KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
.           NITER,NOUTP,FACTO,PVALU,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
.           FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
.           MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
.           TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
.           REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
KOUNT=0
NEQNS=NSVAB
DO 40 IEQNS=1,NEQNS
IF(IFPRE(IEQNS).EQ.1) GOTO 20

C
C          REDUCE  RHS
C

IF(IEQNS.EQ.NEQNS) GOTO 40
IEQN1=IEQNS+1
DO 10 IROWS=IEQN1,NEQNS
KOUNT=KOUNT+1
FACTR=FRESV(KOUNT)
IF(FACTR.EQ.0)GOTO 10
ASLOD(IROWS)=ASLOD(IROWS)-FACTR*ASLOD(IEQNS)
10  CONTINUE
GOTO 40

C
C          ADJUST RHS TO PRESCRIBED DISPLACEMENTS
C

20  DO 30 IROWS=IEQNS,NEQNS
     ASLOD(IROWS)=ASLOD(IROWS)-ASTIF(IROWS,IEQNS)*FIXED(IEQNS)
30  CONTINUE
40  CONTINUE
RETURN
END
```

RESOLV alt programı standart Gaussian yok etme yöntemini kullanarak yük terimlerini azaltır. Gaussian çarpanlara ayırma terimleri subroutine GREduc alt programından elde edilir, kaydedilir ve RESOLV programında bu verilerden yararlanılır.

#### 4.1.9 Subroutine BAKSUB

```

C*****
C
C          BACK-SUBSTITUTION ROUTINE
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
.           KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
.           NITER,NOUTP,FACTO,PVALU,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
.           FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
.           MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
.           TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
.           REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)

C
C          BACK-SUBSTITUTION ROUTINE
C

      NEQNS=NSVAB
      DO 10 IEQNS=1,NEQNS
      REACT(IEQNS)=0.0
10    CONTINUE
      NEQN1=NEQNS+1
      DO 40 IEQNS=1,NEQNS
      NBACK=NEQN1-IEQNS
      PIVOT=ASTIF(NBACK,NBACK)
      RESID=ASLOD(NBACK)
      IF(NBACK.EQ.NEQNS) GOTO 30
      NBAC1=NBACK+1
      DO 20 ICOLS=NBAC1,NEQNS
      RESID=RESID-ASTIF(NBACK,ICOLS)*XDISP(ICOLS)
20    CONTINUE
30    IF(IFPRE(NBACK).EQ.0) XDISP(NBACK)=RESID/PIVOT
      IF(IFPRE(NBACK).EQ.1) XDISP(NBACK)=FIXED(NBACK)
      IF(IFPRE(NBACK).EQ.1) REACT(NBACK)=-RESID
40    CONTINUE
      GO TO (100,110,110,110,110),NALGO
100   KOUNT=0
      DO 50 IPOIN=1,NPOIN
      DO 50 IDOFN=1,NDOFN
      KOUNT=KOUNT+1
      TDISP(IPOIN,IDOFN)=XDISP(KOUNT)
50    TREAC(IPOIN,IDOFN)=REACT(KOUNT)
      GO TO 120
110   KOUNT=0
      DO 51 IPOIN=1,NPOIN
      DO 51 IDOFN=1,NDOFN
      KOUNT=KOUNT+1
      TDISP(IPOIN,IDOFN)=TDISP(IPOIN,IDOFN)+XDISP(KOUNT)
51    TREAC(IPOIN,IDOFN)=TREAC(IPOIN,IDOFN)+REACT(KOUNT)
      DO 90 IPOIN=1,NPOIN
      DO 60 IELEM=1,NELEM
      DO 60 INODE=1,NNODE
      NLOCA=LNODS(IELEM,INODE)
60    IF(IPOIN.EQ.NLOCA) GOTO 70
70    DO 80 IDOFN=1,NDOFN
      NPOSN=(IPOIN-1)*NDOFN+IDOFN

```

```

80   IEVAB=(INODE-1)*NDOFN+IDOFN
90   TLOAD(IELEM,IEVAB) = TLOAD(IELEM,IEVAB)+REACT(NPOSN)
90   CONTINUE
120  CONTINUE
     RETURN
     END

```

Bu alt programa özgü değişken parametreler;

**ASLOD(MEQNS):** İndirgenmiş yük vektörü.

**ASTIF(MEQNS, MEQNS):** İndirgenmiş global rijitlik matrisi.

**IEQNS, NEQNS, MEQNS:** Sırasıyla denklemlerin içeriği, numarası ve maksimum  
değeri.

**IFPRE(MEQNS):** Düğüm noktasının bağlanma durumunu tanımlayan  
parametrelerin vektörü.

**FIXED(MEQNS):** Öngörülmüş yer değiştirme vektörü. (Önceden bir değer  
atanmamışsa 0 alınır. )

**PIVOT:** Yok edilen değişkenin köşegen terimi.

**REACT(MEQNS):** Öngörülmüş yer değiştirmeli düğüm noktalarındaki tepkiler.

**XDISP(MEQNS):** Düğüm noktalarındaki yer değiştirmeler.

Bu programın yardımcı programın orjinal hali (Owen-Hinton):

## SUBROUTINE BAKSUB

```

C*****
C          BACK-SUBSTITUTION ROUTINE
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
      KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
      NITER,NOUTP,FACTO,PVALU
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
      .           FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
      .           MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
      .           TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
      .           REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
C
C          BACK-SUBSTITUTION ROUTINE
C
      NEQNS=NSVAB
      DO 10 IEQNS=1,NEQNS
      REACT(IEQNS)=0.0
10    CONTINUE
      NEQN1=NEQNS+1
      DO 40 IEQNS=1,NEQNS
      NBACK=NEQN1-IEQNS

```

```

PIVOT=ASTIF(NBACK,NBACK)
RESID=ASLOD(NBACK)
IF(NBACK.EQ.NEQNS) GOTO 30
NBAC1=NBACK+1
DO 20 ICOLS=NBAC1,NEQNS
RESID=RESID-ASTIF(NBACK,ICOLS)*XDISP(ICOLS)
20 CONTINUE
30 IF(IFPRE(NBACK).EQ.0) XDISP(NBACK)=RESID/PIVOT
IF(IFPRE(NBACK).EQ.1) XDISP(NBACK)=FIXED(NBACK)
IF(IFPRE(NBACK).EQ.1) REACT(NBACK)=-RESID
40 CONTINUE
KOUNT=0
DO 50 IPOIN=1,NPOIN
DO 50 IDOFTN=1,NDOFTN
KOUNT=KOUNT+1
TDISP(IPOIN,IDOFTN)=XDISP(KOUNT)
50 TREAC(IPOIN,IDOFTN)=REACT(KOUNT)
RETURN
END

```

#### 4.1.10 Subroutine REFORB

```

C*****
C
C      CALCULATES INTERNAL EQUIVALENT NODAL FORCES
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
.           KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
.           NITER,NOUTP,FACTO,PVALU,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
.           FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
.           MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
.           TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
.           REACT(52),FRESV(1352),PEFIF(52),ESTIF(4,4)
DO 10 IELEM=1,NELEM
DO 10 IEVAB=1,NEVAB
10 ELOAD(IELEM,IEVAB)=0.0
DO 70 IELEM=1,NELEM
LPROP=MATNO(IELEM)
EIVAL=PROPS(LPROP,1)
SVALU=PROPS(LPROP,2)
YIELD=PROPS(LPROP,3)
HARDS=PROPS(LPROP,4)
NODE1=LNODS(IELEM,1)
NODE2=LNODS(IELEM,2)
ELENG=ABS(COORD(NODE2)-COORD(NODE1))
beta=12.*EIVAL/SVALU/ELENG**2
ELAML=(EZK/4./EIVAL)**0.25*ELENG
C
VALU1=12.*EIVAL/ELENG**3/(1.+BETA)
VALU2=6.*EIVAL/ELENG**2/(1.+BETA)
VALU3=4.*EIVAL*(1.+0.25*BETA)/ELENG/(1.+BETA)
VALU4=2.*EIVAL*(1.-0.5*BETA)/ELENG/(1.+BETA)
EK(1,1)=VALU1+(13./35.)*ezk*eleng
EK(1,2)=VALU2+(11./210.)*ezk*eleng**2
EK(1,3)=-VALU1+(9./70.)*ezk*eleng
EK(1,4)=VALU2-(13./420.)*ezk*eleng**2

```

```

EK(2,2)=VALU3+(1./105.)*ezk*eleng**3
EK(2,3)=-ESTIF(1,4)
EK(2,4)=VALU4-(1./140.)*ezk*eleng**3
EK(3,3)=EK(1,1)
EK(3,4)=-EK(1,2)
EK(4,4)= EK(2,2)
DO 11 ISTIF=1,4
DO 11 JSTIF=ISTIF,4
11 EK(JSTIF,ISTIF)=EK(ISTIF,JSTIF)

C
WNOD1=XDISP(NODE1*NDOFN-1)
WNOD2=XDISP(NODE2*NDOFN-1)
THTA1=XDISP(NODE1*NDOFN)
THTA2=XDISP(NODE2*NDOFN)

C
P1=EK(1,1)*WNOD1+EK(1,2)*THTA1+EK(1,3)*WNOD2+EK(1,4)*THTA2
P2=EK(2,1)*WNOD1+EK(2,2)*THTA1+EK(2,3)*WNOD2+EK(2,4)*THTA2
P3=EK(3,1)*WNOD1+EK(3,2)*THTA1+EK(3,3)*WNOD2+EK(3,4)*THTA2
P4=EK(4,1)*WNOD1+EK(4,2)*THTA1+EK(4,3)*WNOD2+EK(4,4)*THTA2
EMORT=0.5*(1.-ELAML**4/96.)*(P2-P4)-0.125*(1.-13./1440.*ELAML**4)*(P1+P3)

C
STRAN=(THTA1-THTA2)/ELENG
STLIN=EMORT
STCUR=STRES(IELEM,1)+STLIN
PREYS=YIELD+HARDS*ABS(PLAST(IELEM))
IF(ABS(STRES(IELEM,1)).GE.PREYS) GOTO 20
ESCUR=ABS(STCUR)-PREYS
IF(ESCUR.LE.0.0) GOTO 40
RFACT=ESCUR/ABS(STLIN)
GOTO 30
20 IF(STRES(IELEM,1).GT.0.0.AND.STLIN.LE.0.0) GOTO 40
IF(STRES(IELEM,1).LT.0.0.AND.STLIN.GE.0.0) GOTO 40
RFACT=1.0
30 REDUC=1.0-RFACT
STRES(IELEM,1)=STRES(IELEM,1)+REDUC*STLIN+
RFACT*EIVAL*(1.0-EIVAL/(EIVAL+HARDS))*STRAN
PLAST(IELEM)=PLAST(IELEM)+RFACT*STRAN*EIVAL/(EIVAL+HARDS)
GOTO 50
40 STRES(IELEM,1)=STRES(IELEM,1)+STLIN
C 50 STRES(IELEM,2)=STRES(IELEM,2)+(SVALU/ELENG)*(WNOD2-WNOD1)
C . -0.5*SVALU*(THTA1+THTA2)
50 STRES(IELEM,2)=STRES(IELEM,2)+0.5*(P3-P1)
ELOAD(IELEM,1)=ELOAD(IELEM,1)-STRES(IELEM,2)
ELOAD(IELEM,2)=ELOAD(IELEM,2)+STRES(IELEM,1)
. -0.5*ELENG*STRES(IELEM,2)
ELOAD(IELEM,3)=ELOAD(IELEM,3)+STRES(IELEM,2)
ELOAD(IELEM,4)=ELOAD(IELEM,4)-STRES(IELEM,1)
. -0.5*ELENG*STRES(IELEM,2)
70 CONTINUE
RETURN
END

```

Yararlanılan kaynaktaki özgün hali aşağıdaki gibidir. (Owen-Hinton)

## SUBROUTINE REFORB

```
C*****CALCULATES INTERNAL EQUIVALENT NODAL FORCES*****
C
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
        .          KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
        .          NITER,NOUTP,FACTO
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
        .          FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
        .          MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
        .          TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
        .          REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
DO 10 IELEM=1,NELEM
DO 10 IEVAB=1,NEVAB
10 ELOAD(IELEM,IEVAB)=0.0
DO 70 IELEM=1,NELEM
LPROP=MATNO(IELEM)
EIVAL=PROPS(LPROP,1)
SVALU=PROPS(LPROP,2)
YIELD=PROPS(LPROP,3)
HARDS=PROPS(LPROP,4)
NODE1=LNODS(IELEM,1)
NODE2=LNODS(IELEM,2)
ELENG=ABS(COORD(NODE2)-COORD(NODE1))
WNOD1=XDISP(NODE1*NDOFN-1)
WNOD2=XDISP(NODE2*NDOFN-1)
THTA1=XDISP(NODE1*NDOFN)
THTA2=XDISP(NODE2*NDOFN)
STRAN=(THTA1-THTA2)/ELENG
STLIN=STRAN*EIVAL
STCUR=STRES(IELEM,1)+STLIN
PREYS=YIELD+HARDS*ABS(PLAST(IELEM))
IF(ABS(STRES(IELEM,1)).GE.PREYS) GOTO 20
ESCUR=ABS(STCUR)-PREYS
IF(ESCUR.LE.0.0) GOTO 40
RFACT=ESCUR/ABS(STLIN)
GOTO 30
20 IF(STRES(IELEM,1).GT.0.0.AND.STLIN.LE.0.0) GOTO 40
IF(STRES(IELEM,1).LT.0.0.AND.STLIN.GE.0.0) GOTO 40
RFACT=1.0
30 REDUC=1.0-RFACT
STRES(IELEM,1)=STRES(IELEM,1)+REDUC*STLIN+
        .          RFACT*EIVAL*(1.0-EIVAL/(EIVAL+HARDS))*STRAN
PLAST(IELEM)=PLAST(IELEM)+RFACT*STRAN*EIVAL/(EIVAL+HARDS)
GOTO 50
40 STRES(IELEM,1)=STRES(IELEM,1)+STLIN
50 STRES(IELEM,2)=STRES(IELEM,2)+(SVALU/ELENG)*(WNOD2-WNOD1)
        .          -0.5*SVALU*(THTA1+THTA2)
ELOAD(IELEM,1)=ELOAD(IELEM,1)-STRES(IELEM,2)
ELOAD(IELEM,2)=ELOAD(IELEM,2)+STRES(IELEM,1)
        .          -0.5*ELENG*STRES(IELEM,2)
ELOAD(IELEM,3)=ELOAD(IELEM,3)+STRES(IELEM,2)
ELOAD(IELEM,4)=ELOAD(IELEM,4)-STRES(IELEM,1)
        .          -0.5*ELENG*STRES(IELEM,2)
70 CONTINUE
RETURN
END
```

#### 4.1.11 Subroutine CONUND

```

C*****
C
C          CHECKS FOR SOLUTION CONVERGENCE
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
      KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
      NITER,NOUTP,FACTO,PVALU,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
      FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
      MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
      TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
      REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
DIMENSION STFOR(52),TOFOR(52)
NCHEK=0
RESID=0.0
RETOT=0.0
DO 10 ISVAB=1,NSVAB
  STFOR (ISVAB)=0.0
10   TOFOR (ISVAB)=0.0
    DO 20 IELEM=1,NELEM
      IEVAB=0
      DO 20 INODE=1,NNODE
        NODNO=LNODS(IELEM, INODE)
        DO 20 IDOFN=1,NDOFN
          IEVAB=IEVAB+1
          NPOSN=(NODNO -1)*NDOFN+IDOFN
          STFOR(NPOSN)=STFOR(NPOSN)+ELOAD(IELEM, IEVAB)
20    TOFOR(NPOSN)=TOFOR(NPOSN)+TLOAD(IELEM, IEVAB)
      DO 30 ISVAB=1,NSVAB
        REFOR=TOFOR(ISVAB)-STFOR(ISVAB)
        RESID=RESID+REFOR*REFOR
30    RETOT=RETOT+TOFOR(ISVAB)*TOFOR(ISVAB)
      DO 40 IELEM=1,NELEM
        DO 40 IEVAB=1,NEVAB
40    ELOAD(IELEM, IEVAB)=TLOAD(IELEM, IEVAB)-ELOAD(IELEM, IEVAB)
      RATIO=100.0*SQRT(RESID/RETOT)
      IF(RATIO.GT.TOLER) NCHEK=1
      IF(IITER.EQ.1) GOTO 50
      IF(RATIO.GT.PVALU) NCHEK=999
50    PVALU=RATIO
      WRITE(6,900) IITER,NCHEK,RATIO
900  FORMAT(1H0,5X,"ITERATION NUMBER=",I5/
            1H0,5X,"CONVERGENCE CODE=",I4,3X,
            "NORM OF RESIDUAL SUM RATIO=",E14.6)
      RETURN
      END

```

CONUND yardımcı programı yakınsamanın artık kuvvet değerlerine bağlı hesaplandığı alt programdır.

Yakınsama kriteri;

$$\frac{\sqrt{\left[ \sum_{i=1}^N (\psi_i^r)^2 \right]}}{\sqrt{\left[ \sum_{i=1}^N (f_i)^2 \right]}} \times 100 \leq TOLER \quad (4.1)$$

Burada N;toplam düğüm noktası sayısı ve r; iterasyon sayısıdır. Yakınsamanın olup olmadığını gösteren parametre ise **NCHEK**'dir.

#### 4.1.12 Subroutine RESULT

```
C*****
C
C          OUTPUTS DISPLACEMENT,REACTIONS AND STRESSES
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLOAD,NPROP,NNODE,IINCS,IITER,
.           KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
.           NITER,NOUTP,FACTO,PVALU,EZK
COMMON/UNIM2/PROPS(5,4),COORD(26),LNODS(25,2),IFPRE(52),
.           FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
.           MATNO(25),STRES(25,2),PLAST(25),XDISP(52),
.           TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
.           REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4)
IF(NDOFN.EQ.1) WRITE(6,900)
900  FORMAT(1H0,5X,"NODE",4X,"DISPL.",12X,"REACTIONS")
IF(NDOFN.EQ.2) WRITE(6,910)
910  FORMAT(1H0,5X,"NODE",4X,"DISPL.",12X,"REACTION",
.           7X,"DISPL.",12X,"REACTION")
DO 10 IPOIN=1,NPOIN
10   WRITE(6,920) IPOIN,(TDISP(IPOIN,IDOFN),TREAC(IPOIN,IDOFN),
.           IDOFN=1,NDOFN)
920  FORMAT(1I0,2(E14.6,5X,E14.6))
IF(NDOFN.EQ.2) WRITE(6,930)
930  FORMAT(1H0,2X,"ELEMENT",12X,"STRESSES",12X,"PL STRAIN")
IF(NDOFN.EQ.1) WRITE(6,940)
940  FORMAT(1H0,2X,"ELEMENT",5X,"STRESSES",5X,"PL STRAIN")
DO 20 IELEM=1,NELEM
20   WRITE(6,950) IELEM,(STRES(IELEM,IDOFN),IDOFN=1,NDOFN),
.           PLAST(IELEM)
950  FORMAT(1I0,3E14.6)
RETURN
END
```

Çıktı sıklığı INCLOD alt programı ile ayarlanan ana programın sonuçlarını ve çıktılarını almayı sağlayan programdır.

## 4.2 Tabakalı Kiriş Programı (TIMLAY)

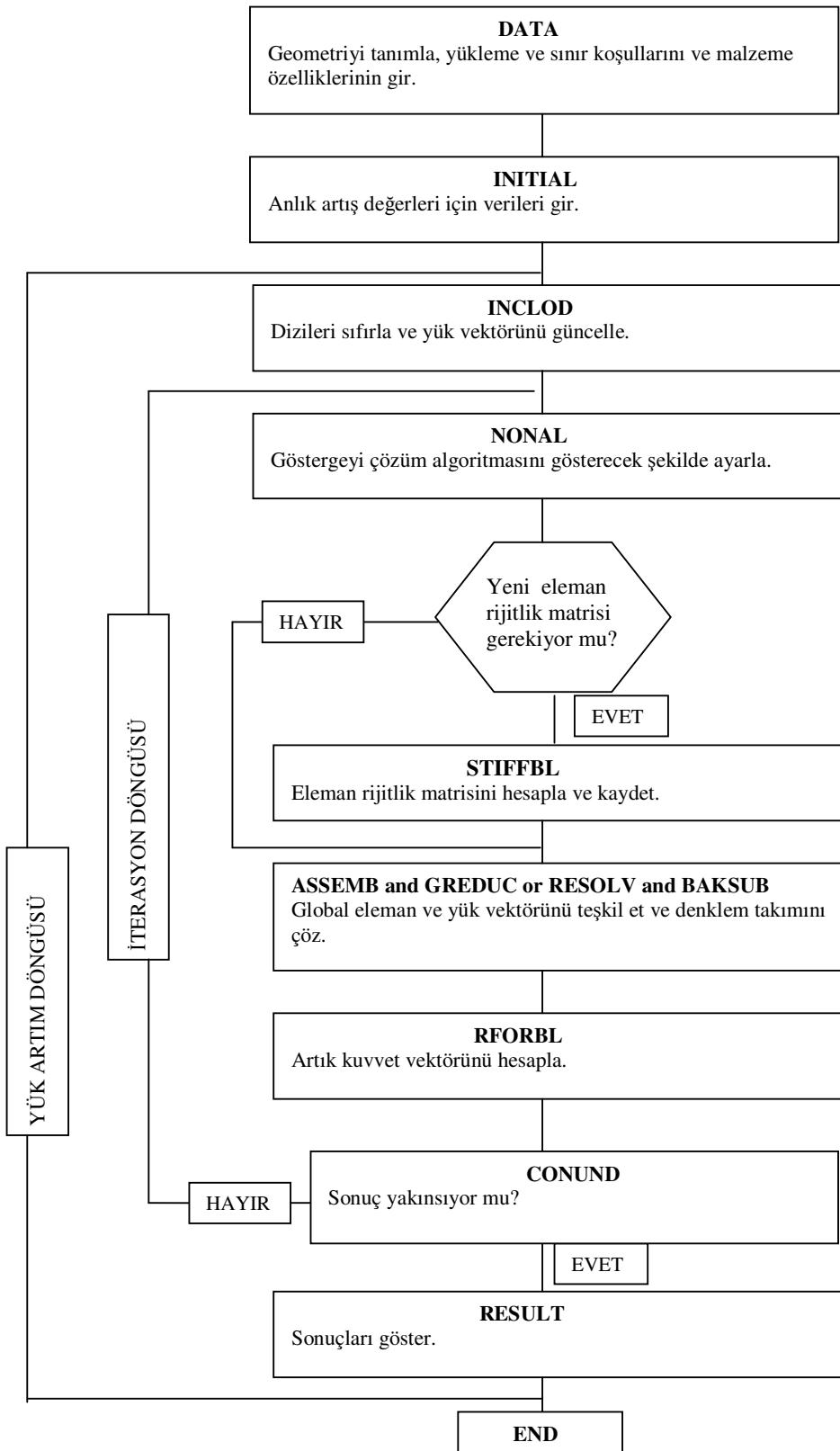
Tabakalı kiriş programının yapısı Şekil (4.1)'de gösterile akış diyagramıyla aynıdır.

Burada sadece STIFFB alt programının yerine STIFBL ve REFORB alt programı yerine de RFORBL gelir. STIFBL alt programı da ilave bir LAYER alt programını çağırır. Tabakalı kiriş ana programı MASTER BEML aşağıdaki gibidir.

### PROGRAM MASTER BEML

```
C*****
C
C      ELASTOPLASTIC LAYERED TIMOSHENKO BEAM PROGRAM
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLAYR,NPROP,NNODE,IINCS,IITER,
.
KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
.
NITER,NOUTP,FACTO
COMMON/UNIM2/PROPS(5,25),COORD(26),LNODS(25,2),IFPRE(52),
.
FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
.
MATNO(25),STRES(25,2),PLAST(250),XDISP(52),
.
TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
.
REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4),
.
STRSL(250,2)
CALL DATA
CALL INITIAL
DO 30 IINCS=1,NINCS
CALL INCLOD
DO 10 IIITER=1,NITER
CALL NONAL
IF(KRESL.EQ.1) CALL STIFBL
CALL ASSEMB
IF(KRESL.EQ.1) CALL GREDUC
IF(KRESL.EQ.2) CALL RESOLV
CALL BAKSUB
CALL RFORBL
CALL CONUND
IF(NCHEK.EQ.0) GOTO 20
IF(IIITER.EQ.1.AND.NOUTP.EQ.1) CALL RESULT
IF(NOUTP.EQ.2) CALL RESULT
10  CONTINUE
WRITE(6,900)
900  FORMAT(1H0,5X,"SOLUTION NOT CONVERGED")
STOP
20  CALL RESULT
30  CONTINUE
STOP
END
```

Program bir akış diyagramı ile gösterilecek olursa;



**Şekil 4.2:** TIMLAY programı akış diyagramı.

TIMOSH programından farklı olan alt programların içerikleri ve görevleri aşağıdaki gibidir.

#### 4.2.1 Subroutine STIFBL

```
C*****  
C  
C          CALCULATES ELEMENT STIFFNESS MATRICES  
C  
C*****  
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLAYR,NPROP,NNODE,IINCS,IITER,  
.      KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,  
.      NITER,NOUTP,FACTO  
COMMON/UNIM2/PROPS(5,25),COORD(26),LNODS(25,2),IFPRE(52),  
.      FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),  
.      MATNO(25),STRES(25,2),PLAST(250),XDISP(52),  
.      TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),  
.      REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4),  
.      STRSL(250,2)  
REWIND 1  
DO 20 IELEM=1,NELEM  
LPROP=MATNO(IELEM)  
CALL LAYER(IELEM,EIVAL,SVALU)  
HARDS=PROPS(LPROP,4)  
NODE1=LNODS(IELEM,1)  
NODE2=LNODS(IELEM,2)  
ELENG=ABS(COORD(NODE2)-COORD(NODE1))  
VALU1=0.5*SVALU  
VALU2=SVALU/ELENG  
VALU3=EIVAL/ELENG  
VALU4=0.25*SVALU*ELENG  
ESTIF(1,1)=VALU2  
ESTIF(1,2)=VALU1  
ESTIF(1,3)=-VALU2  
ESTIF(1,4)=VALU1  
ESTIF(2,2)=VALU3+VALU4  
ESTIF(2,3)=-VALU1  
ESTIF(2,4)=-VALU3+VALU4  
ESTIF(3,3)=VALU2  
ESTIF(3,4)=-VALU1  
ESTIF(4,4)=VALU3+VALU4  
DO 10 ISTIF=1,4  
DO 10 JSTIF=ISTIF,4  
10    ESTIF(JSTIF,ISTIF)=ESTIF(ISTIF,JSTIF)  
        WRITE(1) ESTIF  
20    CONTINUE  
        RETURN  
        END
```

STIFBL elastoplastik-tabakalı Timoshenko kırışı için eleman rijitlik matrislerini hesaplayan alt programdır.

#### 4.2.2 Subroutine RFORBL

```

C*****CALCULATES INTERNAL EQUIVALENT NODAL FORCES*****
C
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLAYR,NPROP,NNODE,IINCS,IITER,
      KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
      NITER,NOUTP,FACTO
COMMON/UNIM2/PROPS(5,25),COORD(26),LNODS(25,2),IFPRE(52),
      FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
      MATNO(25),STRES(25,2),PLAST(250),XDISP(52),
      TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
      REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4),
      STRSL(250,2)
DIMENSION STRAN(2)
DO 15 IELEM=1,NELEM
DO 10 IEVAB=1,NEVAB
  10ELOAD(IELEM,IEVAB)=0.0
    DO 15 IDOFN=1,NDOFN
      15STRES(IELEM,IDOFN)=0.0
        KLAYR=0
DO 70 IELEM=1,NELEM
  LPROP=MATNO(IELEM)
  YOUNG=PROPS(LPROP,1)
  SHEAR=PROPS(LPROP,2)
  YIELD=PROPS(LPROP,3)
  HARD=PROPS(LPROP,4)
  THKTO=PROPS(LPROP,5)
  NODE1=LNODS(IELEM,1)
  NODE2=LNODS(IELEM,2)
  ELENG=ABS(COORD(NODE2)-COORD(NODE1))
  WNOD1=XDISP(NODE1*NDOFN-1)
  WNOD2=XDISP(NODE2*NDOFN-1)
  THTA1=XDISP(NODE1*NDOFN)
  THTA2=XDISP(NODE2*NDOFN)
  STRAN(1)=(THTA1-THTA2)/ELENG
  STRAN(2)=(WNOD2-WNOD1)/ELENG
    -0.5*(THTA1+THTA2)
  ZMIDL=-THKTO/2.0
  KOUNT=5
DO 50 ILAYR=1,NLAYR
  KLAYR=KLAYR+1
  KOUNT=KOUNT+1
  BRDTH=PROPS(LPROP,KOUNT)
  KOUNT=KOUNT+1
  THICK=PROPS(LPROP,KOUNT)
  ZMIDL=ZMIDL+THICK/2.0
  STLIN=YOUNG*STRAN(1)*ZMIDL
  STCUR=STRSL(KLAYR,1)+STLIN
  PREYS=YIELD+HARD*ABS(PLAST(KLAYR))
  IF(ABS(STCUR(KLAYR,1)).GE.PREYS) GOTO 20
  ESCUR=ABS(STCUR)-PREYS
  IF(ESCUR.LE.0.0) GOTO 40
  RFACT=ESCUR/ABS(STLIN)
  GOTO 30
20    IF(STRSL(KLAYR,1).GT.0.0.AND.STLIN.LE.0.0) GOTO 40
      IF(STRSL(KLAYR,1).LT.0.0.AND.STLIN.GE.0.0) GOTO 40

```

```

RFACT=1.0
30    REDUC=1.0-RFACT
        STRSL(KLAYR,1)=STRSL(KLAYR,1)+REDUC*STLIN+ RFACT*YOUNG
                    *(1.0- YOUNG/(YOUNG+HARDS))*STRAN(1)*ZMIDL
        PLAST(KLAYR)=PLAST(KLAYR)+RFACT*STRAN(1)*YOUNG/(YOUNG+HARDS)
                    *ZMIDL
        GOTO 45
40    STRSL(KLAYR,1)=STRSL(KLAYR,1)+STLIN
45    STRSL(KLAYR,2)=STRSL(KLAYR,2)+STRAN(2)*SHEAR
        STRES(IELEM,1)=STRES(IELEM,1)+STRSL(KLAYR,1)*
                    BRDTH*THICK*ZMIDL
        STRES(IELEM,2)=STRES(IELEM,2)+STRSL(KLAYR,2)*
                    BRDTH*THICK
        ZMIDL=ZMIDL+THICK/2.0
50    CONTINUE
        ELOAD(IELEM,1)=ELOAD(IELEM,1)-STRES(IELEM,2)
        ELOAD(IELEM,2)=ELOAD(IELEM,2)+STRES(IELEM,1)
                    -0.5*ELENG*STRES(IELEM,2)
        ELOAD(IELEM,3)=ELOAD(IELEM,3)+STRES(IELEM,2)
        ELOAD(IELEM,4)=ELOAD(IELEM,4)-STRES(IELEM,1)
                    -0.5*ELENG*STRES(IELEM,2)
70    CONTINUE
    RETURN
    END

```

RFORBL orta nokta kuralını kullanarak tabakalı kiriş için  $\mathbf{p}$  değerini elde eder.

#### 4.2.3 Subroutine LAYER (IELEM, EIVAL, SVALU)

```

C*****
C
C      CALCULATES INTEGRATED VALUES FOR EI AND GA THROUGH DEPTH
C
C*****
COMMON/UNIM1/NPOIN,NELEM,NBOUN,NLAYR,NPROP,NNODE,JINCS,IITER,
        .          KRESL,NCHEK,TOLER,NALGO,NSVAB,NDOFN,NINCS,NEVAB,
        .          NITER,NOUTP,FACTO
COMMON/UNIM2/PROPS(5,25),COORD(26),LNODS(25,2),IFPRE(52),
        .          FIXED(52),TLOAD(25,4),RLOAD(25,4),ELOAD(25,4),
        .          MATNO(25),STRES(25,2),PLAST(250),XDISP(52),
        .          TDISP(26,2),TREAC(26,2),ASTIF(52,52),ASLOD(52),
        .          REACT(52),FRESV(1352),PEFIX(52),ESTIF(4,4),
        .          STRSL(250,2)
EIVAL=0.0
SVALU=0.0
LPROP=MATNO(IELEM)
KLAYR=(IELEM-1)*NLAYR
SHEAR=PROPS(LPROP,2)
HARDS=PROPS(LPROP,4)
THKTO=PROPS(LPROP,5)
ZMIDL=-THKTO/2.0
KOUNT=5
DO 10 ILAYR=1,NLAYR
KLAYR=KLAYR+1
YOUNG=PROPS(LPROP,1)
IF(PLAST(KLAYR).NE.0.0) YOUNG=YOUNG*(1.0-YOUNG/(YOUNG+HARDS))

```

```
KOUNT=KOUNT+1
BRDTH=PROPS(LPROP, KOUNT)
KOUNT=KOUNT+1
THICK=PROPS(LPROP,KOUNT)
ZMIDL=ZMIDL+THICK/2.0
EIVAL=EIVAL+YOUNG*BRDTH*THICK*ZMIDL*ZMIDL
SVALU=SVALU+SHEAR*BRDTH*THICK
ZMIDL=ZMIDL+THICK/2.0
10      CONTINUE
        RETURN
        END
```

LAYER eğilme rüjütlüğü EI'nın yaklaşık değerini ve GA'nın gerçek değerini orta nokta kuralı ile bulan alt programdır.



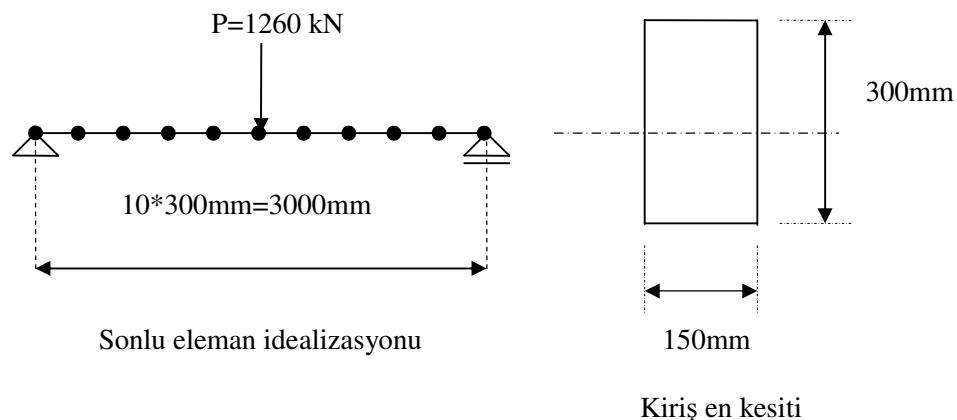
## 5. UYGULAMALAR

Önceki bölümlerde açıklanan tabakalı ve tabakasız Timoshenko kırışı elastoplastik çözümleri ile ilgili olarak 2 farklı yükleme (tekil ve yayılı yükleme) için çözüm yapılacaktır. Ayrıca tabakasız yaklaşımında kırışın elastik zemine oturması durumu için de uygulamalar yapılacaktır.

### 5.1 Tabakasız Elastoplastik Timoshenko Kırış Örnekleri

#### 5.1.1 Tekil yüklü tabakasız Timoshenko kırış örneği

Aşağıda geometrisi ve yükleme şekli verilen basit kırışe ait elastoplastik çözüm aranmaktadır.



**Şekil 5.1:** Tekil yük etkisi altındaki kırış

Problemin girişi ile ilgili parametreler aşağıda verilmiştir:

**11(NPOIN) 10(NELEM) 2(NBOUN) 1(NMATS) 4(NPROP) 2(NNODE)14(NINCS)  
2(NALGO) 2(NDOFN)**

**1**(1nolu malzeme) **7.0875e10**(EI) **2423070.**(GA/1.5) **843750.**(M<sub>0</sub>) **0.**(H<sup>I</sup>)

Elemanlara ait giriş bilgileri aşağıda tablo halinde özetlenmiştir:

**Çizelge 5.1:** Eleman idealleştirilmesi ile ilgili giriş bilgileri.

Eleman No	i	j	x <sub>i</sub>	x <sub>j</sub>	Malzeme No
1	1	2	0	300	1
2	2	3	300	600	1
3	3	4	600	900	1
4	4	5	900	1200	1
5	5	6	1200	1500	1
6	6	7	1500	1800	1
7	7	8	1800	2100	1
8	8	9	2100	2400	1
9	9	10	2400	2700	1
10	10	11	2700	3000	1

Düğüm nokta <u>numarası</u>	Mesnetlenme <u>durumu</u>	Moment çökme <u>değeri</u>	Dönme <u>değeri</u>	Dışarıdan <u>verilmiş dönme</u>
1(ilk)	1(tutulu)	0.	0.	0.
11(son)	1(tutulu)	0.	0.	0.

Eleman <u>numarası</u>	İlk D.N.'daki <u>yük</u>	İlk D.N.'daki <u>moment</u>	Son D.N.'daki <u>yük</u>	Son D.N.'daki <u>moment</u>
6	1260.	0.	0.	0.
10	0.	0.	0.	0.

**0.0E-3** (elastik zemin değeri=0)

<b>100</b> (iterasyon sayısı yük için kN)	<b>2</b> (NOUTP her yük artımı ve iterasyonda sonuçları basar.)	<b>0.30</b> (yükün %30'u ile hesaba başlanır ve her sefer için bu sütundaki oran kadar arttırılarak bir önceki değere eklenir. İlk değeri <b>378kN</b> )	<b>0.5</b> (tolerans değeri)
100	2	0.20 ( <b>630kN</b> )	0.5
100	2	0.10 ( <b>756kN</b> )	0.5
100	2	0.10 ( <b>882kN</b> )	0.5
100	2	0.05 ( <b>945kN</b> )	0.5
100	2	0.05 ( <b>1008kN</b> )	0.5
100	2	0.05 ( <b>1071kN</b> )	0.5
100	2	0.05 ( <b>1134kN</b> )	0.5
100	2	0.02 ( <b>1159kN</b> )	0.5
100	2	0.02 ( <b>1184kN</b> )	0.5
100	2	0.02 ( <b>1209kN</b> )	0.5
100	2	0.02 ( <b>1234kN</b> )	0.5
100	2	0.01 ( <b>1247kN</b> )	0.5
100	2	0.01 ( <b>1260kN</b> )	0.5

**Formatlı veri girişi:**

```

11 10 2 1 4 2 14 2 2
    1 7.0875e10    2423070.    843750.    0.
1 1 2 1
2 2 3 1
3 3 4 1
4 4 5 1
5 5 6 1
6 6 7 1
7 7 8 1
8 8 9 1
9 9 10 1
10 10 11 1
    1      0.
    2      300.
    3      600.

```

4	900.			
5	1200.			
6	1500.			
7	1800.			
8	2100.			
9	2400.			
10	2700.			
11	3000.			
1	1	0.	0	0.
11	1	0.	0	0.
6	1260.	0.	0.	0.
10	0.	0.	0.	0.

### 0.0E-3

100	2	0.30	0.5
100	2	0.20	0.5
100	2	0.10	0.5
100	2	0.10	0.5
100	2	0.05	0.5
100	2	0.05	0.5
100	2	0.05	0.5
100	2	0.05	0.5
100	2	0.02	0.5
100	2	0.02	0.5
100	2	0.02	0.5
100	2	0.02	0.5
100	2	0.01	0.5
100	2	0.01	0.5

### Veri girişi sonrası alınan sonuçlar:

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NPOIN= 11 NELEM= 10 NBOUN= 2 NMATS= 1
NPROP= 4 NNODE= 2 NINCS= 14 NALGO= 2
NDOFN= 2
0 MATERIAL PROPERTIES
 1 .7087500E+11 .2423070E+07 .8437500E+06 .0000000E+00
0 EL NODES MAT.
 1 1 2 1
 2 2 3 1
 3 3 4 1
 4 4 5 1
 5 5 6 1
 6 6 7 1
 7 7 8 1
 8 8 9 1
 9 9 10 1
10 10 11 1
0 NODE COORD.
 1 .00000
 2 300.00000
 3 600.00000
 4 900.00000

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      5 1200.00000
      6 1500.00000
      7 1800.00000
      8 2100.00000
      9 2400.00000
     10 2700.00000
     11 3000.00000
0 RES.NODE CODE PRES.VALUES CODE PRES.VALUES
    1 1   .00000  0   .00000
    11 1   .00000  0   .00000
0 ELEMENT NODAL LOADS
    1   .00000   .00000   .00000   .00000
    2   .00000   .00000   .00000   .00000
    3   .00000   .00000   .00000   .00000
    4   .00000   .00000   .00000   .00000
    5   .00000   .00000   .00000   .00000
    6 1260.00000   .00000   .00000   .00000
    7   .00000   .00000   .00000   .00000
    8   .00000   .00000   .00000   .00000
    9   .00000   .00000   .00000   .00000
   10   .00000   .00000   .00000   .00000
ELASTIC SOIL COEFFICIENT= .000000E+00
0 IINCS= 1 NITER= 100 NOUTP= 2 FACTO= .300000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .892957E-01
0 NODE DISPL. REACTION DISPL. REACTION
    1 .000000E+00 -.189001E+03 .300001E-02 .000000E+00
    2 .911402E+00 .000000E+00 .288001E-02 .000000E+00
    3 .175080E+01 .000000E+00 .252001E-02 .000000E+00
    4 .244621E+01 .000000E+00 .192000E-02 .000000E+00
    5 .292561E+01 .000000E+00 .108000E-02 .000000E+00
    6 .311701E+01 .000000E+00 -.424235E-09 .000000E+00
    7 .292561E+01 .000000E+00 -.108000E-02 .000000E+00
    8 .244620E+01 .000000E+00 -.192000E-02 .000000E+00
    9 .175080E+01 .000000E+00 -.252000E-02 .000000E+00
   10 .911402E+00 .000000E+00 -.288001E-02 .000000E+00
   11 .000000E+00 -.189001E+03 -.300001E-02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
    1 .283500E+05 .189001E+03 .000000E+00
    2 .850501E+05 .189001E+03 .000000E+00
    3 .141750E+06 .189001E+03 .000000E+00
    4 .198451E+06 .189000E+03 .000000E+00
    5 .255150E+06 .188999E+03 .000000E+00
    6 .255150E+06 -.188999E+03 .000000E+00
    7 .198450E+06 -.189000E+03 .000000E+00
    8 .141750E+06 -.189001E+03 .000000E+00
    9 .850502E+05 -.189000E+03 .000000E+00
   10 .283500E+05 -.189000E+03 .000000E+00
0 IINCS= 2 NITER= 100 NOUTP= 2 FACTO= .200000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .382387E-01
0 NODE DISPL. REACTION DISPL. REACTION
    1 .000000E+00 -.315001E+03 .500000E-02 .000000E+00
    2 .151900E+01 .000000E+00 .480000E-02 .000000E+00
    3 .291800E+01 .000000E+00 .420000E-02 .000000E+00
    4 .407700E+01 .000000E+00 .320000E-02 .000000E+00
    5 .487600E+01 .000000E+00 .180000E-02 .000000E+00
    6 .519500E+01 .000000E+00 -.268042E-09 .000000E+00
    7 .487600E+01 .000000E+00 -.180000E-02 .000000E+00
    8 .407700E+01 .000000E+00 -.320000E-02 .000000E+00

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9 .291800E+01 .000000E+00 -.420000E-02 .000000E+00
10 .151900E+01 .000000E+00 -.480000E-02 .000000E+00
11 .000000E+00 -.315001E+03 -.500000E-02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .472501E+05 .315000E+03 .000000E+00
2 .141750E+06 .315000E+03 .000000E+00
3 .236250E+06 .315001E+03 .000000E+00
4 .330750E+06 .315000E+03 .000000E+00
5 .425250E+06 .315000E+03 .000000E+00
6 .425250E+06 -.315000E+03 .000000E+00
7 .330750E+06 -.315001E+03 .000000E+00
8 .236250E+06 -.315000E+03 .000000E+00
9 .141750E+06 -.315000E+03 .000000E+00
10 .472500E+05 -.315000E+03 .000000E+00
0 IINCS= 3 NITER= 100 NOUTP= 2 FACTO= .100000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .189532E-01
0 NODE DISPL. REACTION DISPL. REACTION
1 .000000E+00 -.378000E+03 .600000E-02 .000000E+00
2 .182280E+01 .000000E+00 .576000E-02 .000000E+00
3 .350160E+01 .000000E+00 .504000E-02 .000000E+00
4 .489240E+01 .000000E+00 .384000E-02 .000000E+00
5 .585120E+01 .000000E+00 .216000E-02 .000000E+00
6 .623400E+01 .000000E+00 -.104533E-09 .000000E+00
7 .585120E+01 .000000E+00 -.216000E-02 .000000E+00
8 .489240E+01 .000000E+00 -.384000E-02 .000000E+00
9 .350160E+01 .000000E+00 -.504000E-02 .000000E+00
10 .182280E+01 .000000E+00 -.576000E-02 .000000E+00
11 .000000E+00 -.378000E+03 -.600000E-02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .567001E+05 .378000E+03 .000000E+00
2 .170100E+06 .378000E+03 .000000E+00
3 .283500E+06 .378000E+03 .000000E+00
4 .396900E+06 .378000E+03 .000000E+00
5 .510300E+06 .377999E+03 .000000E+00
6 .510300E+06 -.378000E+03 .000000E+00
7 .396900E+06 -.378000E+03 .000000E+00
8 .283500E+06 -.378000E+03 .000000E+00
9 .170100E+06 -.378000E+03 .000000E+00
10 .567000E+05 -.378000E+03 .000000E+00
0 IINCS= 4 NITER= 100 NOUTP= 2 FACTO= .100000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .221761E-01
0 NODE DISPL. REACTION DISPL. REACTION
1 .000000E+00 -.441001E+03 .700000E-02 .000000E+00
2 .212660E+01 .000000E+00 .672000E-02 .000000E+00
3 .408520E+01 .000000E+00 .588000E-02 .000000E+00
4 .570780E+01 .000000E+00 .448000E-02 .000000E+00
5 .682640E+01 .000000E+00 .252000E-02 .000000E+00
6 .727300E+01 .000000E+00 .101090E-09 .000000E+00
7 .682640E+01 .000000E+00 -.252000E-02 .000000E+00
8 .570780E+01 .000000E+00 -.448000E-02 .000000E+00
9 .408520E+01 .000000E+00 -.588000E-02 .000000E+00
10 .212660E+01 .000000E+00 -.672000E-02 .000000E+00
11 .000000E+00 -.441000E+03 -.700000E-02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .661500E+05 .441000E+03 .000000E+00
2 .198450E+06 .441000E+03 .000000E+00
3 .330750E+06 .441000E+03 .000000E+00
4 .463050E+06 .441000E+03 .000000E+00

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      5 .595350E+06 .441000E+03 .000000E+00
      6 .595350E+06 -.441001E+03 .000000E+00
      7 .463050E+06 -.441001E+03 .000000E+00
      8 .330750E+06 -.441000E+03 .000000E+00
      9 .198450E+06 -.441000E+03 .000000E+00
     10 .661500E+05 -.441000E+03 .000000E+00
0 IINCS= 5 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .146137E-01
0 NODE DISPL. REACTION DISPL. REACTION
    1 .000000E+00 -.472500E+03 .750000E-02 .000000E+00
    2 .227850E+01 .000000E+00 .720000E-02 .000000E+00
    3 .437700E+01 .000000E+00 .630000E-02 .000000E+00
    4 .611550E+01 .000000E+00 .480000E-02 .000000E+00
    5 .731400E+01 .000000E+00 .270000E-02 .000000E+00
    6 .779250E+01 .000000E+00 .233608E-09 .000000E+00
    7 .731400E+01 .000000E+00 -.270000E-02 .000000E+00
    8 .611550E+01 .000000E+00 -.480000E-02 .000000E+00
    9 .437700E+01 .000000E+00 -.630000E-02 .000000E+00
   10 .227850E+01 .000000E+00 -.720000E-02 .000000E+00
   11 .000000E+00 -.472500E+03 -.750000E-02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
    1 .708750E+05 .472500E+03 .000000E+00
    2 .212625E+06 .472500E+03 .000000E+00
    3 .354375E+06 .472500E+03 .000000E+00
    4 .496125E+06 .472500E+03 .000000E+00
    5 .637875E+06 .472500E+03 .000000E+00
    6 .637875E+06 -.472500E+03 .000000E+00
    7 .496125E+06 -.472500E+03 .000000E+00
    8 .354375E+06 -.472500E+03 .000000E+00
    9 .212625E+06 -.472500E+03 .000000E+00
   10 .708750E+05 -.472500E+03 .000000E+00
0 IINCS= 6 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .891275E-02
0 NODE DISPL. REACTION DISPL. REACTION
    1 .000000E+00 -.504000E+03 .800000E-02 .000000E+00
    2 .243040E+01 .000000E+00 .768000E-02 .000000E+00
    3 .466880E+01 .000000E+00 .672000E-02 .000000E+00
    4 .652320E+01 .000000E+00 .512000E-02 .000000E+00
    5 .780160E+01 .000000E+00 .288000E-02 .000000E+00
    6 .831200E+01 .000000E+00 -.220702E-10 .000000E+00
    7 .780160E+01 .000000E+00 -.288000E-02 .000000E+00
    8 .652320E+01 .000000E+00 -.512000E-02 .000000E+00
    9 .466880E+01 .000000E+00 -.672000E-02 .000000E+00
   10 .243040E+01 .000000E+00 -.768000E-02 .000000E+00
   11 .000000E+00 -.504000E+03 -.800000E-02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
    1 .756000E+05 .504000E+03 .000000E+00
    2 .226800E+06 .504000E+03 .000000E+00
    3 .378000E+06 .504000E+03 .000000E+00
    4 .529200E+06 .504000E+03 .000000E+00
    5 .680400E+06 .504000E+03 .000000E+00
    6 .680400E+06 -.504000E+03 .000000E+00
    7 .529200E+06 -.504000E+03 .000000E+00
    8 .378000E+06 -.504000E+03 .000000E+00
    9 .226800E+06 -.504000E+03 .000000E+00
   10 .756000E+05 -.504000E+03 .000000E+00
0 IINCS= 7 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00
0 ITERATION NUMBER= 1

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0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .963762E-02  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .000000E+00 -.535500E+03 .850000E-02 .000000E+00  
   2 .258230E+01 .000000E+00 .816000E-02 .000000E+00  
   3 .496060E+01 .000000E+00 .714000E-02 .000000E+00  
   4 .693090E+01 .000000E+00 .544000E-02 .000000E+00  
   5 .828920E+01 .000000E+00 .306000E-02 .000000E+00  
   6 .883150E+01 .000000E+00 .128388E-09 .000000E+00  
   7 .828920E+01 .000000E+00 -.306000E-02 .000000E+00  
   8 .693090E+01 .000000E+00 -.544000E-02 .000000E+00  
   9 .496060E+01 .000000E+00 -.714000E-02 .000000E+00  
 10 .258230E+01 .000000E+00 -.816000E-02 .000000E+00  
 11 .000000E+00 -.535500E+03 -.850000E-02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
   1 .803250E+05 .535500E+03 .000000E+00  
   2 .240975E+06 .535500E+03 .000000E+00  
   3 .401625E+06 .535500E+03 .000000E+00  
   4 .562275E+06 .535500E+03 .000000E+00  
   5 .722925E+06 .535500E+03 .000000E+00  
   6 .722925E+06 -.535500E+03 .000000E+00  
   7 .562275E+06 -.535500E+03 .000000E+00  
   8 .401625E+06 -.535500E+03 .000000E+00  
   9 .240975E+06 -.535500E+03 .000000E+00  
 10 .803250E+05 -.535500E+03 .000000E+00  
 0 IINCS= 8 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .884383E-02  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .000000E+00 -.567000E+03 .900000E-02 .000000E+00  
   2 .273420E+01 .000000E+00 .864000E-02 .000000E+00  
   3 .525240E+01 .000000E+00 .756000E-02 .000000E+00  
   4 .733860E+01 .000000E+00 .576000E-02 .000000E+00  
   5 .877680E+01 .000000E+00 .324000E-02 .000000E+00  
   6 .935100E+01 .000000E+00 -.716963E-10 .000000E+00  
   7 .877680E+01 .000000E+00 -.324000E-02 .000000E+00  
   8 .733860E+01 .000000E+00 -.576000E-02 .000000E+00  
   9 .525240E+01 .000000E+00 -.756000E-02 .000000E+00  
 10 .273420E+01 .000000E+00 -.864000E-02 .000000E+00  
 11 .000000E+00 -.567000E+03 -.900000E-02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
   1 .850500E+05 .567000E+03 .000000E+00  
   2 .255150E+06 .567000E+03 .000000E+00  
   3 .425250E+06 .567000E+03 .000000E+00  
   4 .595350E+06 .567000E+03 .000000E+00  
   5 .765450E+06 .567000E+03 .000000E+00  
   6 .765450E+06 -.567000E+03 .000000E+00  
   7 .595350E+06 -.567000E+03 .000000E+00  
   8 .425250E+06 -.567000E+03 .000000E+00  
   9 .255150E+06 -.567000E+03 .000000E+00  
 10 .850500E+05 -.567000E+03 .000000E+00  
 0 IINCS= 9 NITER= 100 NOUTP= 2 FACTO= .200000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .470999E-02  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .000000E+00 -.579600E+03 .920000E-02 .000000E+00  
   2 .279496E+01 .000000E+00 .883200E-02 .000000E+00  
   3 .536912E+01 .000000E+00 .772800E-02 .000000E+00  
   4 .750168E+01 .000000E+00 .588800E-02 .000000E+00  
   5 .897184E+01 .000000E+00 .331200E-02 .000000E+00  
 6 .955880E+01 .000000E+00 .581999E-10 .000000E+00

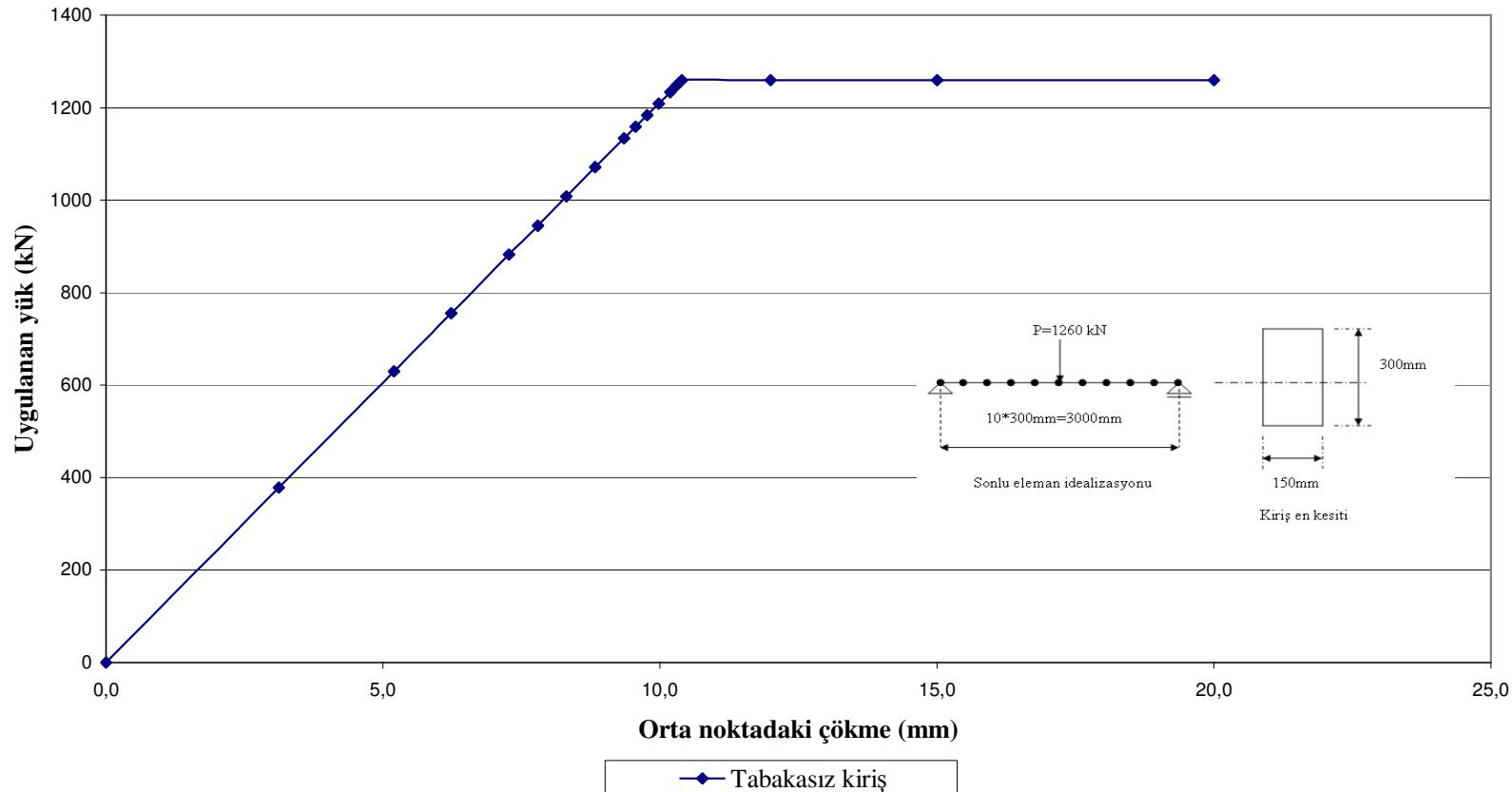
	7	.897184E+01	.000000E+00	-.331200E-02	.000000E+00
	8	.750168E+01	.000000E+00	-.588800E-02	.000000E+00
	9	.536912E+01	.000000E+00	-.772800E-02	.000000E+00
	10	.279496E+01	.000000E+00	-.883200E-02	.000000E+00
	11	.000000E+00	-.579600E+03	-.920000E-02	.000000E+00
0	ELEMENT	STRESSES	PL STRAIN		
1	.869400E+05	.579600E+03	.000000E+00		
2	.260820E+06	.579600E+03	.000000E+00		
3	.434700E+06	.579600E+03	.000000E+00		
4	.608580E+06	.579600E+03	.000000E+00		
5	.782460E+06	.579600E+03	.000000E+00		
6	.782460E+06	-.579600E+03	.000000E+00		
7	.608580E+06	-.579600E+03	.000000E+00		
8	.434700E+06	-.579600E+03	.000000E+00		
9	.260820E+06	-.579600E+03	.000000E+00		
10	.869400E+05	-.579600E+03	.000000E+00		
0	IINCS= 10	NITER= 100	NOUTP= 2	FACTO= .200000E-01	TOLER= .500000E+00
0	ITERATION NUMBER= 1				
0	CONVERGENCE CODE= 0	NORM OF RESIDUAL SUM RATIO= .219712E-02			
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.000000E+00	-.592200E+03	.940000E-02	.000000E+00	
2	.285572E+01	.000000E+00	.902400E-02	.000000E+00	
3	.548584E+01	.000000E+00	.789600E-02	.000000E+00	
4	.766476E+01	.000000E+00	.601600E-02	.000000E+00	
5	.916688E+01	.000000E+00	.338400E-02	.000000E+00	
6	.976660E+01	.000000E+00	.484551E-10	.000000E+00	
7	.916688E+01	.000000E+00	-.338400E-02	.000000E+00	
8	.766476E+01	.000000E+00	-.601600E-02	.000000E+00	
9	.548584E+01	.000000E+00	-.789600E-02	.000000E+00	
10	.285572E+01	.000000E+00	-.902400E-02	.000000E+00	
11	.000000E+00	-.592200E+03	-.940000E-02	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.888300E+05	.592200E+03	.000000E+00		
2	.266490E+06	.592200E+03	.000000E+00		
3	.444150E+06	.592200E+03	.000000E+00		
4	.621810E+06	.592200E+03	.000000E+00		
5	.799470E+06	.592200E+03	.000000E+00		
6	.799470E+06	-.592200E+03	.000000E+00		
7	.621810E+06	-.592200E+03	.000000E+00		
8	.444150E+06	-.592200E+03	.000000E+00		
9	.266490E+06	-.592200E+03	.000000E+00		
10	.888300E+05	-.592200E+03	.000000E+00		
0	IINCS= 11	NITER= 100	NOUTP= 2	FACTO= .200000E-01	TOLER= .500000E+00
0	ITERATION NUMBER= 1				
0	CONVERGENCE CODE= 0	NORM OF RESIDUAL SUM RATIO= .474426E-02			
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.000000E+00	-.604800E+03	.960000E-02	.000000E+00	
2	.291648E+01	.000000E+00	.921600E-02	.000000E+00	
3	.560256E+01	.000000E+00	.806400E-02	.000000E+00	
4	.782784E+01	.000000E+00	.614400E-02	.000000E+00	
5	.936192E+01	.000000E+00	.345600E-02	.000000E+00	
6	.997440E+01	.000000E+00	.410544E-10	.000000E+00	
7	.936192E+01	.000000E+00	-.345600E-02	.000000E+00	
8	.782784E+01	.000000E+00	-.614400E-02	.000000E+00	
9	.560256E+01	.000000E+00	-.806400E-02	.000000E+00	
10	.291648E+01	.000000E+00	-.921600E-02	.000000E+00	
11	.000000E+00	-.604800E+03	-.960000E-02	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.907200E+05	.604800E+03	.000000E+00		
2	.272160E+06	.604800E+03	.000000E+00		

3 .453600E+06 .604800E+03 .000000E+00  
 4 .635040E+06 .604800E+03 .000000E+00  
 5 .816480E+06 .604800E+03 .000000E+00  
 6 .816480E+06 -.604800E+03 .000000E+00  
 7 .635040E+06 -.604800E+03 .000000E+00  
 8 .453600E+06 -.604800E+03 .000000E+00  
 9 .272160E+06 -.604800E+03 .000000E+00  
 10 .907200E+05 -.604800E+03 .000000E+00  
 0 IINCS= 12 NITER= 100 NOUTP= 2 FACTO= .200000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .232051E-02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.617400E+03 .980000E-02 .000000E+00  
 2 .297724E+01 .000000E+00 .940800E-02 .000000E+00  
 3 .571928E+01 .000000E+00 .823200E-02 .000000E+00  
 4 .799092E+01 .000000E+00 .627200E-02 .000000E+00  
 5 .955696E+01 .000000E+00 .352800E-02 .000000E+00  
 6 .101822E+02 .000000E+00 .250100E-09 .000000E+00  
 7 .955696E+01 .000000E+00 -.352800E-02 .000000E+00  
 8 .799092E+01 .000000E+00 -.627200E-02 .000000E+00  
 9 .571928E+01 .000000E+00 -.823200E-02 .000000E+00  
 10 .297724E+01 .000000E+00 -.940800E-02 .000000E+00  
 11 .000000E+00 -.617400E+03 -.980000E-02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .926100E+05 .617400E+03 .000000E+00  
 2 .277830E+06 .617400E+03 .000000E+00  
 3 .463050E+06 .617400E+03 .000000E+00  
 4 .648270E+06 .617400E+03 .000000E+00  
 5 .833490E+06 .617400E+03 .000000E+00  
 6 .833490E+06 -.617400E+03 .000000E+00  
 7 .648270E+06 -.617400E+03 .000000E+00  
 8 .463050E+06 -.617400E+03 .000000E+00  
 9 .277830E+06 -.617400E+03 .000000E+00  
 10 .926100E+05 -.617400E+03 .000000E+00  
 0 IINCS= 13 NITER= 100 NOUTP= 2 FACTO= .100000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .751606E-02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.623700E+03 .990000E-02 .000000E+00  
 2 .300762E+01 .000000E+00 .950400E-02 .000000E+00  
 3 .577764E+01 .000000E+00 .831600E-02 .000000E+00  
 4 .807246E+01 .000000E+00 .633600E-02 .000000E+00  
 5 .965448E+01 .000000E+00 .356400E-02 .000000E+00  
 6 .102861E+02 .000000E+00 .296988E-09 .000000E+00  
 7 .965448E+01 .000000E+00 -.356400E-02 .000000E+00  
 8 .807246E+01 .000000E+00 -.633600E-02 .000000E+00  
 9 .577764E+01 .000000E+00 -.831600E-02 .000000E+00  
 10 .300762E+01 .000000E+00 -.950400E-02 .000000E+00  
 11 .000000E+00 -.623700E+03 -.990000E-02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .935550E+05 .623700E+03 .000000E+00  
 2 .280665E+06 .623700E+03 .000000E+00  
 3 .467775E+06 .623700E+03 .000000E+00  
 4 .654885E+06 .623700E+03 .000000E+00  
 5 .841995E+06 .623700E+03 .000000E+00  
 6 .841995E+06 -.623700E+03 .000000E+00  
 7 .654885E+06 -.623700E+03 .000000E+00  
 8 .467775E+06 -.623700E+03 .000000E+00  
 9 .280665E+06 -.623700E+03 .000000E+00  
 10 .935550E+05 -.623700E+03 .000000E+00

```

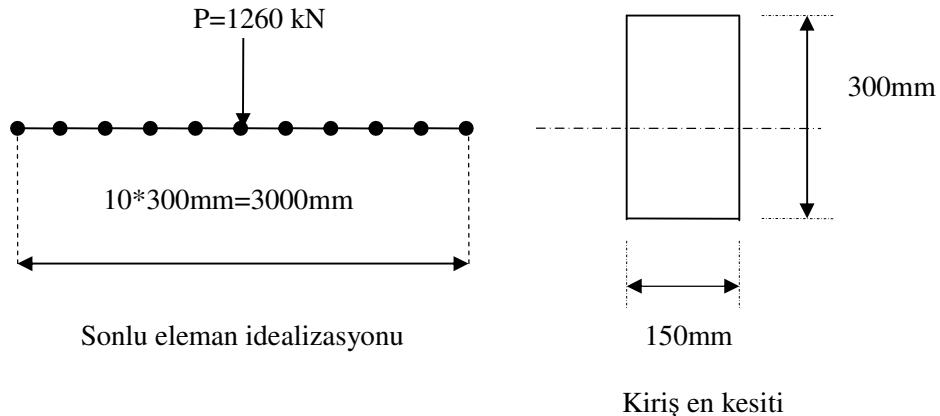
0 IINCS= 14 NITER= 100 NOUTP= 2 FACTO= .100000E-01 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .618578E+03
0 NODE   DISPL.      REACTION    DISPL.      REACTION
  1 .000000E+00   -.630000E+03  .100000E-01   .000000E+00
  2 .303800E+01   .000000E+00  .960000E-02   .000000E+00
  3 .583600E+01   .000000E+00  .840000E-02   .000000E+00
  4 .815400E+01   .000000E+00  .640000E-02   .000000E+00
  5 .975200E+01   .000000E+00  .360000E-02   .000000E+00
  6 .103900E+02   .000000E+00  .245570E-09   .000000E+00
  7 .975200E+01   .000000E+00  -.360000E-02   .000000E+00
  8 .815400E+01   .000000E+00  -.640000E-02   .000000E+00
  9 .583600E+01   .000000E+00  -.840000E-02   .000000E+00
 10 .303800E+01   .000000E+00  -.960000E-02   .000000E+00
 11 .000000E+00   -.630000E+03  -.100000E-01   .000000E+00
0 ELEMENT      STRESSES      PL STRAIN
  1 .945000E+05  .630000E+03  .000000E+00
  2 .283500E+06  .630000E+03  .000000E+00
  3 .472500E+06  .630000E+03  .000000E+00
  4 .661500E+06  .630000E+03  .000000E+00
  5 .843750E+06  .630000E+03  .952363E-07
  6 .843750E+06  -.630000E+03  .952363E-07
  7 .661500E+06  -.630000E+03  .000000E+00
  8 .472500E+06  -.630000E+03  .000000E+00
  9 .283500E+06  -.630000E+03  .000000E+00
 10 .945000E+05  -.630000E+03  .000000E+00

```



Şekil 5.2: Tekil yüklü tabakasız Timoshenko kırışı örneği

### 5.1.2 Elastik zemine oturan tekil yüklü tabakasız Timoshenko kırışı örneği



**Şekil 5.3:** Tekil yük etkisi altındaki kiriş

Bu örnekte elastik zemin etkilerini daha iyi gözlemleyebilmek için mesnetler kaldırılarak çözüm yapılmıştır. Kayma şekil değiştirmelerini içeren sistem rijitlik matrisi ilk örnekte olduğu gibi hesaba katılmıştır.

Kiriş malzeme özellikleri ilk örnekteki gibi olup  $k_0$ (Elastik zemin katsayısı)  $6000\text{t/m}^3$  alınmıştır. Bu durumda;

$$EZK=k_0*b = 6.10^{-5}(\text{kN/mm}^3)*150(\text{mm})=9.10^{-3} \text{ kN/mm}$$

Kiriş malzeme özellikleri ilk örnekteki gibidir. Veri giriş bilgilerinde ilk örnektenden farklı olarak kiriş mesnetlenmesinden kaynaklanan farklılık aşağıda gösterilmiştir. Mesnetlenme durumu ve elastik zemin katsayısı değeri dışında veri girişi örnek 5.1 ile aynıdır.

Düğüm noktası numarası	Mesnetlenme durumu	Moment çökme değeri	Dönme değeri	Dışarıdan verilmiş dönme
1(ilk)	0 (serbest)	0.	0.	0.
11(son)	0 (serbest)	0.	0.	0.

**Veri girişi sonrası alınan sonuçlar;**

```
NPOIN= 11 NELEM= 10 NBOUN= 2 NMATS= 1
NPROP= 4 NNODE= 2 NINCS= 14 NALGO= 2
NDOFN= 2
0 MATERIAL PROPERTIES
    1 .7087500E+11 .2423070E+07 .8437500E+06 .0000000E+00
0 EL NODES MAT.
    1 1 2 1
    2 2 3 1
    3 3 4 1
    4 4 5 1
    5 5 6 1
    6 6 7 1
    7 7 8 1
    8 8 9 1
    9 9 10 1
   10 10 11 1
0 NODE COORD.
    1 .00000
    2 300.00000
    3 600.00000
    4 900.00000
    5 1200.00000
    6 1500.00000
    7 1800.00000
    8 2100.00000
    9 2400.00000
   10 2700.00000
   11 3000.00000
0 RES.NODE CODE PRES.VALUES CODE PRES.VALUES
    1 0 .00000 0 .00000
   11 0 .00000 0 .00000
0 ELEMENT NODAL LOADS
    1 .00000 .00000 .00000 .00000
    2 .00000 .00000 .00000 .00000
    3 .00000 .00000 .00000 .00000
    4 .00000 .00000 .00000 .00000
    5 .00000 .00000 .00000 .00000
    6 1260.00000 .00000 .00000 .00000
    7 .00000 .00000 .00000 .00000
    8 .00000 .00000 .00000 .00000
    9 .00000 .00000 .00000 .00000
   10 .00000 .00000 .00000 .00000
ELASTIC SOIL COEFFICIENT= .900000E-02
0 IINCS= 1 NITER= 100 NOUTP= 2 FACTO= .300000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .336351E+02
0 NODE DISPL. REACTION DISPL. REACTION
    1 .133092E+02 .000000E+00 .977460E-03 .000000E+00
    2 .136042E+02 .000000E+00 .969804E-03 .000000E+00
    3 .138955E+02 .000000E+00 .915887E-03 .000000E+00
    4 .141626E+02 .000000E+00 .768534E-03 .000000E+00
    5 .143701E+02 .000000E+00 .479602E-03 .000000E+00
```

6	.144684E+02	.000000E+00	.139451E-06	.000000E+00	
7	.143702E+02	.000000E+00	-.479327E-03	.000000E+00	
8	.141627E+02	.000000E+00	-.768266E-03	.000000E+00	
9	.138958E+02	.000000E+00	-.915625E-03	.000000E+00	
10	.136045E+02	.000000E+00	-.969544E-03	.000000E+00	
11	.133096E+02	.000000E+00	-.977204E-03	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.271286E+04	.181826E+02	.000000E+00		
2	.136619E+05	.549391E+02	.000000E+00		
3	.357551E+05	.924781E+02	.000000E+00		
4	.692193E+05	.130723E+03	.000000E+00		
5	.114243E+06	.169502E+03	.000000E+00		
6	.114243E+06	-.169509E+03	.000000E+00		
7	.692209E+05	-.130719E+03	.000000E+00		
8	.357563E+05	-.924745E+02	.000000E+00		
9	.136625E+05	-.549402E+02	.000000E+00		
10	.271384E+04	-.181772E+02	.000000E+00		
0	ITERATION NUMBER=	2			
0	CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.308732E+02	
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.272934E+02	.000000E+00	.980206E-03	.000000E+00	
2	.275897E+02	.000000E+00	.976034E-03	.000000E+00	
3	.278835E+02	.000000E+00	.923957E-03	.000000E+00	
4	.281532E+02	.000000E+00	.775983E-03	.000000E+00	
5	.283628E+02	.000000E+00	.484097E-03	.000000E+00	
6	.284619E+02	.000000E+00	.267290E-06	.000000E+00	
7	.283629E+02	.000000E+00	-.483567E-03	.000000E+00	
8	.281535E+02	.000000E+00	-.775460E-03	.000000E+00	
9	.278840E+02	.000000E+00	-.923438E-03	.000000E+00	
10	.275904E+02	.000000E+00	-.975518E-03	.000000E+00	
11	.272941E+02	.000000E+00	-.979695E-03	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.282956E+04	.188959E+02	.000000E+00		
2	.141671E+05	.566872E+02	.000000E+00		
3	.368415E+05	.944785E+02	.000000E+00		
4	.708572E+05	.132289E+03	.000000E+00		
5	.116215E+06	.170095E+03	.000000E+00		
6	.116216E+06	-.170093E+03	.000000E+00		
7	.708589E+05	-.132281E+03	.000000E+00		
8	.368428E+05	-.944778E+02	.000000E+00		
9	.141678E+05	-.566788E+02	.000000E+00		
10	.283064E+04	-.188928E+02	.000000E+00		
0	ITERATION NUMBER=	3			
0	CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.308614E+02	
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.412920E+02	.000000E+00	.960905E-03	.000000E+00	
2	.415832E+02	.000000E+00	.960703E-03	.000000E+00	
3	.418730E+02	.000000E+00	.912560E-03	.000000E+00	
4	.421399E+02	.000000E+00	.768469E-03	.000000E+00	
5	.423478E+02	.000000E+00	.480417E-03	.000000E+00	
6	.424463E+02	.000000E+00	.392654E-06	.000000E+00	
7	.423480E+02	.000000E+00	-.479636E-03	.000000E+00	
8	.421403E+02	.000000E+00	-.767695E-03	.000000E+00	
9	.418737E+02	.000000E+00	-.911791E-03	.000000E+00	
10	.415841E+02	.000000E+00	-.959937E-03	.000000E+00	
11	.412932E+02	.000000E+00	-.960143E-03	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.283206E+04	.189067E+02	.000000E+00		
2	.141778E+05	.567215E+02	.000000E+00		
3	.368643E+05	.945234E+02	.000000E+00		

```

4 .708912E+05 .132318E+03 .000000E+00
5 .116255E+06 .170102E+03 .000000E+00
6 .116256E+06 -.170105E+03 .000000E+00
7 .708929E+05 -.132322E+03 .000000E+00
8 .368656E+05 -.945218E+02 .000000E+00
9 .141785E+05 -.567185E+02 .000000E+00
10 .283313E+04 -.189092E+02 .000000E+00
0) ITERATION NUMBER= 4
0) CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308624E+02
0) NODE  DISPL.      REACTION    DISPL.      REACTION
   1 .552910E+02    .000000E+00  .941146E-03    .000000E+00
   2 .555769E+02    .000000E+00  .944925E-03    .000000E+00
   3 .558625E+02    .000000E+00  .900760E-03    .000000E+00
   4 .561264E+02    .000000E+00  .760645E-03    .000000E+00
   5 .563326E+02    .000000E+00  .476568E-03    .000000E+00
   6 .564306E+02    .000000E+00  .517624E-06    .000000E+00
   7 .563329E+02    .000000E+00  -.475537E-03   .000000E+00
   8 .561270E+02    .000000E+00  -.759621E-03   .000000E+00
   9 .558634E+02    .000000E+00  -.899741E-03   .000000E+00
  10 .555781E+02    .000000E+00  -.943908E-03   .000000E+00
  11 .552926E+02    .000000E+00  -.940134E-03   .000000E+00
0) ELEMENT      STRESSES     PL STRAIN
   1 .283211E+04  .189151E+02  .000000E+00
   2 .141780E+05  .567250E+02  .000000E+00
   3 .368648E+05  .945198E+02  .000000E+00
   4 .708919E+05  .132323E+03  .000000E+00
   5 .116256E+06  .170113E+03  .000000E+00
   6 .116257E+06  -.170107E+03  .000000E+00
   7 .708936E+05  -.132318E+03  .000000E+00
   8 .368660E+05  -.945282E+02  .000000E+00
   9 .141787E+05  -.567262E+02  .000000E+00
  10 .283318E+04  -.189036E+02  .000000E+00
0) ITERATION NUMBER= 5
0) CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308666E+02
0) NODE  DISPL.      REACTION    DISPL.      REACTION
   1 .692900E+02    .000000E+00  .921377E-03    .000000E+00
   2 .695705E+02    .000000E+00  .929137E-03    .000000E+00
   3 .698520E+02    .000000E+00  .888951E-03    .000000E+00
   4 .701130E+02    .000000E+00  .752815E-03    .000000E+00
   5 .703174E+02    .000000E+00  .472715E-03    .000000E+00
   6 .704149E+02    .000000E+00  .642217E-06    .000000E+00
   7 .703178E+02    .000000E+00  -.471435E-03   .000000E+00
   8 .701138E+02    .000000E+00  -.751541E-03   .000000E+00
   9 .698532E+02    .000000E+00  -.887683E-03   .000000E+00
  10 .695720E+02    .000000E+00  -.927871E-03   .000000E+00
  11 .692919E+02    .000000E+00  -.920116E-03   .000000E+00
0) ELEMENT      STRESSES     PL STRAIN
   1 .283211E+04  .189112E+02  .000000E+00
   2 .141780E+05  .567275E+02  .000000E+00
   3 .368648E+05  .945309E+02  .000000E+00
   4 .708919E+05  .132314E+03  .000000E+00
   5 .116256E+06  .170109E+03  .000000E+00
   6 .116257E+06  -.170111E+03  .000000E+00
   7 .708936E+05  -.132318E+03  .000000E+00
   8 .368661E+05  -.945233E+02  .000000E+00
   9 .141787E+05  -.567308E+02  .000000E+00
  10 .283319E+04  -.189081E+02  .000000E+00
0) ITERATION NUMBER= 6
0) CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308717E+02
0) NODE  DISPL.      REACTION    DISPL.      REACTION

```

	1	.832890E+02	.000000E+00	.901611E-03	.000000E+00
	2	.835642E+02	.000000E+00	.913351E-03	.000000E+00
	3	.838415E+02	.000000E+00	.877145E-03	.000000E+00
	4	.840996E+02	.000000E+00	.744987E-03	.000000E+00
	5	.843022E+02	.000000E+00	.468865E-03	.000000E+00
	6	.843991E+02	.000000E+00	.769919E-06	.000000E+00
	7	.843027E+02	.000000E+00	-.467330E-03	.000000E+00
	8	.841005E+02	.000000E+00	-.743458E-03	.000000E+00
	9	.838429E+02	.000000E+00	-.875621E-03	.000000E+00
	10	.835660E+02	.000000E+00	-.911829E-03	.000000E+00
	11	.832913E+02	.000000E+00	-.900093E-03	.000000E+00
0	ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189152E+02	.000000E+00		
2	.141780E+05	.567193E+02	.000000E+00		
3	.368648E+05	.945251E+02	.000000E+00		
4	.708919E+05	.132318E+03	.000000E+00		
5	.116256E+06	.170112E+03	.000000E+00		
6	.116257E+06	-.170104E+03	.000000E+00		
7	.708935E+05	-.132312E+03	.000000E+00		
8	.368660E+05	-.945262E+02	.000000E+00		
9	.141787E+05	-.567197E+02	.000000E+00		
10	.283315E+04	-.189097E+02	.000000E+00		
0	ITERATION NUMBER=	7			
0	CONVERGENCE CODE=	999	NORM OF RESIDUAL SUM RATIO=	.308738E+02	
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.972880E+02	.000000E+00	.881844E-03	.000000E+00	
2	.975578E+02	.000000E+00	.897565E-03	.000000E+00	
3	.978311E+02	.000000E+00	.865339E-03	.000000E+00	
4	.980861E+02	.000000E+00	.737159E-03	.000000E+00	
5	.982870E+02	.000000E+00	.465015E-03	.000000E+00	
6	.983834E+02	.000000E+00	.897078E-06	.000000E+00	
7	.982876E+02	.000000E+00	-.463225E-03	.000000E+00	
8	.980872E+02	.000000E+00	-.735376E-03	.000000E+00	
9	.978327E+02	.000000E+00	-.863560E-03	.000000E+00	
10	.975600E+02	.000000E+00	-.895790E-03	.000000E+00	
11	.972906E+02	.000000E+00	-.880073E-03	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189130E+02	.000000E+00		
2	.141780E+05	.567233E+02	.000000E+00		
3	.368648E+05	.945254E+02	.000000E+00		
4	.708919E+05	.132322E+03	.000000E+00		
5	.116256E+06	.170109E+03	.000000E+00		
6	.116257E+06	-.170107E+03	.000000E+00		
7	.708936E+05	-.132316E+03	.000000E+00		
8	.368660E+05	-.945203E+02	.000000E+00		
9	.141787E+05	-.567172E+02	.000000E+00		
10	.283319E+04	-.189129E+02	.000000E+00		
0	ITERATION NUMBER=	8			
0	CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.308706E+02	
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.111287E+03	.000000E+00	.862079E-03	.000000E+00	
2	.111551E+03	.000000E+00	.881781E-03	.000000E+00	
3	.111821E+03	.000000E+00	.853534E-03	.000000E+00	
4	.112073E+03	.000000E+00	.729333E-03	.000000E+00	
5	.112272E+03	.000000E+00	.461166E-03	.000000E+00	
6	.112368E+03	.000000E+00	.102571E-05	.000000E+00	
7	.112272E+03	.000000E+00	-.459119E-03	.000000E+00	
8	.112074E+03	.000000E+00	-.727292E-03	.000000E+00	
9	.111822E+03	.000000E+00	-.851498E-03	.000000E+00	
10	.111554E+03	.000000E+00	-.879748E-03	.000000E+00	

11 .111290E+03 .000000E+00 -.860050E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189145E+02 .000000E+00  
 2 .141780E+05 .567250E+02 .000000E+00  
 3 .368648E+05 .945234E+02 .000000E+00  
 4 .708919E+05 .132318E+03 .000000E+00  
 5 .116256E+06 .170110E+03 .000000E+00  
 6 .116257E+06 -.170101E+03 .000000E+00  
 7 .708936E+05 -.132318E+03 .000000E+00  
 8 .368661E+05 -.945237E+02 .000000E+00  
 9 .141788E+05 -.567243E+02 .000000E+00  
 10 .283321E+04 -.189138E+02 .000000E+00  
 0 ITERATION NUMBER= 9  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308743E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .125286E+03 .000000E+00 .842310E-03 .000000E+00  
 2 .125545E+03 .000000E+00 .865992E-03 .000000E+00  
 3 .125810E+03 .000000E+00 .841725E-03 .000000E+00  
 4 .126059E+03 .000000E+00 .721502E-03 .000000E+00  
 5 .126257E+03 .000000E+00 .457313E-03 .000000E+00  
 6 .126352E+03 .000000E+00 .114991E-05 .000000E+00  
 7 .126257E+03 .000000E+00 -.455017E-03 .000000E+00  
 8 .126061E+03 .000000E+00 -.719213E-03 .000000E+00  
 9 .125812E+03 .000000E+00 -.839441E-03 .000000E+00  
 10 .125548E+03 .000000E+00 -.863711E-03 .000000E+00  
 11 .125289E+03 .000000E+00 -.840032E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189114E+02 .000000E+00  
 2 .141780E+05 .567160E+02 .000000E+00  
 3 .368648E+05 .945229E+02 .000000E+00  
 4 .708919E+05 .132316E+03 .000000E+00  
 5 .116256E+06 .170106E+03 .000000E+00  
 6 .116257E+06 -.170111E+03 .000000E+00  
 7 .708936E+05 -.132322E+03 .000000E+00  
 8 .368661E+05 -.945243E+02 .000000E+00  
 9 .141787E+05 -.567225E+02 .000000E+00  
 10 .283319E+04 -.189121E+02 .000000E+00  
 0 ITERATION NUMBER= 10  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308653E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .139285E+03 .000000E+00 .822542E-03 .000000E+00  
 2 .139539E+03 .000000E+00 .850205E-03 .000000E+00  
 3 .139800E+03 .000000E+00 .829916E-03 .000000E+00  
 4 .140046E+03 .000000E+00 .713672E-03 .000000E+00  
 5 .140241E+03 .000000E+00 .453461E-03 .000000E+00  
 6 .140336E+03 .000000E+00 .127557E-05 .000000E+00  
 7 .140242E+03 .000000E+00 -.450914E-03 .000000E+00  
 8 .140047E+03 .000000E+00 -.711132E-03 .000000E+00  
 9 .139802E+03 .000000E+00 -.827381E-03 .000000E+00  
 10 .139542E+03 .000000E+00 -.847671E-03 .000000E+00  
 11 .139289E+03 .000000E+00 -.820011E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189008E+02 .000000E+00  
 2 .141780E+05 .567239E+02 .000000E+00  
 3 .368648E+05 .945270E+02 .000000E+00  
 4 .708919E+05 .132324E+03 .000000E+00  
 5 .116256E+06 .170113E+03 .000000E+00  
 6 .116257E+06 -.170112E+03 .000000E+00  
 7 .708935E+05 -.132319E+03 .000000E+00  
 8 .368660E+05 -.945233E+02 .000000E+00

9 .141787E+05 -.567197E+02 .000000E+00  
 10 .283315E+04 -.189158E+02 .000000E+00  
 0 ITERATION NUMBER= 11  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308690E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .153284E+03 .000000E+00 .802773E-03 .000000E+00  
 2 .153532E+03 .000000E+00 .834417E-03 .000000E+00  
 3 .153789E+03 .000000E+00 .818108E-03 .000000E+00  
 4 .154032E+03 .000000E+00 .705842E-03 .000000E+00  
 5 .154226E+03 .000000E+00 .449609E-03 .000000E+00  
 6 .154320E+03 .000000E+00 .140045E-05 .000000E+00  
 7 .154227E+03 .000000E+00 -.446812E-03 .000000E+00  
 8 .154034E+03 .000000E+00 -.703052E-03 .000000E+00  
 9 .153792E+03 .000000E+00 -.815323E-03 .000000E+00  
 10 .153536E+03 .000000E+00 -.831634E-03 .000000E+00  
 11 .153288E+03 .000000E+00 -.799993E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189027E+02 .000000E+00  
 2 .141780E+05 .567259E+02 .000000E+00  
 3 .368648E+05 .945314E+02 .000000E+00  
 4 .708919E+05 .132326E+03 .000000E+00  
 5 .116256E+06 .170108E+03 .000000E+00  
 6 .116257E+06 -.170111E+03 .000000E+00  
 7 .708936E+05 -.132318E+03 .000000E+00  
 8 .368661E+05 -.945245E+02 .000000E+00  
 9 .141787E+05 -.567306E+02 .000000E+00  
 10 .283319E+04 -.189143E+02 .000000E+00  
 0 ITERATION NUMBER= 12  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308595E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .167283E+03 .000000E+00 .783004E-03 .000000E+00  
 2 .167526E+03 .000000E+00 .818629E-03 .000000E+00  
 3 .167779E+03 .000000E+00 .806299E-03 .000000E+00  
 4 .168019E+03 .000000E+00 .698012E-03 .000000E+00  
 5 .168211E+03 .000000E+00 .445757E-03 .000000E+00  
 6 .168305E+03 .000000E+00 .152541E-05 .000000E+00  
 7 .168212E+03 .000000E+00 -.442710E-03 .000000E+00  
 8 .168021E+03 .000000E+00 -.694972E-03 .000000E+00  
 9 .167781E+03 .000000E+00 -.803264E-03 .000000E+00  
 10 .167530E+03 .000000E+00 -.815596E-03 .000000E+00  
 11 .167287E+03 .000000E+00 -.779975E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189048E+02 .000000E+00  
 2 .141780E+05 .567220E+02 .000000E+00  
 3 .368648E+05 .945239E+02 .000000E+00  
 4 .708919E+05 .132323E+03 .000000E+00  
 5 .116256E+06 .170110E+03 .000000E+00  
 6 .116257E+06 -.170104E+03 .000000E+00  
 7 .708936E+05 -.132325E+03 .000000E+00  
 8 .368661E+05 -.945270E+02 .000000E+00  
 9 .141787E+05 -.567246E+02 .000000E+00  
 10 .283319E+04 -.189142E+02 .000000E+00  
 0 ITERATION NUMBER= 13  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308835E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .181282E+03 .000000E+00 .763237E-03 .000000E+00  
 2 .181520E+03 .000000E+00 .802842E-03 .000000E+00  
 3 .181768E+03 .000000E+00 .794492E-03 .000000E+00  
 4 .182006E+03 .000000E+00 .690183E-03 .000000E+00  
 5 .182196E+03 .000000E+00 .441906E-03 .000000E+00

6 .182289E+03 .000000E+00 .165202E-05 .000000E+00  
 7 .182197E+03 .000000E+00 -.438605E-03 .000000E+00  
 8 .182008E+03 .000000E+00 -.686890E-03 .000000E+00  
 9 .181771E+03 .000000E+00 -.791203E-03 .000000E+00  
 10 .181524E+03 .000000E+00 -.799556E-03 .000000E+00  
 11 .181287E+03 .000000E+00 -.759953E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189170E+02 .000000E+00  
 2 .141780E+05 .567282E+02 .000000E+00  
 3 .368648E+05 .945263E+02 .000000E+00  
 4 .708919E+05 .132323E+03 .000000E+00  
 5 .116256E+06 .170108E+03 .000000E+00  
 6 .116257E+06 -.170107E+03 .000000E+00  
 7 .708936E+05 -.132311E+03 .000000E+00  
 8 .368661E+05 -.945216E+02 .000000E+00  
 9 .141787E+05 -.567231E+02 .000000E+00  
 10 .283319E+04 -.189128E+02 .000000E+00  
 0 ITERATION NUMBER= 14  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308754E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .195281E+03 .000000E+00 .743468E-03 .000000E+00  
 2 .195513E+03 .000000E+00 .787055E-03 .000000E+00  
 3 .195758E+03 .000000E+00 .782684E-03 .000000E+00  
 4 .195992E+03 .000000E+00 .682353E-03 .000000E+00  
 5 .196181E+03 .000000E+00 .438054E-03 .000000E+00  
 6 .196273E+03 .000000E+00 .177730E-05 .000000E+00  
 7 .196182E+03 .000000E+00 -.434503E-03 .000000E+00  
 8 .195994E+03 .000000E+00 -.678809E-03 .000000E+00  
 9 .195761E+03 .000000E+00 -.779144E-03 .000000E+00  
 10 .195518E+03 .000000E+00 -.783517E-03 .000000E+00  
 11 .195286E+03 .000000E+00 -.739934E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189120E+02 .000000E+00  
 2 .141780E+05 .567233E+02 .000000E+00  
 3 .368648E+05 .945300E+02 .000000E+00  
 4 .708919E+05 .132324E+03 .000000E+00  
 5 .116256E+06 .170103E+03 .000000E+00  
 6 .116257E+06 -.170113E+03 .000000E+00  
 7 .708936E+05 -.132318E+03 .000000E+00  
 8 .368660E+05 -.945308E+02 .000000E+00  
 9 .141787E+05 -.567180E+02 .000000E+00  
 10 .283316E+04 -.189141E+02 .000000E+00  
 0 ITERATION NUMBER= 15  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308728E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .209280E+03 .000000E+00 .723698E-03 .000000E+00  
 2 .209507E+03 .000000E+00 .771265E-03 .000000E+00  
 3 .209747E+03 .000000E+00 .770874E-03 .000000E+00  
 4 .209979E+03 .000000E+00 .674522E-03 .000000E+00  
 5 .210166E+03 .000000E+00 .434200E-03 .000000E+00  
 6 .210257E+03 .000000E+00 .190059E-05 .000000E+00  
 7 .210167E+03 .000000E+00 -.430402E-03 .000000E+00  
 8 .209981E+03 .000000E+00 -.670731E-03 .000000E+00  
 9 .209751E+03 .000000E+00 -.767088E-03 .000000E+00  
 10 .209512E+03 .000000E+00 -.767481E-03 .000000E+00  
 11 .209286E+03 .000000E+00 -.719917E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189050E+02 .000000E+00  
 2 .141780E+05 .567165E+02 .000000E+00  
 3 .368648E+05 .945195E+02 .000000E+00

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4 .708919E+05 .132312E+03 .000000E+00
5 .116256E+06 .170108E+03 .000000E+00
6 .116257E+06 -.170108E+03 .000000E+00
7 .708936E+05 -.132314E+03 .000000E+00
8 .368661E+05 -.945234E+02 .000000E+00
9 .141787E+05 -.567264E+02 .000000E+00
10 .283317E+04 -.189102E+02 .000000E+00
0 ITERATION NUMBER= 16
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308681E+02
0 NODE DISPL. REACTION DISPL. REACTION
 1 .223279E+03 .000000E+00 .703930E-03 .000000E+00
 2 .223501E+03 .000000E+00 .755477E-03 .000000E+00
 3 .223737E+03 .000000E+00 .759066E-03 .000000E+00
 4 .223965E+03 .000000E+00 .666692E-03 .000000E+00
 5 .224150E+03 .000000E+00 .430348E-03 .000000E+00
 6 .224242E+03 .000000E+00 .202627E-05 .000000E+00
 7 .224152E+03 .000000E+00 -.426299E-03 .000000E+00
 8 .223968E+03 .000000E+00 -.662650E-03 .000000E+00
 9 .223740E+03 .000000E+00 -.755028E-03 .000000E+00
10 .223506E+03 .000000E+00 -.751441E-03 .000000E+00
11 .223285E+03 .000000E+00 -.699897E-03 .000000E+00
0 ELEMENT STRESSES PL STRAIN
 1 .283211E+04 .189067E+02 .000000E+00
 2 .141780E+05 .567244E+02 .000000E+00
 3 .368648E+05 .945236E+02 .000000E+00
 4 .708919E+05 .132320E+03 .000000E+00
 5 .116256E+06 .170108E+03 .000000E+00
 6 .116257E+06 -.170109E+03 .000000E+00
 7 .708935E+05 -.132317E+03 .000000E+00
 8 .368660E+05 -.945163E+02 .000000E+00
 9 .141787E+05 -.567234E+02 .000000E+00
10 .283318E+04 -.189133E+02 .000000E+00
0 ITERATION NUMBER= 17
0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308727E+02
0 NODE DISPL. REACTION DISPL. REACTION
 1 .237278E+03 .000000E+00 .684162E-03 .000000E+00
 2 .237494E+03 .000000E+00 .739691E-03 .000000E+00
 3 .237726E+03 .000000E+00 .747258E-03 .000000E+00
 4 .237952E+03 .000000E+00 .658863E-03 .000000E+00
 5 .238135E+03 .000000E+00 .426497E-03 .000000E+00
 6 .238226E+03 .000000E+00 .215285E-05 .000000E+00
 7 .238137E+03 .000000E+00 -.422195E-03 .000000E+00
 8 .237954E+03 .000000E+00 -.654568E-03 .000000E+00
 9 .237730E+03 .000000E+00 -.742968E-03 .000000E+00
10 .237500E+03 .000000E+00 -.735402E-03 .000000E+00
11 .237284E+03 .000000E+00 -.679876E-03 .000000E+00
0 ELEMENT STRESSES PL STRAIN
 1 .283211E+04 .189121E+02 .000000E+00
 2 .141780E+05 .567177E+02 .000000E+00
 3 .368648E+05 .945254E+02 .000000E+00
 4 .708919E+05 .132320E+03 .000000E+00
 5 .116256E+06 .170113E+03 .000000E+00
 6 .116257E+06 -.170099E+03 .000000E+00
 7 .708936E+05 -.132326E+03 .000000E+00
 8 .368660E+05 -.945217E+02 .000000E+00
 9 .141787E+05 -.567204E+02 .000000E+00
10 .283319E+04 -.189164E+02 .000000E+00
0 ITERATION NUMBER= 18
0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308728E+02
0 NODE DISPL. REACTION DISPL. REACTION

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	1	.251277E+03	.000000E+00	.664394E-03	.000000E+00
	2	.251488E+03	.000000E+00	.723903E-03	.000000E+00
	3	.251716E+03	.000000E+00	.735450E-03	.000000E+00
	4	.251938E+03	.000000E+00	.651033E-03	.000000E+00
	5	.252120E+03	.000000E+00	.422644E-03	.000000E+00
	6	.252210E+03	.000000E+00	.227748E-05	.000000E+00
	7	.252121E+03	.000000E+00	-.418093E-03	.000000E+00
	8	.251941E+03	.000000E+00	-.646489E-03	.000000E+00
	9	.251720E+03	.000000E+00	-.730910E-03	.000000E+00
	10	.251493E+03	.000000E+00	-.719365E-03	.000000E+00
	11	.251284E+03	.000000E+00	-.659858E-03	.000000E+00
0	ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189082E+02	.000000E+00		
2	.141780E+05	.567263E+02	.000000E+00		
3	.368648E+05	.945242E+02	.000000E+00		
4	.708919E+05	.132310E+03	.000000E+00		
5	.116256E+06	.170109E+03	.000000E+00		
6	.116257E+06	-.170110E+03	.000000E+00		
7	.708936E+05	-.132319E+03	.000000E+00		
8	.368661E+05	-.945226E+02	.000000E+00		
9	.141787E+05	-.567309E+02	.000000E+00		
10	.283317E+04	-.189147E+02	.000000E+00		
0	ITERATION NUMBER=	19			
0	CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.308703E+02	
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.265276E+03	.000000E+00	.644622E-03	.000000E+00	
2	.265482E+03	.000000E+00	.708112E-03	.000000E+00	
3	.265705E+03	.000000E+00	.723638E-03	.000000E+00	
4	.265925E+03	.000000E+00	.643200E-03	.000000E+00	
5	.266105E+03	.000000E+00	.418789E-03	.000000E+00	
6	.266194E+03	.000000E+00	.239958E-05	.000000E+00	
7	.266106E+03	.000000E+00	-.413993E-03	.000000E+00	
8	.265928E+03	.000000E+00	-.638411E-03	.000000E+00	
9	.265710E+03	.000000E+00	-.718854E-03	.000000E+00	
10	.265487E+03	.000000E+00	-.703329E-03	.000000E+00	
11	.265283E+03	.000000E+00	-.639841E-03	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189040E+02	.000000E+00		
2	.141780E+05	.567160E+02	.000000E+00		
3	.368648E+05	.945164E+02	.000000E+00		
4	.708919E+05	.132319E+03	.000000E+00		
5	.116256E+06	.170110E+03	.000000E+00		
6	.116257E+06	-.170110E+03	.000000E+00		
7	.708936E+05	-.132315E+03	.000000E+00		
8	.368661E+05	-.945266E+02	.000000E+00		
9	.141787E+05	-.567207E+02	.000000E+00		
10	.283317E+04	-.189107E+02	.000000E+00		
0	ITERATION NUMBER=	20			
0	CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.308558E+02	
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.279275E+03	.000000E+00	.624853E-03	.000000E+00	
2	.279475E+03	.000000E+00	.692324E-03	.000000E+00	
3	.279695E+03	.000000E+00	.711830E-03	.000000E+00	
4	.279912E+03	.000000E+00	.635370E-03	.000000E+00	
5	.280090E+03	.000000E+00	.414936E-03	.000000E+00	
6	.280179E+03	.000000E+00	.252458E-05	.000000E+00	
7	.280091E+03	.000000E+00	-.409891E-03	.000000E+00	
8	.279915E+03	.000000E+00	-.630331E-03	.000000E+00	
9	.279699E+03	.000000E+00	-.706795E-03	.000000E+00	
10	.279481E+03	.000000E+00	-.687291E-03	.000000E+00	

11	.279282E+03	.000000E+00	-.619823E-03	.000000E+00	
0 ELEMENT	STRESSES	PL STRAIN			
1	.283211E+04	.189062E+02	.000000E+00		
2	.141780E+05	.567245E+02	.000000E+00		
3	.368648E+05	.945273E+02	.000000E+00		
4	.708919E+05	.132321E+03	.000000E+00		
5	.116256E+06	.170111E+03	.000000E+00		
6	.116257E+06	-.170103E+03	.000000E+00		
7	.708936E+05	-.132321E+03	.000000E+00		
8	.368661E+05	-.945290E+02	.000000E+00		
9	.141787E+05	-.567208E+02	.000000E+00		
10	.283320E+04	-.189108E+02	.000000E+00		
0	ITERATION NUMBER=	21			
0	CONVERGENCE CODE=	999	NORM OF RESIDUAL SUM RATIO=	.308629E+02	
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.293274E+03	.000000E+00	.605084E-03	.000000E+00	
2	.293469E+03	.000000E+00	.676536E-03	.000000E+00	
3	.293684E+03	.000000E+00	.700021E-03	.000000E+00	
4	.293898E+03	.000000E+00	.627539E-03	.000000E+00	
5	.294075E+03	.000000E+00	.411084E-03	.000000E+00	
6	.294163E+03	.000000E+00	.264932E-05	.000000E+00	
7	.294076E+03	.000000E+00	-.405789E-03	.000000E+00	
8	.293901E+03	.000000E+00	-.622251E-03	.000000E+00	
9	.293689E+03	.000000E+00	-.694737E-03	.000000E+00	
10	.293475E+03	.000000E+00	-.671253E-03	.000000E+00	
11	.293282E+03	.000000E+00	-.599804E-03	.000000E+00	
0 ELEMENT	STRESSES	PL STRAIN			
1	.283211E+04	.189084E+02	.000000E+00		
2	.141780E+05	.567269E+02	.000000E+00		
3	.368648E+05	.945260E+02	.000000E+00		
4	.708919E+05	.132312E+03	.000000E+00		
5	.116256E+06	.170107E+03	.000000E+00		
6	.116257E+06	-.170108E+03	.000000E+00		
7	.708936E+05	-.132315E+03	.000000E+00		
8	.368661E+05	-.945308E+02	.000000E+00		
9	.141787E+05	-.567262E+02	.000000E+00		
10	.283320E+04	-.189099E+02	.000000E+00		
0	ITERATION NUMBER=	22			
0	CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.308601E+02	
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.307273E+03	.000000E+00	.585314E-03	.000000E+00	
2	.307463E+03	.000000E+00	.660747E-03	.000000E+00	
3	.307674E+03	.000000E+00	.688212E-03	.000000E+00	
4	.307885E+03	.000000E+00	.619708E-03	.000000E+00	
5	.308059E+03	.000000E+00	.407230E-03	.000000E+00	
6	.308147E+03	.000000E+00	.277350E-05	.000000E+00	
7	.308061E+03	.000000E+00	-.401687E-03	.000000E+00	
8	.307888E+03	.000000E+00	-.614172E-03	.000000E+00	
9	.307679E+03	.000000E+00	-.682679E-03	.000000E+00	
10	.307469E+03	.000000E+00	-.655216E-03	.000000E+00	
11	.307281E+03	.000000E+00	-.579786E-03	.000000E+00	
0 ELEMENT	STRESSES	PL STRAIN			
1	.283211E+04	.189065E+02	.000000E+00		
2	.141780E+05	.567189E+02	.000000E+00		
3	.368648E+05	.945265E+02	.000000E+00		
4	.708919E+05	.132316E+03	.000000E+00		
5	.116256E+06	.170110E+03	.000000E+00		
6	.116257E+06	-.170112E+03	.000000E+00		
7	.708936E+05	-.132314E+03	.000000E+00		
8	.368661E+05	-.945259E+02	.000000E+00		

9 .141787E+05 -.567252E+02 .000000E+00  
 10 .283320E+04 -.189091E+02 .000000E+00  
 0 ITERATION NUMBER= 23  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308720E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .321272E+03 .000000E+00 .565543E-03 .000000E+00  
 2 .321456E+03 .000000E+00 .644956E-03 .000000E+00  
 3 .321663E+03 .000000E+00 .676400E-03 .000000E+00  
 4 .321871E+03 .000000E+00 .611875E-03 .000000E+00  
 5 .322044E+03 .000000E+00 .403375E-03 .000000E+00  
 6 .322131E+03 .000000E+00 .289545E-05 .000000E+00  
 7 .322046E+03 .000000E+00 -.397588E-03 .000000E+00  
 8 .321875E+03 .000000E+00 -.606094E-03 .000000E+00  
 9 .321669E+03 .000000E+00 -.670624E-03 .000000E+00  
 10 .321463E+03 .000000E+00 -.639181E-03 .000000E+00  
 11 .321280E+03 .000000E+00 -.559770E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189082E+02 .000000E+00  
 2 .141780E+05 .567208E+02 .000000E+00  
 3 .368648E+05 .945247E+02 .000000E+00  
 4 .708919E+05 .132312E+03 .000000E+00  
 5 .116256E+06 .170112E+03 .000000E+00  
 6 .116257E+06 -.170112E+03 .000000E+00  
 7 .708936E+05 -.132315E+03 .000000E+00  
 8 .368661E+05 -.945229E+02 .000000E+00  
 9 .141788E+05 -.567198E+02 .000000E+00  
 10 .283321E+04 -.189158E+02 .000000E+00  
 0 ITERATION NUMBER= 24  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308681E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .335271E+03 .000000E+00 .545772E-03 .000000E+00  
 2 .335450E+03 .000000E+00 .629165E-03 .000000E+00  
 3 .335653E+03 .000000E+00 .664589E-03 .000000E+00  
 4 .335858E+03 .000000E+00 .604042E-03 .000000E+00  
 5 .336029E+03 .000000E+00 .399520E-03 .000000E+00  
 6 .336116E+03 .000000E+00 .301802E-05 .000000E+00  
 7 .336031E+03 .000000E+00 -.393488E-03 .000000E+00  
 8 .335862E+03 .000000E+00 -.598017E-03 .000000E+00  
 9 .335658E+03 .000000E+00 -.658568E-03 .000000E+00  
 10 .335457E+03 .000000E+00 -.623145E-03 .000000E+00  
 11 .335280E+03 .000000E+00 -.539754E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189030E+02 .000000E+00  
 2 .141780E+05 .567157E+02 .000000E+00  
 3 .368648E+05 .945220E+02 .000000E+00  
 4 .708919E+05 .132314E+03 .000000E+00  
 5 .116256E+06 .170112E+03 .000000E+00  
 6 .116257E+06 -.170106E+03 .000000E+00  
 7 .708936E+05 -.132316E+03 .000000E+00  
 8 .368661E+05 -.945204E+02 .000000E+00  
 9 .141788E+05 -.567272E+02 .000000E+00  
 10 .283321E+04 -.189110E+02 .000000E+00  
 0 ITERATION NUMBER= 25  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308660E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .349270E+03 .000000E+00 .526002E-03 .000000E+00  
 2 .349444E+03 .000000E+00 .613377E-03 .000000E+00  
 3 .349642E+03 .000000E+00 .652780E-03 .000000E+00  
 4 .349844E+03 .000000E+00 .596212E-03 .000000E+00  
 5 .350014E+03 .000000E+00 .395668E-03 .000000E+00

	STRESSES	PL STRAIN		
6	.350100E+03	.000000E+00 .314297E-05	.000000E+00	
7	.350016E+03	.000000E+00 -.389385E-03	.000000E+00	
8	.349848E+03	.000000E+00 -.589936E-03	.000000E+00	
9	.349648E+03	.000000E+00 -.646508E-03	.000000E+00	
10	.349451E+03	.000000E+00 -.607106E-03	.000000E+00	
11	.349279E+03	.000000E+00 -.519734E-03	.000000E+00	
0 ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189057E+02 .000000E+00		
2	.141780E+05	.567186E+02 .000000E+00		
3	.368648E+05	.945272E+02 .000000E+00		
4	.708919E+05	.132317E+03 .000000E+00		
5	.116256E+06	.170107E+03 .000000E+00		
6	.116257E+06	-.170112E+03 .000000E+00		
7	.708936E+05	-.132324E+03 .000000E+00		
8	.368660E+05	-.945242E+02 .000000E+00		
9	.141787E+05	-.567169E+02 .000000E+00		
10	.283319E+04	-.189071E+02 .000000E+00		
0 ITERATION NUMBER= 26				
0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308823E+02				
0 NODE	DISPL.	REACTION	DISPL.	REACTION
1	.363269E+03	.000000E+00	.506236E-03	.000000E+00
2	.363437E+03	.000000E+00	.597592E-03	.000000E+00
3	.363632E+03	.000000E+00	.640974E-03	.000000E+00
4	.363831E+03	.000000E+00	.588384E-03	.000000E+00
5	.363999E+03	.000000E+00	.391818E-03	.000000E+00
6	.364084E+03	.000000E+00	.327089E-05	.000000E+00
7	.364001E+03	.000000E+00	-.385280E-03	.000000E+00
8	.363835E+03	.000000E+00	-.581853E-03	.000000E+00
9	.363638E+03	.000000E+00	-.634446E-03	.000000E+00
10	.363445E+03	.000000E+00	-.591065E-03	.000000E+00
11	.363279E+03	.000000E+00	-.499711E-03	.000000E+00
0 ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189153E+02 .000000E+00		
2	.141780E+05	.567221E+02 .000000E+00		
3	.368648E+05	.945269E+02 .000000E+00		
4	.708919E+05	.132320E+03 .000000E+00		
5	.116256E+06	.170109E+03 .000000E+00		
6	.116257E+06	-.170098E+03 .000000E+00		
7	.708935E+05	-.132312E+03 .000000E+00		
8	.368660E+05	-.945208E+02 .000000E+00		
9	.141787E+05	-.567237E+02 .000000E+00		
10	.283318E+04	-.189140E+02 .000000E+00		
0 ITERATION NUMBER= 27				
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308761E+02				
0 NODE	DISPL.	REACTION	DISPL.	REACTION
1	.377268E+03	.000000E+00	.486465E-03	.000000E+00
2	.377431E+03	.000000E+00	.581802E-03	.000000E+00
3	.377621E+03	.000000E+00	.629163E-03	.000000E+00
4	.377818E+03	.000000E+00	.580552E-03	.000000E+00
5	.377983E+03	.000000E+00	.387963E-03	.000000E+00
6	.378068E+03	.000000E+00	.339325E-05	.000000E+00
7	.377985E+03	.000000E+00	-.381180E-03	.000000E+00
8	.377822E+03	.000000E+00	-.573776E-03	.000000E+00
9	.377628E+03	.000000E+00	-.622391E-03	.000000E+00
10	.377439E+03	.000000E+00	-.575030E-03	.000000E+00
11	.377278E+03	.000000E+00	-.479696E-03	.000000E+00
0 ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189032E+02 .000000E+00		
2	.141780E+05	.567163E+02 .000000E+00		
3	.368648E+05	.945175E+02 .000000E+00		

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4 .708919E+05 .132321E+03 .000000E+00
5 .116256E+06 .170104E+03 .000000E+00
6 .116257E+06 -.170105E+03 .000000E+00
7 .708936E+05 -.132313E+03 .000000E+00
8 .368661E+05 -.945236E+02 .000000E+00
9 .141788E+05 -.567176E+02 .000000E+00
10 .283319E+04 -.189137E+02 .000000E+00
0) ITERATION NUMBER= 28
0) CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308705E+02
0) NODE  DISPL.      REACTION      DISPL.      REACTION
   1 .391267E+03    .000000E+00  .466698E-03    .000000E+00
   2 .391425E+03    .000000E+00  .566015E-03    .000000E+00
   3 .391611E+03    .000000E+00  .617356E-03    .000000E+00
   4 .391804E+03    .000000E+00  .572723E-03    .000000E+00
   5 .391968E+03    .000000E+00  .384112E-03    .000000E+00
   6 .392053E+03    .000000E+00  .351936E-05    .000000E+00
   7 .391970E+03    .000000E+00  -.377077E-03   .000000E+00
   8 .391808E+03    .000000E+00  -.565694E-03   .000000E+00
   9 .391617E+03    .000000E+00  -.610331E-03   .000000E+00
  10 .391433E+03   .000000E+00  -.558991E-03   .000000E+00
  11 .391277E+03   .000000E+00  -.459675E-03   .000000E+00
0) ELEMENT      STRESSES      PL STRAIN
   1 .283211E+04  .189094E+02  .000000E+00
   2 .141780E+05  .567227E+02  .000000E+00
   3 .368648E+05  .945263E+02  .000000E+00
   4 .708919E+05  .132322E+03  .000000E+00
   5 .116256E+06  .170115E+03  .000000E+00
   6 .116257E+06  -.170112E+03  .000000E+00
   7 .708936E+05  -.132322E+03  .000000E+00
   8 .368661E+05  -.945285E+02  .000000E+00
   9 .141787E+05  -.567204E+02  .000000E+00
  10 .283318E+04  -.189167E+02  .000000E+00
0) ITERATION NUMBER= 29
0) CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308718E+02
0) NODE  DISPL.      REACTION      DISPL.      REACTION
   1 .405266E+03    .000000E+00  .446927E-03    .000000E+00
   2 .405418E+03    .000000E+00  .550225E-03    .000000E+00
   3 .405600E+03    .000000E+00  .605545E-03    .000000E+00
   4 .405791E+03    .000000E+00  .564891E-03    .000000E+00
   5 .405953E+03    .000000E+00  .380257E-03    .000000E+00
   6 .406037E+03    .000000E+00  .364228E-05    .000000E+00
   7 .405955E+03    .000000E+00  -.372976E-03   .000000E+00
   8 .405795E+03    .000000E+00  -.557616E-03   .000000E+00
   9 .405607E+03    .000000E+00  -.598275E-03   .000000E+00
  10 .405427E+03   .000000E+00  -.542955E-03   .000000E+00
  11 .405277E+03   .000000E+00  -.439659E-03   .000000E+00
0) ELEMENT      STRESSES      PL STRAIN
   1 .283211E+04  .189032E+02  .000000E+00
   2 .141780E+05  .567166E+02  .000000E+00
   3 .368648E+05  .945227E+02  .000000E+00
   4 .708919E+05  .132310E+03  .000000E+00
   5 .116256E+06  .170108E+03  .000000E+00
   6 .116257E+06  -.170101E+03  .000000E+00
   7 .708936E+05  -.132318E+03  .000000E+00
   8 .368661E+05  -.945204E+02  .000000E+00
   9 .141787E+05  -.567281E+02  .000000E+00
  10 .283320E+04  -.189121E+02  .000000E+00
0) ITERATION NUMBER= 30
0) CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308796E+02
0) NODE  DISPL.      REACTION      DISPL.      REACTION

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	1	.419265E+03	.000000E+00	.427159E-03	.000000E+00		
	2	.419412E+03	.000000E+00	.534437E-03	.000000E+00		
	3	.419590E+03	.000000E+00	.593737E-03	.000000E+00		
	4	.419777E+03	.000000E+00	.557061E-03	.000000E+00		
	5	.419938E+03	.000000E+00	.376406E-03	.000000E+00		
	6	.420021E+03	.000000E+00	.376820E-05	.000000E+00		
	7	.419940E+03	.000000E+00	.368873E-03	.000000E+00		
	8	.419782E+03	.000000E+00	.-549535E-03	.000000E+00		
	9	.419597E+03	.000000E+00	.-586215E-03	.000000E+00		
	10	.419421E+03	.000000E+00	.-526915E-03	.000000E+00		
	11	.419276E+03	.000000E+00	.-419638E-03	.000000E+00		
0 ELEMENT STRESSES PL STRAIN	1	.283211E+04	.189105E+02	.000000E+00			
	2	.141780E+05	.567240E+02	.000000E+00			
	3	.368648E+05	.945263E+02	.000000E+00			
	4	.708919E+05	.132317E+03	.000000E+00			
	5	.116256E+06	.170114E+03	.000000E+00			
	6	.116257E+06	.-170109E+03	.000000E+00			
	7	.708936E+05	.-132321E+03	.000000E+00			
	8	.368661E+05	.-945136E+02	.000000E+00			
	9	.141787E+05	.-567193E+02	.000000E+00			
	10	.283316E+04	.-189158E+02	.000000E+00			
0 ITERATION NUMBER= 31	0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308655E+02	0 NODE DISPL. REACTION DISPL. REACTION	1	.433264E+03	.000000E+00	.407392E-03	.000000E+00
	2	.433405E+03	.000000E+00	.518651E-03	.000000E+00		
	3	.433579E+03	.000000E+00	.581931E-03	.000000E+00		
	4	.433764E+03	.000000E+00	.549233E-03	.000000E+00		
	5	.433923E+03	.000000E+00	.372555E-03	.000000E+00		
	6	.434005E+03	.000000E+00	.389503E-05	.000000E+00		
	7	.433925E+03	.000000E+00	.-364769E-03	.000000E+00		
	8	.433769E+03	.000000E+00	.-541453E-03	.000000E+00		
	9	.433587E+03	.000000E+00	.-574155E-03	.000000E+00		
	10	.433415E+03	.000000E+00	.-510876E-03	.000000E+00		
	11	.433275E+03	.000000E+00	.-399618E-03	.000000E+00		
0 ELEMENT STRESSES PL STRAIN	1	.283211E+04	.189151E+02	.000000E+00			
	2	.141780E+05	.567288E+02	.000000E+00			
	3	.368648E+05	.945212E+02	.000000E+00			
	4	.708919E+05	.132323E+03	.000000E+00			
	5	.116256E+06	.170112E+03	.000000E+00			
	6	.116257E+06	.-170105E+03	.000000E+00			
	7	.708936E+05	.-132318E+03	.000000E+00			
	8	.368661E+05	.-945255E+02	.000000E+00			
	9	.141787E+05	.-567227E+02	.000000E+00			
	10	.283320E+04	.-189067E+02	.000000E+00			
0 ITERATION NUMBER= 32	0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308668E+02	0 NODE DISPL. REACTION DISPL. REACTION	1	.447263E+03	.000000E+00	.387622E-03	.000000E+00
	2	.447399E+03	.000000E+00	.502862E-03	.000000E+00		
	3	.447569E+03	.000000E+00	.570121E-03	.000000E+00		
	4	.447750E+03	.000000E+00	.541401E-03	.000000E+00		
	5	.447908E+03	.000000E+00	.368701E-03	.000000E+00		
	6	.447990E+03	.000000E+00	.401840E-05	.000000E+00		
	7	.447910E+03	.000000E+00	.-360668E-03	.000000E+00		
	8	.447755E+03	.000000E+00	.-533375E-03	.000000E+00		
	9	.447576E+03	.000000E+00	.-562098E-03	.000000E+00		
	10	.447409E+03	.000000E+00	.-494839E-03	.000000E+00		

11	.447275E+03	.000000E+00	-.379600E-03	.000000E+00
0 ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189078E+02	.000000E+00	
2	.141780E+05	.567155E+02	.000000E+00	
3	.368648E+05	.945227E+02	.000000E+00	
4	.708919E+05	.132310E+03	.000000E+00	
5	.116256E+06	.170105E+03	.000000E+00	
6	.116257E+06	-.170102E+03	.000000E+00	
7	.708936E+05	-.132322E+03	.000000E+00	
8	.368661E+05	-.945249E+02	.000000E+00	
9	.141787E+05	-.567261E+02	.000000E+00	
10	.283319E+04	-.189042E+02	.000000E+00	
0	ITERATION NUMBER=	33		
0 CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.308638E+02	
0 NODE	DISPL.	REACTION	DISPL.	REACTION
1	.461262E+03	.000000E+00	.367852E-03	.000000E+00
2	.461393E+03	.000000E+00	.487072E-03	.000000E+00
3	.461558E+03	.000000E+00	.558311E-03	.000000E+00
4	.461737E+03	.000000E+00	.533570E-03	.000000E+00
5	.461892E+03	.000000E+00	.364848E-03	.000000E+00
6	.461974E+03	.000000E+00	.414225E-05	.000000E+00
7	.461895E+03	.000000E+00	-.356567E-03	.000000E+00
8	.461742E+03	.000000E+00	-.525295E-03	.000000E+00
9	.461566E+03	.000000E+00	-.550040E-03	.000000E+00
10	.461403E+03	.000000E+00	-.478802E-03	.000000E+00
11	.461274E+03	.000000E+00	-.359582E-03	.000000E+00
0 ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189126E+02	.000000E+00	
2	.141780E+05	.567204E+02	.000000E+00	
3	.368648E+05	.945238E+02	.000000E+00	
4	.708919E+05	.132315E+03	.000000E+00	
5	.116256E+06	.170109E+03	.000000E+00	
6	.116257E+06	-.170105E+03	.000000E+00	
7	.708936E+05	-.132320E+03	.000000E+00	
8	.368661E+05	-.945255E+02	.000000E+00	
9	.141787E+05	-.567305E+02	.000000E+00	
10	.283317E+04	-.189086E+02	.000000E+00	
0	ITERATION NUMBER=	34		
0 CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.308619E+02	
0 NODE	DISPL.	REACTION	DISPL.	REACTION
1	.475261E+03	.000000E+00	.348083E-03	.000000E+00
2	.475386E+03	.000000E+00	.471284E-03	.000000E+00
3	.475548E+03	.000000E+00	.546502E-03	.000000E+00
4	.475724E+03	.000000E+00	.525739E-03	.000000E+00
5	.475877E+03	.000000E+00	.360995E-03	.000000E+00
6	.475958E+03	.000000E+00	.426694E-05	.000000E+00
7	.475880E+03	.000000E+00	-.352464E-03	.000000E+00
8	.475729E+03	.000000E+00	-.517215E-03	.000000E+00
9	.475556E+03	.000000E+00	-.537982E-03	.000000E+00
10	.475397E+03	.000000E+00	-.462764E-03	.000000E+00
11	.475273E+03	.000000E+00	-.339563E-03	.000000E+00
0 ELEMENT	STRESSES	PL STRAIN		
1	.283211E+04	.189093E+02	.000000E+00	
2	.141780E+05	.567233E+02	.000000E+00	
3	.368648E+05	.945230E+02	.000000E+00	
4	.708919E+05	.132312E+03	.000000E+00	
5	.116256E+06	.170111E+03	.000000E+00	
6	.116257E+06	-.170110E+03	.000000E+00	
7	.708936E+05	-.132314E+03	.000000E+00	
8	.368661E+05	-.945278E+02	.000000E+00	

9 .141787E+05 -.567245E+02 .000000E+00  
 10 .283320E+04 -.189087E+02 .000000E+00  
 0 ITERATION NUMBER= 35  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308838E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .489260E+03 .000000E+00 .328313E-03 .000000E+00  
 2 .489380E+03 .000000E+00 .455495E-03 .000000E+00  
 3 .489538E+03 .000000E+00 .534693E-03 .000000E+00  
 4 .489710E+03 .000000E+00 .517909E-03 .000000E+00  
 5 .489862E+03 .000000E+00 .357142E-03 .000000E+00  
 6 .489943E+03 .000000E+00 .439131E-05 .000000E+00  
 7 .489865E+03 .000000E+00 -.348363E-03 .000000E+00  
 8 .489715E+03 .000000E+00 -.509136E-03 .000000E+00  
 9 .489546E+03 .000000E+00 -.525924E-03 .000000E+00  
 10 .489391E+03 .000000E+00 -.446726E-03 .000000E+00  
 11 .489273E+03 .000000E+00 -.319545E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189127E+02 .000000E+00  
 2 .141780E+05 .567147E+02 .000000E+00  
 3 .368648E+05 .945167E+02 .000000E+00  
 4 .708919E+05 .132310E+03 .000000E+00  
 5 .116256E+06 .170107E+03 .000000E+00  
 6 .116257E+06 -.170108E+03 .000000E+00  
 7 .708936E+05 -.132319E+03 .000000E+00  
 8 .368661E+05 -.945232E+02 .000000E+00  
 9 .141787E+05 -.567236E+02 .000000E+00  
 10 .283320E+04 -.189078E+02 .000000E+00  
 0 ITERATION NUMBER= 36  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308592E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .503259E+03 .000000E+00 .308542E-03 .000000E+00  
 2 .503374E+03 .000000E+00 .439705E-03 .000000E+00  
 3 .503527E+03 .000000E+00 .522882E-03 .000000E+00  
 4 .503697E+03 .000000E+00 .510076E-03 .000000E+00  
 5 .503847E+03 .000000E+00 .353287E-03 .000000E+00  
 6 .503927E+03 .000000E+00 .451416E-05 .000000E+00  
 7 .503849E+03 .000000E+00 -.344263E-03 .000000E+00  
 8 .503702E+03 .000000E+00 -.501058E-03 .000000E+00  
 9 .503535E+03 .000000E+00 -.513867E-03 .000000E+00  
 10 .503385E+03 .000000E+00 -.430691E-03 .000000E+00  
 11 .503272E+03 .000000E+00 -.299528E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189067E+02 .000000E+00  
 2 .141780E+05 .567211E+02 .000000E+00  
 3 .368648E+05 .945194E+02 .000000E+00  
 4 .708919E+05 .132316E+03 .000000E+00  
 5 .116256E+06 .170113E+03 .000000E+00  
 6 .116257E+06 -.170103E+03 .000000E+00  
 7 .708936E+05 -.132321E+03 .000000E+00  
 8 .368661E+05 -.945274E+02 .000000E+00  
 9 .141787E+05 -.567255E+02 .000000E+00  
 10 .283318E+04 -.189099E+02 .000000E+00  
 0 ITERATION NUMBER= 37  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308817E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .517258E+03 .000000E+00 .288771E-03 .000000E+00  
 2 .517367E+03 .000000E+00 .423915E-03 .000000E+00  
 3 .517517E+03 .000000E+00 .511071E-03 .000000E+00  
 4 .517683E+03 .000000E+00 .502243E-03 .000000E+00  
 5 .517832E+03 .000000E+00 .349432E-03 .000000E+00

6 .517911E+03 .000000E+00 .463624E-05 .000000E+00  
 7 .517834E+03 .000000E+00 -.340163E-03 .000000E+00  
 8 .517689E+03 .000000E+00 -.492981E-03 .000000E+00  
 9 .517525E+03 .000000E+00 -.501811E-03 .000000E+00  
 10 .517379E+03 .000000E+00 -.414655E-03 .000000E+00  
 11 .517271E+03 .000000E+00 -.279512E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189144E+02 .000000E+00  
 2 .141780E+05 .567167E+02 .000000E+00  
 3 .368648E+05 .945236E+02 .000000E+00  
 4 .708919E+05 .132312E+03 .000000E+00  
 5 .116256E+06 .170108E+03 .000000E+00  
 6 .116257E+06 -.170109E+03 .000000E+00  
 7 .708936E+05 -.132317E+03 .000000E+00  
 8 .368661E+05 -.945246E+02 .000000E+00  
 9 .141787E+05 -.567203E+02 .000000E+00  
 10 .283321E+04 -.189167E+02 .000000E+00  
 0 ITERATION NUMBER= 38  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308584E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .531257E+03 .000000E+00 .269002E-03 .000000E+00  
 2 .531361E+03 .000000E+00 .408127E-03 .000000E+00  
 3 .531506E+03 .000000E+00 .499262E-03 .000000E+00  
 4 .531670E+03 .000000E+00 .494413E-03 .000000E+00  
 5 .531816E+03 .000000E+00 .345580E-03 .000000E+00  
 6 .531895E+03 .000000E+00 .476175E-05 .000000E+00  
 7 .531819E+03 .000000E+00 -.336060E-03 .000000E+00  
 8 .531676E+03 .000000E+00 -.484900E-03 .000000E+00  
 9 .531515E+03 .000000E+00 -.489752E-03 .000000E+00  
 10 .531373E+03 .000000E+00 -.398616E-03 .000000E+00  
 11 .531271E+03 .000000E+00 -.259492E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189040E+02 .000000E+00  
 2 .141780E+05 .567248E+02 .000000E+00  
 3 .368648E+05 .945279E+02 .000000E+00  
 4 .708919E+05 .132321E+03 .000000E+00  
 5 .116256E+06 .170102E+03 .000000E+00  
 6 .116257E+06 -.170109E+03 .000000E+00  
 7 .708935E+05 -.132318E+03 .000000E+00  
 8 .368660E+05 -.945231E+02 .000000E+00  
 9 .141787E+05 -.567230E+02 .000000E+00  
 10 .283319E+04 -.189074E+02 .000000E+00  
 0 ITERATION NUMBER= 39  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308783E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .545256E+03 .000000E+00 .249234E-03 .000000E+00  
 2 .545355E+03 .000000E+00 .392340E-03 .000000E+00  
 3 .545496E+03 .000000E+00 .487455E-03 .000000E+00  
 4 .545656E+03 .000000E+00 .486584E-03 .000000E+00  
 5 .545801E+03 .000000E+00 .341729E-03 .000000E+00  
 6 .545880E+03 .000000E+00 .488788E-05 .000000E+00  
 7 .545804E+03 .000000E+00 -.331956E-03 .000000E+00  
 8 .545662E+03 .000000E+00 -.476818E-03 .000000E+00  
 9 .545505E+03 .000000E+00 -.477692E-03 .000000E+00  
 10 .545367E+03 .000000E+00 -.382576E-03 .000000E+00  
 11 .545270E+03 .000000E+00 -.239472E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189101E+02 .000000E+00  
 2 .141780E+05 .567249E+02 .000000E+00  
 3 .368648E+05 .945304E+02 .000000E+00

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4 .708919E+05 .132327E+03 .000000E+00
5 .116256E+06 .170114E+03 .000000E+00
6 .116257E+06 -.170111E+03 .000000E+00
7 .708935E+05 -.132321E+03 .000000E+00
8 .368660E+05 -.945160E+02 .000000E+00
9 .141787E+05 -.567198E+02 .000000E+00
10 .283318E+04 -.189104E+02 .000000E+00
0 ITERATION NUMBER= 40
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308588E+02
0 NODE DISPL. REACTION DISPL. REACTION
 1 .559255E+03 .000000E+00 .229466E-03 .000000E+00
 2 .559348E+03 .000000E+00 .376552E-03 .000000E+00
 3 .559485E+03 .000000E+00 .475647E-03 .000000E+00
 4 .559643E+03 .000000E+00 .478754E-03 .000000E+00
 5 .559786E+03 .000000E+00 .337876E-03 .000000E+00
 6 .559864E+03 .000000E+00 .501279E-05 .000000E+00
 7 .559789E+03 .000000E+00 -.327854E-03 .000000E+00
 8 .559649E+03 .000000E+00 -.468739E-03 .000000E+00
 9 .559494E+03 .000000E+00 -.465634E-03 .000000E+00
10 .559361E+03 .000000E+00 -.366539E-03 .000000E+00
11 .559270E+03 .000000E+00 -.219454E-03 .000000E+00
0 ELEMENT STRESSES PL STRAIN
 1 .283211E+04 .189056E+02 .000000E+00
 2 .141780E+05 .567205E+02 .000000E+00
 3 .368648E+05 .945286E+02 .000000E+00
 4 .708919E+05 .132317E+03 .000000E+00
 5 .116256E+06 .170109E+03 .000000E+00
 6 .116257E+06 -.170110E+03 .000000E+00
 7 .708936E+05 -.132315E+03 .000000E+00
 8 .368661E+05 -.945293E+02 .000000E+00
 9 .141787E+05 -.567305E+02 .000000E+00
10 .283319E+04 -.189088E+02 .000000E+00
0 ITERATION NUMBER= 41
0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308708E+02
0 NODE DISPL. REACTION DISPL. REACTION
 1 .573254E+03 .000000E+00 .209698E-03 .000000E+00
 2 .573342E+03 .000000E+00 .360765E-03 .000000E+00
 3 .573475E+03 .000000E+00 .463839E-03 .000000E+00
 4 .573630E+03 .000000E+00 .470925E-03 .000000E+00
 5 .573771E+03 .000000E+00 .334025E-03 .000000E+00
 6 .573848E+03 .000000E+00 .513880E-05 .000000E+00
 7 .573774E+03 .000000E+00 -.323751E-03 .000000E+00
 8 .573636E+03 .000000E+00 -.460657E-03 .000000E+00
 9 .573484E+03 .000000E+00 -.453574E-03 .000000E+00
10 .573354E+03 .000000E+00 -.350499E-03 .000000E+00
11 .573269E+03 .000000E+00 -.199433E-03 .000000E+00
0 ELEMENT STRESSES PL STRAIN
 1 .283211E+04 .189067E+02 .000000E+00
 2 .141780E+05 .567218E+02 .000000E+00
 3 .368648E+05 .945259E+02 .000000E+00
 4 .708919E+05 .132325E+03 .000000E+00
 5 .116256E+06 .170115E+03 .000000E+00
 6 .116257E+06 -.170105E+03 .000000E+00
 7 .708936E+05 -.132318E+03 .000000E+00
 8 .368660E+05 -.945166E+02 .000000E+00
 9 .141787E+05 -.567219E+02 .000000E+00
10 .283317E+04 -.189126E+02 .000000E+00
0 ITERATION NUMBER= 42
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308644E+02
0 NODE DISPL. REACTION DISPL. REACTION

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1 .587253E+03 .000000E+00 .189932E-03 .000000E+00
2 .587336E+03 .000000E+00 .344979E-03 .000000E+00
3 .587464E+03 .000000E+00 .452033E-03 .000000E+00
4 .587616E+03 .000000E+00 .463098E-03 .000000E+00
5 .587756E+03 .000000E+00 .330175E-03 .000000E+00
6 .587832E+03 .000000E+00 .526656E-05 .000000E+00
7 .587759E+03 .000000E+00 -.319645E-03 .000000E+00
8 .587622E+03 .000000E+00 -.452574E-03 .000000E+00
9 .587474E+03 .000000E+00 -.441512E-03 .000000E+00
10 .587348E+03 .000000E+00 -.334458E-03 .000000E+00
11 .587268E+03 .000000E+00 -.179411E-03 .000000E+00

0 ELEMENT STRESSES PL STRAIN
1 .283211E+04 .189100E+02 .000000E+00
2 .141780E+05 .567190E+02 .000000E+00
3 .368648E+05 .945256E+02 .000000E+00
4 .708919E+05 .132322E+03 .000000E+00
5 .116256E+06 .170111E+03 .000000E+00
6 .116257E+06 -.170104E+03 .000000E+00
7 .708935E+05 -.132318E+03 .000000E+00
8 .368660E+05 -.945187E+02 .000000E+00
9 .141787E+05 -.567219E+02 .000000E+00
10 .283317E+04 -.189065E+02 .000000E+00

0 ITERATION NUMBER= 43
0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308650E+02
0 NODE DISPL. REACTION DISPL. REACTION
1 .601252E+03 .000000E+00 .170162E-03 .000000E+00
2 .601329E+03 .000000E+00 .329191E-03 .000000E+00
3 .601454E+03 .000000E+00 .440224E-03 .000000E+00
4 .601603E+03 .000000E+00 .455267E-03 .000000E+00
5 .601740E+03 .000000E+00 .326322E-03 .000000E+00
6 .601817E+03 .000000E+00 .539072E-05 .000000E+00
7 .601744E+03 .000000E+00 -.315544E-03 .000000E+00
8 .601609E+03 .000000E+00 -.444495E-03 .000000E+00
9 .601464E+03 .000000E+00 -.429455E-03 .000000E+00
10 .601342E+03 .000000E+00 -.318422E-03 .000000E+00
11 .601268E+03 .000000E+00 -.159393E-03 .000000E+00

0 ELEMENT STRESSES PL STRAIN
1 .283211E+04 .189069E+02 .000000E+00
2 .141780E+05 .567161E+02 .000000E+00
3 .368648E+05 .945190E+02 .000000E+00
4 .708919E+05 .132314E+03 .000000E+00
5 .116256E+06 .170108E+03 .000000E+00
6 .116257E+06 -.170107E+03 .000000E+00
7 .708936E+05 -.132322E+03 .000000E+00
8 .368661E+05 -.945251E+02 .000000E+00
9 .141787E+05 -.567257E+02 .000000E+00
10 .283319E+04 -.189041E+02 .000000E+00

0 ITERATION NUMBER= 44
0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308651E+02
0 NODE DISPL. REACTION DISPL. REACTION
1 .615251E+03 .000000E+00 .150394E-03 .000000E+00
2 .615323E+03 .000000E+00 .313404E-03 .000000E+00
3 .615443E+03 .000000E+00 .428416E-03 .000000E+00
4 .615589E+03 .000000E+00 .447437E-03 .000000E+00
5 .615725E+03 .000000E+00 .322470E-03 .000000E+00
6 .615801E+03 .000000E+00 .551669E-05 .000000E+00
7 .615728E+03 .000000E+00 -.311440E-03 .000000E+00
8 .615596E+03 .000000E+00 -.436413E-03 .000000E+00
9 .615453E+03 .000000E+00 -.417394E-03 .000000E+00
10 .615336E+03 .000000E+00 -.302382E-03 .000000E+00

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11 .615267E+03 .000000E+00 -.139372E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189079E+02 .000000E+00  
 2 .141780E+05 .567234E+02 .000000E+00  
 3 .368648E+05 .945225E+02 .000000E+00  
 4 .708919E+05 .132321E+03 .000000E+00  
 5 .116256E+06 .170114E+03 .000000E+00  
 6 .116257E+06 -.170109E+03 .000000E+00  
 7 .708935E+05 -.132319E+03 .000000E+00  
 8 .368660E+05 -.945246E+02 .000000E+00  
 9 .141787E+05 -.567169E+02 .000000E+00  
 10 .283315E+04 -.189139E+02 .000000E+00  
 0 ITERATION NUMBER= 45  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308863E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .629250E+03 .000000E+00 .130624E-03 .000000E+00  
 2 .629317E+03 .000000E+00 .297614E-03 .000000E+00  
 3 .629433E+03 .000000E+00 .416606E-03 .000000E+00  
 4 .629576E+03 .000000E+00 .439606E-03 .000000E+00  
 5 .629710E+03 .000000E+00 .318616E-03 .000000E+00  
 6 .629785E+03 .000000E+00 .563994E-05 .000000E+00  
 7 .629713E+03 .000000E+00 -.307340E-03 .000000E+00  
 8 .629582E+03 .000000E+00 -.428335E-03 .000000E+00  
 9 .629443E+03 .000000E+00 -.405338E-03 .000000E+00  
 10 .629330E+03 .000000E+00 -.286347E-03 .000000E+00  
 11 .629267E+03 .000000E+00 -.119357E-03 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189127E+02 .000000E+00  
 2 .141780E+05 .567161E+02 .000000E+00  
 3 .368648E+05 .945239E+02 .000000E+00  
 4 .708919E+05 .132314E+03 .000000E+00  
 5 .116256E+06 .170113E+03 .000000E+00  
 6 .116257E+06 -.170111E+03 .000000E+00  
 7 .708936E+05 -.132315E+03 .000000E+00  
 8 .368661E+05 -.945224E+02 .000000E+00  
 9 .141788E+05 -.567243E+02 .000000E+00  
 10 .283320E+04 -.189208E+02 .000000E+00  
 0 ITERATION NUMBER= 46  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308686E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .643249E+03 .000000E+00 .110855E-03 .000000E+00  
 2 .643310E+03 .000000E+00 .281826E-03 .000000E+00  
 3 .643422E+03 .000000E+00 .404797E-03 .000000E+00  
 4 .643562E+03 .000000E+00 .431775E-03 .000000E+00  
 5 .643695E+03 .000000E+00 .314764E-03 .000000E+00  
 6 .643769E+03 .000000E+00 .576447E-05 .000000E+00  
 7 .643698E+03 .000000E+00 -.303238E-03 .000000E+00  
 8 .643569E+03 .000000E+00 -.420256E-03 .000000E+00  
 9 .643433E+03 .000000E+00 -.393280E-03 .000000E+00  
 10 .643324E+03 .000000E+00 -.270309E-03 .000000E+00  
 11 .643266E+03 .000000E+00 -.993378E-04 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189095E+02 .000000E+00  
 2 .141780E+05 .567130E+02 .000000E+00  
 3 .368648E+05 .945293E+02 .000000E+00  
 4 .708919E+05 .132318E+03 .000000E+00  
 5 .116256E+06 .170103E+03 .000000E+00  
 6 .116257E+06 -.170109E+03 .000000E+00  
 7 .708936E+05 -.132321E+03 .000000E+00  
 8 .368661E+05 -.945304E+02 .000000E+00

9 .141787E+05 -.567240E+02 .000000E+00  
 10 .283320E+04 -.189085E+02 .000000E+00  
 0 ITERATION NUMBER= 47  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308645E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .657247E+03 .000000E+00 .910834E-04 .000000E+00  
 2 .657304E+03 .000000E+00 .266035E-03 .000000E+00  
 3 .657412E+03 .000000E+00 .392985E-03 .000000E+00  
 4 .657549E+03 .000000E+00 .423942E-03 .000000E+00  
 5 .657680E+03 .000000E+00 .310908E-03 .000000E+00  
 6 .657754E+03 .000000E+00 .588672E-05 .000000E+00  
 7 .657683E+03 .000000E+00 -.299138E-03 .000000E+00  
 8 .657556E+03 .000000E+00 -.412178E-03 .000000E+00  
 9 .657422E+03 .000000E+00 -.381224E-03 .000000E+00  
 10 .657318E+03 .000000E+00 -.254273E-03 .000000E+00  
 11 .657265E+03 .000000E+00 -.793214E-04 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189111E+02 .000000E+00  
 2 .141780E+05 .567208E+02 .000000E+00  
 3 .368648E+05 .945212E+02 .000000E+00  
 4 .708919E+05 .132320E+03 .000000E+00  
 5 .116256E+06 .170110E+03 .000000E+00  
 6 .116257E+06 -.170109E+03 .000000E+00  
 7 .708936E+05 -.132316E+03 .000000E+00  
 8 .368661E+05 -.945219E+02 .000000E+00  
 9 .141787E+05 -.567254E+02 .000000E+00  
 10 .283320E+04 -.189099E+02 .000000E+00  
 0 ITERATION NUMBER= 48  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308797E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .671246E+03 .000000E+00 .713165E-04 .000000E+00  
 2 .671298E+03 .000000E+00 .250249E-03 .000000E+00  
 3 .671401E+03 .000000E+00 .381179E-03 .000000E+00  
 4 .671536E+03 .000000E+00 .416114E-03 .000000E+00  
 5 .671664E+03 .000000E+00 .307058E-03 .000000E+00  
 6 .671738E+03 .000000E+00 .601424E-05 .000000E+00  
 7 .671668E+03 .000000E+00 -.295033E-03 .000000E+00  
 8 .671543E+03 .000000E+00 -.404095E-03 .000000E+00  
 9 .671412E+03 .000000E+00 -.369162E-03 .000000E+00  
 10 .671312E+03 .000000E+00 -.238232E-03 .000000E+00  
 11 .671265E+03 .000000E+00 -.592990E-04 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189157E+02 .000000E+00  
 2 .141780E+05 .567255E+02 .000000E+00  
 3 .368648E+05 .945220E+02 .000000E+00  
 4 .708919E+05 .132324E+03 .000000E+00  
 5 .116256E+06 .170113E+03 .000000E+00  
 6 .116257E+06 -.170101E+03 .000000E+00  
 7 .708935E+05 -.132310E+03 .000000E+00  
 8 .368660E+05 -.945244E+02 .000000E+00  
 9 .141787E+05 -.567199E+02 .000000E+00  
 10 .283319E+04 -.189107E+02 .000000E+00  
 0 ITERATION NUMBER= 49  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308843E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .685245E+03 .000000E+00 .515513E-04 .000000E+00  
 2 .685291E+03 .000000E+00 .234465E-03 .000000E+00  
 3 .685391E+03 .000000E+00 .369374E-03 .000000E+00  
 4 .685522E+03 .000000E+00 .408287E-03 .000000E+00  
 5 .685649E+03 .000000E+00 .303209E-03 .000000E+00

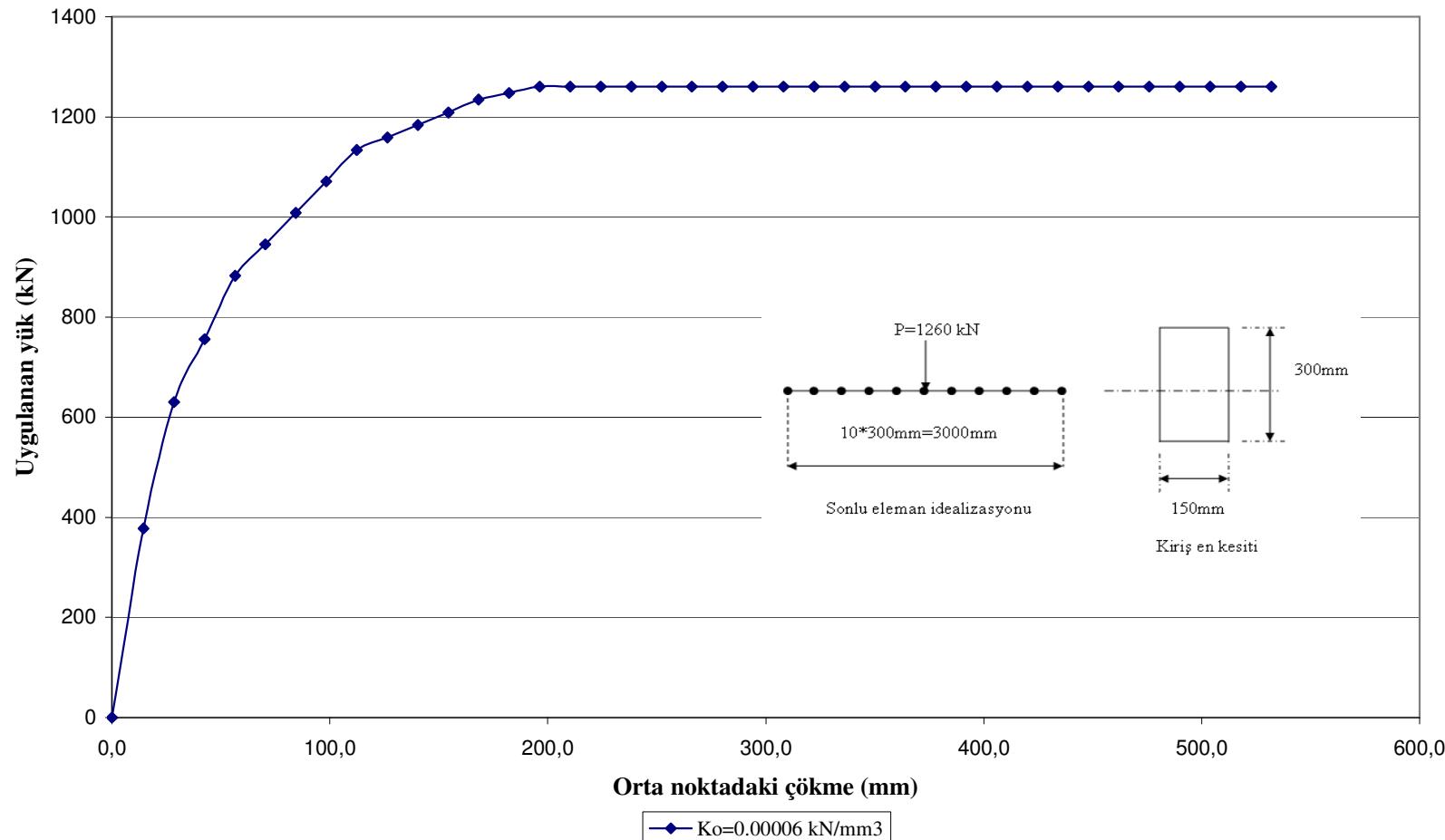
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6 .685722E+03 .000000E+00 .614260E-05 .000000E+00
7 .685653E+03 .000000E+00 -.290927E-03 .000000E+00
8 .685529E+03 .000000E+00 -.396011E-03 .000000E+00
9 .685402E+03 .000000E+00 -.357101E-03 .000000E+00
10 .685306E+03 .000000E+00 -.222190E-03 .000000E+00
11 .685264E+03 .000000E+00 -.392770E-04 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .283211E+04 .189172E+02 .000000E+00
2 .141780E+05 .567272E+02 .000000E+00
3 .368648E+05 .945200E+02 .000000E+00
4 .708919E+05 .132320E+03 .000000E+00
5 .116256E+06 .170108E+03 .000000E+00
6 .116257E+06 -.170107E+03 .000000E+00
7 .708936E+05 -.132317E+03 .000000E+00
8 .368661E+05 -.945208E+02 .000000E+00
9 .141787E+05 -.567199E+02 .000000E+00
10 .283319E+04 -.189168E+02 .000000E+00
0 ITERATION NUMBER= 50
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308792E+02
0 NODE DISPL. REACTION DISPL. REACTION
1 .699244E+03 .000000E+00 .317822E-04 .000000E+00
2 .699285E+03 .000000E+00 .218676E-03 .000000E+00
3 .699380E+03 .000000E+00 .357565E-03 .000000E+00
4 .699509E+03 .000000E+00 .400457E-03 .000000E+00
5 .699634E+03 .000000E+00 .299356E-03 .000000E+00
6 .699706E+03 .000000E+00 .626692E-05 .000000E+00
7 .699638E+03 .000000E+00 -.286826E-03 .000000E+00
8 .699516E+03 .000000E+00 -.387932E-03 .000000E+00
9 .699392E+03 .000000E+00 -.345043E-03 .000000E+00
10 .699300E+03 .000000E+00 -.206153E-03 .000000E+00
11 .699264E+03 .000000E+00 -.192590E-04 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .283211E+04 .189016E+02 .000000E+00
2 .141780E+05 .567179E+02 .000000E+00
3 .368648E+05 .945255E+02 .000000E+00
4 .708919E+05 .132312E+03 .000000E+00
5 .116256E+06 .170104E+03 .000000E+00
6 .116257E+06 -.170111E+03 .000000E+00
7 .708936E+05 -.132316E+03 .000000E+00
8 .368661E+05 -.945214E+02 .000000E+00
9 .141787E+05 -.567304E+02 .000000E+00
10 .283317E+04 -.189151E+02 .000000E+00
0 ITERATION NUMBER= 51
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308708E+02
0 NODE DISPL. REACTION DISPL. REACTION
1 .713243E+03 .000000E+00 .120107E-04 .000000E+00
2 .713279E+03 .000000E+00 .202886E-03 .000000E+00
3 .713370E+03 .000000E+00 .345753E-03 .000000E+00
4 .713495E+03 .000000E+00 .392624E-03 .000000E+00
5 .713619E+03 .000000E+00 .295501E-03 .000000E+00
6 .713691E+03 .000000E+00 .638930E-05 .000000E+00
7 .713622E+03 .000000E+00 -.282726E-03 .000000E+00
8 .713503E+03 .000000E+00 -.379855E-03 .000000E+00
9 .713381E+03 .000000E+00 -.332987E-03 .000000E+00
10 .713294E+03 .000000E+00 -.190118E-03 .000000E+00
11 .713263E+03 .000000E+00 .757291E-06 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .283211E+04 .189153E+02 .000000E+00
2 .141780E+05 .567256E+02 .000000E+00
3 .368648E+05 .945171E+02 .000000E+00

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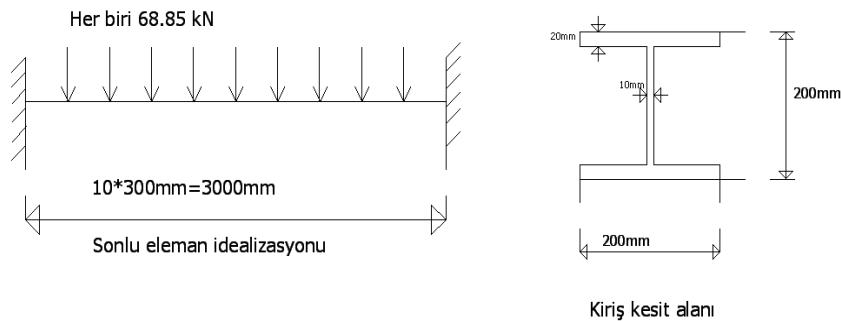
4 .708919E+05 .132319E+03 .000000E+00  
 5 .116256E+06 .170105E+03 .000000E+00  
 6 .116257E+06 -.170105E+03 .000000E+00  
 7 .708936E+05 -.132317E+03 .000000E+00  
 8 .368661E+05 -.945253E+02 .000000E+00  
 9 .141787E+05 -.567258E+02 .000000E+00  
 10 .283320E+04 -.189104E+02 .000000E+00  
 0) ITERATION NUMBER= 52  
 0) CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308821E+02  
 0) NODE DISPL. REACTION DISPL. REACTION  
 1 .727242E+03 .000000E+00 -.775882E-05 .000000E+00  
 2 .727272E+03 .000000E+00 .187097E-03 .000000E+00  
 3 .727359E+03 .000000E+00 .333944E-03 .000000E+00  
 4 .727482E+03 .000000E+00 .384793E-03 .000000E+00  
 5 .727604E+03 .000000E+00 .291648E-03 .000000E+00  
 6 .727675E+03 .000000E+00 .651357E-05 .000000E+00  
 7 .727607E+03 .000000E+00 -.278624E-03 .000000E+00  
 8 .727489E+03 .000000E+00 -.371775E-03 .000000E+00  
 9 .727371E+03 .000000E+00 -.320929E-03 .000000E+00  
 10 .727288E+03 .000000E+00 -.174080E-03 .000000E+00  
 11 .727262E+03 .000000E+00 .207757E-04 .000000E+00  
 0) ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189128E+02 .000000E+00  
 2 .141780E+05 .567171E+02 .000000E+00  
 3 .368648E+05 .945172E+02 .000000E+00  
 4 .708919E+05 .132311E+03 .000000E+00  
 5 .116256E+06 .170108E+03 .000000E+00  
 6 .116257E+06 -.170109E+03 .000000E+00  
 7 .708936E+05 -.132316E+03 .000000E+00  
 8 .368661E+05 -.945206E+02 .000000E+00  
 9 .141787E+05 -.567250E+02 .000000E+00  
 10 .283320E+04 -.189096E+02 .000000E+00  
 0) ITERATION NUMBER= 53  
 0) CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .308591E+02  
 0) NODE DISPL. REACTION DISPL. REACTION  
 1 .741241E+03 .000000E+00 -.275286E-04 .000000E+00  
 2 .741266E+03 .000000E+00 .171308E-03 .000000E+00  
 3 .741349E+03 .000000E+00 .322135E-03 .000000E+00  
 4 .741468E+03 .000000E+00 .376962E-03 .000000E+00  
 5 .741589E+03 .000000E+00 .287795E-03 .000000E+00  
 6 .741659E+03 .000000E+00 .663765E-05 .000000E+00  
 7 .741592E+03 .000000E+00 -.274523E-03 .000000E+00  
 8 .741476E+03 .000000E+00 -.363696E-03 .000000E+00  
 9 .741361E+03 .000000E+00 -.308871E-03 .000000E+00  
 10 .741282E+03 .000000E+00 -.158043E-03 .000000E+00  
 11 .741262E+03 .000000E+00 .407940E-04 .000000E+00  
 0) ELEMENT STRESSES PL STRAIN  
 1 .283211E+04 .189047E+02 .000000E+00  
 2 .141780E+05 .567214E+02 .000000E+00  
 3 .368648E+05 .945177E+02 .000000E+00  
 4 .708919E+05 .132316E+03 .000000E+00  
 5 .116256E+06 .170111E+03 .000000E+00  
 6 .116257E+06 -.170107E+03 .000000E+00  
 7 .708936E+05 -.132321E+03 .000000E+00  
 8 .368661E+05 -.945279E+02 .000000E+00  
 9 .141787E+05 -.567240E+02 .000000E+00  
 10 .283320E+04 -.189087E+02 .000000E+00

0 ITERATION NUMBER= 54  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .308620E+02  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .755240E+03 .000000E+00 -.472976E-04 .000000E+00  
   2 .755260E+03 .000000E+00 .155519E-03 .000000E+00  
   3 .755338E+03 .000000E+00 .310326E-03 .000000E+00  
   4 .755455E+03 .000000E+00 .369132E-03 .000000E+00  
   5 .755573E+03 .000000E+00 .283942E-03 .000000E+00  
   6 .755643E+03 .000000E+00 .676233E-05 .000000E+00  
   7 .755577E+03 .000000E+00 -.270420E-03 .000000E+00  
   8 .755463E+03 .000000E+00 -.355616E-03 .000000E+00  
   9 .755351E+03 .000000E+00 -.296813E-03 .000000E+00  
 10 .755276E+03 .000000E+00 -.142005E-03 .000000E+00  
 11 .755261E+03 .000000E+00 .608128E-04 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
   1 .283211E+04 .189075E+02 .000000E+00  
   2 .141780E+05 .567182E+02 .000000E+00  
   3 .368648E+05 .945292E+02 .000000E+00  
   4 .708919E+05 .132313E+03 .000000E+00  
   5 .116256E+06 .170107E+03 .000000E+00  
   6 .116257E+06 -.170106E+03 .000000E+00  
   7 .708936E+05 -.132315E+03 .000000E+00  
   8 .368661E+05 -.945240E+02 .000000E+00  
   9 .141787E+05 -.567240E+02 .000000E+00  
 10 .283320E+04 -.189087E+02 .000000E+00



**Şekil 5.4:** Elastik zemine oturan tekil yüklü tabakasız Timoshenko kirişi örneği

### 5.1.3 Uniform yayılı yüklü tabakasız Timoshenko kırışı örneği



**Sekil 5.5:** Uniform yayılı yük etkimesi hali

#### Kırışın malzeme özellikleri:

$$E \text{ (Elastisite modülü)} = 210 \text{ kN/mm}^2$$

$$\nu \text{ (Poisson oranı)} = 0.3$$

$$\sigma_0 \text{ (Akma gerilmesi)} = 0.25 \text{ kN/mm}^2$$

$$H^I \text{ (Pekleşme parametresi)} = 0.0$$

#### Kırış geometrisi:

$$b = 150\text{mm}$$

$$t = 300\text{mm}$$

$$l = 3000\text{mm}$$

Bu problemin çözümü için kayma şekil değiştirmelerini dikkate alan rijitlik matrisi kullanılmıştır.

**Probleme ait bilgilerin programa giriş listesi:**

Buradaki idealleştirme Problem 5.1.1'deki gibidir.Yükleme durumu hariç diğer tüm veriler formattı girişe uygundur.

11 10 2 1 4 2 14 2 2  
11.43808e10 516921.6 212000. 0.

1 1 2 1

2 2 3 1

3 3 4 1

4 4 5 1

5 5 6 1

6 6 7 1

7 7 8 1

8 8 9 1

9 9 10 1

10 10 11 1

1 0.

2 300.

3 600.

4 900.

5 1200.

6 1500.

7 1800.

8 2100.

9 2400.

10 2700.

11 3000.

1 1 0. 1 0.

11 1 0. 1 0.

0.0E-3 (Elastik zemin değeri=0)

<b>Eleman <u>numarası</u></b>	<b>İlk D.N.’daki <u>yük</u></b>	<b>İlk D.N’daki <u>moment</u></b>	<b>Son D.N’daki <u>yük</u></b>	<b>Son D.N’daki <u>moment</u></b>
1	68.85	0.	68.85	0.
2	68.85	0.	68.85	0.
3	68.85	0.	68.85	0.
4	68.85	0.	68.85	0.
5	68.85	0.	68.85	0.
6	68.85	0.	68.85	0.
7	68.85	0.	68.85	0.
8	68.85	0.	68.85	0.
9	68.85	0.	68.85	0.
10	68.85	0.	68.85	0.
100 2	0.30	0.5		
100 2	0.20	0.5		
100 2	0.10	0.5		
100 2	0.10	0.5		
100 2	0.05	0.5		
100 2	0.05	0.5		
100 2	0.05	0.5		
100 2	0.05	0.5		
100 2	0.02	0.5		
100 2	0.02	0.5		
100 2	0.02	0.5		
100 2	0.01	0.5		
100 2	0.01	0.5		

**Veri girişi sonrası alınan sonuçlar;**

```
NPOIN= 11 NELEM= 10 NBOUN= 2 NMATS= 1
NPROP= 4 NNODE= 2 NINCS= 14 NALGO= 2
NDOFN= 2
0 MATERIAL PROPERTIES
    1 .1438080E+11 .5169216E+06 .2120000E+06 .0000000E+00
0 EL NODES MAT.
    1 1 2 1
    2 2 3 1
    3 3 4 1
    4 4 5 1
    5 5 6 1
    6 6 7 1
    7 7 8 1
    8 8 9 1
    9 9 10 1
    10 10 11 1
0 NODE COORD.
    1     .00000
    2   300.00000
    3   600.00000
    4   900.00000
    5  1200.00000
    6  1500.00000
    7  1800.00000
    8  2100.00000
    9  2400.00000
   10  2700.00000
   11  3000.00000
0 RES.NODE CODE PRES.VALUES CODE PRES.VALUES
    1 1     .00000  1     .00000
   11 1     .00000  1     .00000
0 ELEMENT NODAL LOADS
    1   68.85000     .00000   68.85000     .00000
    2   68.85000     .00000   68.85000     .00000
    3   68.85000     .00000   68.85000     .00000
    4   68.85000     .00000   68.85000     .00000
    5   68.85000     .00000   68.85000     .00000
    6   68.85000     .00000   68.85000     .00000
    7   68.85000     .00000   68.85000     .00000
    8   68.85000     .00000   68.85000     .00000
    9   68.85000     .00000   68.85000     .00000
   10   68.85000     .00000   68.85000     .00000
ELASTIC SOIL COEFFICIENT=     .000000E+00
0 IINCS= 1 NITER= 100 NOUTP= 2 FACTO= .300000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .114560E-03
0 NODE DISPL. REACTION DISPL. REACTION
    1 .000000E+00 -.206550E+03 .000000E+00 -.102242E+06
    2 .369650E+00 .000000E+00 .155120E-02 .000000E+00
    3 .101910E+01 .000000E+00 .206826E-02 .000000E+00
    4 .167690E+01 .000000E+00 .180973E-02 .000000E+00
    5 .214913E+01 .000000E+00 .103413E-02 .000000E+00
    6 .231947E+01 .000000E+00 .112103E-08 .000000E+00
    7 .214913E+01 .000000E+00 -.103413E-02 .000000E+00
    8 .167690E+01 .000000E+00 -.180973E-02 .000000E+00
    9 .101910E+01 .000000E+00 -.206826E-02 .000000E+00
   10 .369650E+00 .000000E+00 -.155120E-02 .000000E+00
```

11 .000000E+00 -.206550E+03 .000000E+00 .102243E+06  
 0 ELEMENT STRESSES PL STRAIN  
 1 -.743582E+05 .185895E+03 .000000E+00  
 2 -.247861E+05 .144585E+03 .000000E+00  
 3 .123930E+05 .103275E+03 .000000E+00  
 4 .371790E+05 .619652E+02 .000000E+00  
 5 .495721E+05 .206549E+02 .000000E+00  
 6 .495722E+05 -.206550E+02 .000000E+00  
 7 .371791E+05 -.619651E+02 .000000E+00  
 8 .123930E+05 -.103275E+03 .000000E+00  
 9 -.247861E+05 -.144585E+03 .000000E+00  
 10 -.743582E+05 -.185895E+03 .000000E+00  
 0 IINCS= 2 NITER= 100 NOUTP= 2 FACTO= .200000E+00 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .380970E-04  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.344250E+03 .000000E+00 -.170404E+06  
 2 .616083E+00 .000000E+00 .258532E-02 .000000E+00  
 3 .169850E+01 .000000E+00 .344710E-02 .000000E+00  
 4 .279482E+01 .000000E+00 .301621E-02 .000000E+00  
 5 .358188E+01 .000000E+00 .172355E-02 .000000E+00  
 6 .386578E+01 .000000E+00 .741700E-09 .000000E+00  
 7 .358188E+01 .000000E+00 -.172355E-02 .000000E+00  
 8 .279482E+01 .000000E+00 -.301621E-02 .000000E+00  
 9 .169850E+01 .000000E+00 -.344710E-02 .000000E+00  
 10 .616083E+00 .000000E+00 -.258533E-02 .000000E+00  
 11 .000000E+00 -.344250E+03 .000000E+00 .170404E+06  
 0 ELEMENT STRESSES PL STRAIN  
 1 -.123930E+06 .309825E+03 .000000E+00  
 2 -.413101E+05 .240975E+03 .000000E+00  
 3 .206549E+05 .172125E+03 .000000E+00  
 4 .619650E+05 .103275E+03 .000000E+00  
 5 .826200E+05 .344251E+02 .000000E+00  
 6 .826201E+05 -.344249E+02 .000000E+00  
 7 .619650E+05 -.103275E+03 .000000E+00  
 8 .206550E+05 -.172125E+03 .000000E+00  
 9 -.413101E+05 -.240975E+03 .000000E+00  
 10 -.123930E+06 -.309825E+03 .000000E+00  
 0 IINCS= 3 NITER= 100 NOUTP= 2 FACTO= .100000E+00 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .144935E-04  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.413100E+03 .000000E+00 -.204485E+06  
 2 .739300E+00 .000000E+00 .310239E-02 .000000E+00  
 3 .203820E+01 .000000E+00 .413652E-02 .000000E+00  
 4 .335379E+01 .000000E+00 .361945E-02 .000000E+00  
 5 .429826E+01 .000000E+00 .206826E-02 .000000E+00  
 6 .463893E+01 .000000E+00 .241158E-09 .000000E+00  
 7 .429826E+01 .000000E+00 -.206826E-02 .000000E+00  
 8 .335379E+01 .000000E+00 -.361945E-02 .000000E+00  
 9 .203820E+01 .000000E+00 -.413652E-02 .000000E+00  
 10 .739300E+00 .000000E+00 -.310239E-02 .000000E+00  
 11 .000000E+00 -.413100E+03 .000000E+00 .204485E+06  
 0 ELEMENT STRESSES PL STRAIN  
 1 -.148716E+06 .371790E+03 .000000E+00  
 2 -.495721E+05 .289170E+03 .000000E+00  
 3 .247859E+05 .206550E+03 .000000E+00  
 4 .743580E+05 .123930E+03 .000000E+00  
 5 .991440E+05 .413101E+02 .000000E+00

```

6 .991440E+05 -.413100E+02 .000000E+00
7 .743580E+05 -.123930E+03 .000000E+00
8 .247860E+05 -.206550E+03 .000000E+00
9 -.495721E+05 -.289170E+03 .000000E+00
10 -.148716E+06 -.371790E+03 .000000E+00

0 IINCS= 4 NITER= 100 NOUTP= 2 FACTO= .100000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .147003E-04
0 NODE DISPL. REACTION DISPL. REACTION
 1 .000000E+00 -.481950E+03 .000000E+00 -.238565E+06
 2 .862516E+00 .000000E+00 .361945E-02 .000000E+00
 3 .237790E+01 .000000E+00 .482594E-02 .000000E+00
 4 .391275E+01 .000000E+00 .422270E-02 .000000E+00
 5 .501463E+01 .000000E+00 .241297E-02 .000000E+00
 6 .541209E+01 .000000E+00 .288634E-09 .000000E+00
 7 .501463E+01 .000000E+00 -.241297E-02 .000000E+00
 8 .391275E+01 .000000E+00 -.422270E-02 .000000E+00
 9 .237790E+01 .000000E+00 -.482594E-02 .000000E+00
10 .862516E+00 .000000E+00 -.361945E-02 .000000E+00
11 .000000E+00 -.481950E+03 .000000E+00 .238565E+06

0 ELEMENT STRESSES PL STRAIN
 1 -.173502E+06 .433755E+03 .000000E+00
 2 -.578341E+05 .337365E+03 .000000E+00
 3 .289169E+05 .240975E+03 .000000E+00
 4 .867509E+05 .144585E+03 .000000E+00
 5 .115668E+06 .481951E+02 .000000E+00
 6 .115668E+06 -.481950E+02 .000000E+00
 7 .867510E+05 -.144585E+03 .000000E+00
 8 .289169E+05 -.240975E+03 .000000E+00
 9 -.578341E+05 -.337365E+03 .000000E+00
10 -.173502E+06 -.433755E+03 .000000E+00

0 IINCS= 5 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .871332E-05
0 NODE DISPL. REACTION DISPL. REACTION
 1 .000000E+00 -.516375E+03 .000000E+00 -.255606E+06
 2 .924124E+00 .000000E+00 .387798E-02 .000000E+00
 3 .254775E+01 .000000E+00 .517065E-02 .000000E+00
 4 .419223E+01 .000000E+00 .452432E-02 .000000E+00
 5 .537282E+01 .000000E+00 .258532E-02 .000000E+00
 6 .579867E+01 .000000E+00 .152198E-09 .000000E+00
 7 .537282E+01 .000000E+00 -.258532E-02 .000000E+00
 8 .419223E+01 .000000E+00 -.452432E-02 .000000E+00
 9 .254775E+01 .000000E+00 -.517065E-02 .000000E+00
10 .924124E+00 .000000E+00 -.387798E-02 .000000E+00
11 .000000E+00 -.516375E+03 .000000E+00 .255606E+06

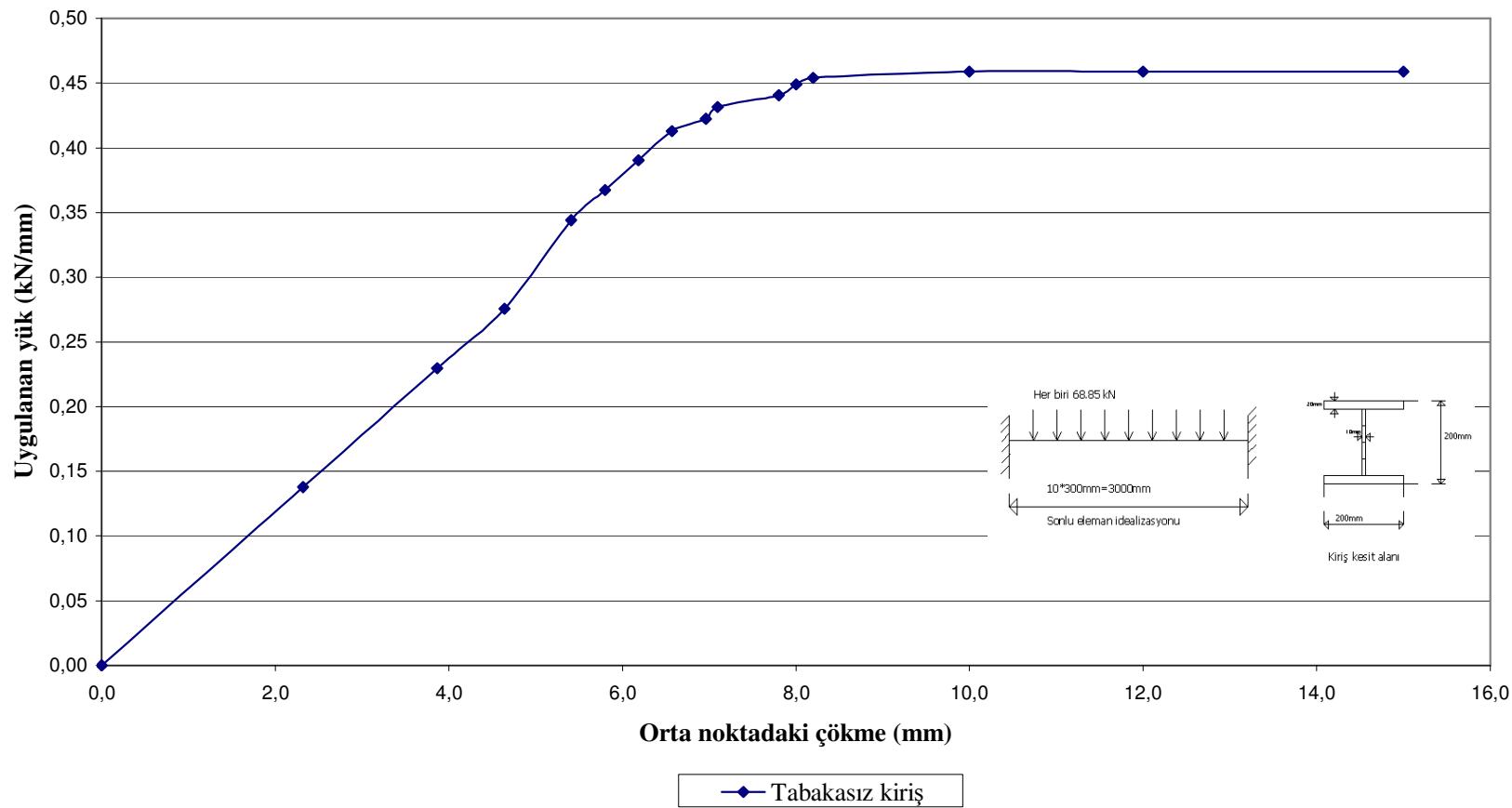
0 ELEMENT STRESSES PL STRAIN
 1 -.185895E+06 .464738E+03 .000000E+00
 2 -.619651E+05 .361463E+03 .000000E+00
 3 .309824E+05 .258188E+03 .000000E+00
 4 .929474E+05 .154913E+03 .000000E+00
 5 .123930E+06 .516376E+02 .000000E+00
 6 .123930E+06 -.516375E+02 .000000E+00
 7 .929475E+05 -.154913E+03 .000000E+00
 8 .309824E+05 -.258188E+03 .000000E+00
 9 -.619651E+05 -.361463E+03 .000000E+00
10 -.185895E+06 -.464738E+03 .000000E+00

0 IINCS= 6 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .612585E-05

```

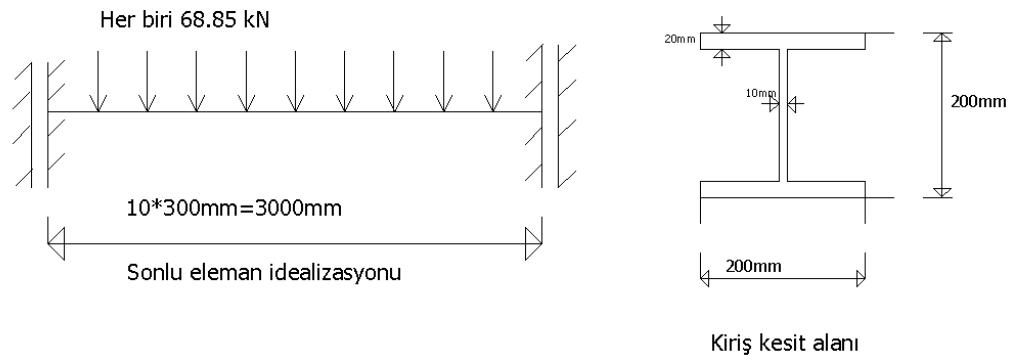
	NODE	DISPL.	REACTION	DISPL.	REACTION
0	1	.000000E+00	-.550800E+03	.000000E+00	-.272646E+06
	2	.985733E+00	.000000E+00	.413652E-02	.000000E+00
	3	.271760E+01	.000000E+00	.551536E-02	.000000E+00
	4	.447171E+01	.000000E+00	.482594E-02	.000000E+00
	5	.573101E+01	.000000E+00	.275768E-02	.000000E+00
	6	.618524E+01	.000000E+00	.195499E-09	.000000E+00
	7	.573101E+01	.000000E+00	-.275768E-02	.000000E+00
	8	.447171E+01	.000000E+00	-.482594E-02	.000000E+00
	9	.271760E+01	.000000E+00	-.551536E-02	.000000E+00
	10	.985733E+00	.000000E+00	-.413652E-02	.000000E+00
	11	.000000E+00	-.550800E+03	.000000E+00	.272646E+06
0	ELEMENT	STRESSES	PL STRAIN		
	1	-.198288E+06	.495720E+03	.000000E+00	
	2	-.660961E+05	.385560E+03	.000000E+00	
	3	.330479E+05	.275400E+03	.000000E+00	
	4	.991439E+05	.165240E+03	.000000E+00	
	5	.132192E+06	.550800E+02	.000000E+00	
	6	.132192E+06	-.550800E+02	.000000E+00	
	7	.991439E+05	-.165240E+03	.000000E+00	
	8	.330479E+05	-.275400E+03	.000000E+00	
	9	-.660961E+05	-.385560E+03	.000000E+00	
	10	-.198288E+06	-.495720E+03	.000000E+00	
0	IINCS= 7	NITER= 100	NOUTP= 2	FACTO= .500000E-01	TOLER= .500000E+00
0	ITERATION NUMBER= 1				
0	CONVERGENCE CODE= 0	NORM OF RESIDUAL SUM RATIO= .636509E-05			
0	NODE	DISPL.	REACTION	DISPL.	REACTION
	1	.000000E+00	-.585225E+03	.000000E+00	-.289687E+06
	2	.104734E+01	.000000E+00	.439505E-02	.000000E+00
	3	.288745E+01	.000000E+00	.586007E-02	.000000E+00
	4	.475120E+01	.000000E+00	.512756E-02	.000000E+00
	5	.608920E+01	.000000E+00	.293003E-02	.000000E+00
	6	.657182E+01	.000000E+00	-.126934E-10	.000000E+00
	7	.608920E+01	.000000E+00	-.293003E-02	.000000E+00
	8	.475120E+01	.000000E+00	-.512756E-02	.000000E+00
	9	.288745E+01	.000000E+00	-.586007E-02	.000000E+00
	10	.104734E+01	.000000E+00	-.439505E-02	.000000E+00
	11	.000000E+00	-.585225E+03	.000000E+00	.289686E+06
0	ELEMENT	STRESSES	PL STRAIN		
	1	-.210681E+06	.526703E+03	.000000E+00	
	2	-.702271E+05	.409658E+03	.000000E+00	
	3	.351134E+05	.292613E+03	.000000E+00	
	4	.105340E+06	.175568E+03	.000000E+00	
	5	.140454E+06	.585225E+02	.000000E+00	
	6	.140454E+06	-.585225E+02	.000000E+00	
	7	.105340E+06	-.175567E+03	.000000E+00	
	8	.351134E+05	-.292613E+03	.000000E+00	
	9	-.702271E+05	-.409658E+03	.000000E+00	
	10	-.210681E+06	-.526702E+03	.000000E+00	
0	IINCS= 8	NITER= 100	NOUTP= 2	FACTO= .500000E-01	TOLER= .500000E+00
0	ITERATION NUMBER= 1				
0	CONVERGENCE CODE= 1	NORM OF RESIDUAL SUM RATIO= .510589E+01			
0	NODE	DISPL.	REACTION	DISPL.	REACTION
	1	.000000E+00	-.619650E+03	.000000E+00	-.306727E+06
	2	.110895E+01	.000000E+00	.465358E-02	.000000E+00
	3	.305730E+01	.000000E+00	.620478E-02	.000000E+00
	4	.503068E+01	.000000E+00	.542918E-02	.000000E+00
	5	.644739E+01	.000000E+00	.310239E-02	.000000E+00
	6	.695840E+01	.000000E+00	.715151E-10	.000000E+00
	7	.644739E+01	.000000E+00	-.310239E-02	.000000E+00

8	.503068E+01	.000000E+00	-.542918E-02	.000000E+00
9	.305730E+01	.000000E+00	-.620478E-02	.000000E+00
10	.110895E+01	.000000E+00	-.465358E-02	.000000E+00
11	.000000E+00	-.619650E+03	.000000E+00	.306727E+06
0	ELEMENT	STRESSES	PL STRAIN	
1	-.212000E+06	.557685E+03	-.770063E-06	
2	-.743581E+05	.433755E+03	.000000E+00	
3	.371789E+05	.309825E+03	.000000E+00	
4	.111537E+06	.185895E+03	.000000E+00	
5	.148716E+06	.619650E+02	.000000E+00	
6	.148716E+06	-.619650E+02	.000000E+00	
7	.111537E+06	-.185895E+03	.000000E+00	
8	.371789E+05	-.309825E+03	.000000E+00	
9	-.743581E+05	-.433755E+03	.000000E+00	
10	-.212000E+06	-.557685E+03	-.770062E-06	



**Şekil 5.6:** Uniform yayılı yüklü tabakasız Timoshenko kırışı örneği

#### 5.1.4 Elastik zemine oturan uniform yayılı yüklü Timoshenko kırışı örneği



**Şekil 5.7:** Uniform yayılı yük etkimesi hali

Elastik zemin etkilerini daha iyi gözlemlenmesi için ankastre mesnetler çökmeye serbest bırakılmıştır. Hesapta kayma şekil değiştirmelerini içeren sistem rijitlik matrisi kullanılmıştır.

Zemin yatak katsayıısı  $6000\text{t}/\text{m}^3$ 'tür. Verilerde elastik zemin değeri  $0.0\text{E}-3$  yerine  $12.0\text{E}-3$  alınır. İlgili data satırlarındaki değişiklik aşağıda gösterilmiştir.

Düğüm noktası <u>numarası</u>	Mesnetlenme <u>durumu</u>	Moment çökme <u>değeri</u>	Dönme <u>değeri</u>	Dışarıdan <u>verilmiş dönme</u>
1(ilk)	0(serbest)	0.	1.	0.
11(son)	0(serbest)	0.	1.	0.

8	68.85	0.	68.85	0.
9	68.85	0.	68.85	0.
10	68.85	0.	68.85	0.

#### 12.0E-3

100	2	0.30	0.5
100	2	0.20	0.5
100	2	0.01	0.5

**Veri girişi sonrası alınan sonuçlar;**

```
NPOIN= 11 NELEM= 10 NBOUN= 2 NMATS= 1
NPROP= 4 NNODE= 2 NINCS= 14 NALGO= 2
NDOFN= 2
0 MATERIAL PROPERTIES
 1 .1438080E+11 .5169216E+06 .2120000E+06 .1000000E+00
0 EL NODES MAT.
 1 1 2 1
 2 2 3 1
 3 3 4 1
 4 4 5 1
 5 5 6 1
 6 6 7 1
 7 7 8 1
 8 8 9 1
 9 9 10 1
10 10 11 1
0 NODE COORD.
 1   .00000
 2 300.00000
 3 600.00000
 4 900.00000
 5 1200.00000
 6 1500.00000
 7 1800.00000
 8 2100.00000
 9 2400.00000
10 2700.00000
11 3000.00000
0 RES.NODE CODE PRES.VALUES CODE PRES.VALUES
 1 0   .00000 1   .00000
11 0   .00000 1   .00000
0 ELEMENT NODAL LOADS
 1 68.85000   .00000 68.85000   .00000
 2 68.85000   .00000 68.85000   .00000
 3 68.85000   .00000 68.85000   .00000
 4 68.85000   .00000 68.85000   .00000
 5 68.85000   .00000 68.85000   .00000
 6 68.85000   .00000 68.85000   .00000
 7 68.85000   .00000 68.85000   .00000
 8 68.85000   .00000 68.85000   .00000
 9 68.85000   .00000 68.85000   .00000
10 68.85000   .00000 68.85000   .00000
ELASTIC SOIL COEFFICIENT= .120000E-01
0 IINCS= 1 NITER= 100 NOUTP= 2 FACTO= .300000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .870388E+01
0 NODE DISPL. REACTION DISPL. REACTION
 1 .114685E+02   .000000E+00   .000000E+00   .103197E+04
 2 .114685E+02   .000000E+00   .220105E-08   .000000E+00
 3 .114685E+02   .000000E+00  -.173750E-09   .000000E+00
 4 .114685E+02   .000000E+00  -.913881E-08   .000000E+00
 5 .114684E+02   .000000E+00  -.166174E-07   .000000E+00
 6 .114684E+02   .000000E+00  -.215181E-07   .000000E+00
 7 .114684E+02   .000000E+00  -.221003E-07   .000000E+00
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8 .114684E+02    .000000E+00 -.166932E-07    .000000E+00
9 .114684E+02    .000000E+00 -.884009E-08    .000000E+00
10 .114684E+02   .000000E+00 -.310441E-08    .000000E+00
11 .114684E+02   .000000E+00 .000000E+00    -.103210E+04
0 ELEMENT      STRESSES      PL STRAIN
1 .102706E+04  -.448227E-03 .000000E+00
2 .102727E+04   .882149E-03 .000000E+00
3 .102759E+04   .600815E-03 .000000E+00
4 .102752E+04   .648499E-04 .000000E+00
5 .102740E+04  -.381470E-05 .000000E+00
6 .102719E+04  -.147724E-02 .000000E+00
7 .102690E+04   .129700E-03 .000000E+00
8 .102678E+04  -.127506E-02 .000000E+00
9 .102688E+04  -.158310E-03 .000000E+00
10 .102701E+04   .632286E-03 .000000E+00
0 ITERATION NUMBER= 2
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .437467E+01
0 NODE  DISPL.      REACTION      DISPL.      REACTION
1 .229369E+02   .000000E+00 .000000E+00   .205923E+04
2 .229369E+02   .000000E+00 .157937E-09   .000000E+00
3 .229369E+02   .000000E+00 -.411525E-08   .000000E+00
4 .229369E+02   .000000E+00 -.146539E-07   .000000E+00
5 .229369E+02   .000000E+00 -.231541E-07   .000000E+00
6 .229369E+02   .000000E+00 -.285291E-07   .000000E+00
7 .229369E+02   .000000E+00 -.291365E-07   .000000E+00
8 .229369E+02   .000000E+00 -.226566E-07   .000000E+00
9 .229369E+02   .000000E+00 -.135627E-07   .000000E+00
10 .229369E+02  .000000E+00 -.557963E-08   .000000E+00
11 .229369E+02  .000000E+00 .000000E+00   -.205912E+04
0 ELEMENT      STRESSES      PL STRAIN
1 .205431E+04  -.324249E-04 .000000E+00
2 .205453E+04  -.489235E-03 .000000E+00
3 .205483E+04  -.629425E-04 .000000E+00
4 .205473E+04  -.715256E-04 .000000E+00
5 .205458E+04   .164986E-03 .000000E+00
6 .205435E+04   .877380E-04 .000000E+00
7 .205401E+04  -.110817E-02 .000000E+00
8 .205388E+04  -.394821E-03 .000000E+00
9 .205393E+04  -.128174E-02 .000000E+00
10 .205405E+04   .113583E-02 .000000E+00
0 ITERATION NUMBER= 3
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .292046E+01
0 NODE  DISPL.      REACTION      DISPL.      REACTION
1 .344053E+02   .000000E+00 .000000E+00   .308642E+04
2 .344053E+02   .000000E+00 -.514861E-09   .000000E+00
3 .344053E+02   .000000E+00 -.535709E-08   .000000E+00
4 .344053E+02   .000000E+00 -.162124E-07   .000000E+00
5 .344053E+02   .000000E+00 -.248831E-07   .000000E+00
6 .344053E+02   .000000E+00 -.302327E-07   .000000E+00
7 .344053E+02   .000000E+00 -.305214E-07   .000000E+00
8 .344053E+02   .000000E+00 -.238264E-07   .000000E+00
9 .344053E+02   .000000E+00 -.140224E-07   .000000E+00
10 .344053E+02  .000000E+00 -.587083E-08   .000000E+00
11 .344053E+02  .000000E+00 .000000E+00   -.308627E+04
0 ELEMENT      STRESSES      PL STRAIN
1 .308151E+04   .103951E-03 .000000E+00
2 .308171E+04  -.991821E-04 .000000E+00
3 .308200E+04   .507355E-03 .000000E+00
4 .308190E+04   .597954E-03 .000000E+00
5 .308174E+04   .864029E-03 .000000E+00

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6	.308149E+04	-.577927E-03	.000000E+00
7	.308116E+04	-.588417E-03	.000000E+00
8	.308101E+04	-.135803E-02	.000000E+00
9	.308109E+04	.165939E-03	.000000E+00
10	.308120E+04	-.100136E-03	.000000E+00
0	ITERATION NUMBER= 4		
0	CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .219159E+01		
0	NODE	DISPL.	REACTION
1	.458738E+02	.000000E+00	.000000E+00
2	.458738E+02	.000000E+00	-.594657E-09
3	.458738E+02	.000000E+00	-.552959E-08
4	.458738E+02	.000000E+00	-.165555E-07
5	.458738E+02	.000000E+00	-.253204E-07
6	.458738E+02	.000000E+00	-.306714E-07
7	.458738E+02	.000000E+00	-.309786E-07
8	.458737E+02	.000000E+00	-.243348E-07
9	.458737E+02	.000000E+00	-.144840E-07
10	.458737E+02	.000000E+00	-.616495E-08
11	.458737E+02	.000000E+00	.000000E+00
11	.458737E+02	.000000E+00	-.411342E+04
0	ELEMENT	STRESSES	PL STRAIN
1	.410867E+04	.120163E-03	.000000E+00
2	.410888E+04	.124741E-02	.000000E+00
3	.410917E+04	.612259E-03	.000000E+00
4	.410906E+04	-.537872E-03	.000000E+00
5	.410890E+04	-.251770E-03	.000000E+00
6	.410865E+04	-.395775E-03	.000000E+00
7	.410832E+04	-.391006E-03	.000000E+00
8	.410817E+04	-.116062E-02	.000000E+00
9	.410824E+04	.319481E-03	.000000E+00
10	.410834E+04	-.400543E-04	.000000E+00
0	ITERATION NUMBER= 5		
0	CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .175385E+01		
0	NODE	DISPL.	REACTION
1	.573422E+02	.000000E+00	.000000E+00
2	.573422E+02	.000000E+00	-.785289E-09
3	.573422E+02	.000000E+00	-.590257E-08
4	.573422E+02	.000000E+00	-.170577E-07
5	.573422E+02	.000000E+00	-.259646E-07
6	.573422E+02	.000000E+00	-.313950E-07
7	.573422E+02	.000000E+00	-.316661E-07
8	.573422E+02	.000000E+00	-.248362E-07
9	.573422E+02	.000000E+00	-.149351E-07
10	.573422E+02	.000000E+00	-.645616E-08
11	.573422E+02	.000000E+00	.000000E+00
11	.573422E+02	.000000E+00	-.514057E+04
0	ELEMENT	STRESSES	PL STRAIN
1	.513584E+04	.159264E-03	.000000E+00
2	.513605E+04	.667572E-04	.000000E+00
3	.513634E+04	.790596E-03	.000000E+00
4	.513623E+04	-.304222E-03	.000000E+00
5	.513606E+04	.267029E-04	.000000E+00
6	.513581E+04	-.108719E-03	.000000E+00
7	.513547E+04	-.149727E-03	.000000E+00
8	.513532E+04	-.967026E-03	.000000E+00
9	.513539E+04	-.824928E-03	.000000E+00
10	.513549E+04	.190735E-04	.000000E+00
0	ITERATION NUMBER= 6		
0	CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .146183E+01		
0	NODE	DISPL.	REACTION
1	.688107E+02	.000000E+00	.000000E+00
2	.688107E+02	.000000E+00	-.109372E-08
2	.688107E+02	.000000E+00	.000000E+00

	STRESSES	PL STRAIN
3	.688107E+02	.000000E+00 -.649106E-08
4	.688107E+02	.000000E+00 -.178776E-07
5	.688107E+02	.000000E+00 -.269558E-07
6	.688106E+02	.000000E+00 -.324418E-07
7	.688106E+02	.000000E+00 -.325471E-07
8	.688106E+02	.000000E+00 -.254232E-07
9	.688106E+02	.000000E+00 -.152425E-07
10	.688106E+02	.000000E+00 -.652691E-08
11	.688106E+02	.000000E+00 .000000E+00
0	ELEMENT	STRESSES PL STRAIN
1	.616301E+04	.222206E-03 .000000E+00
2	.616322E+04	.154400E-02 .000000E+00
3	.616351E+04	.107765E-02 .000000E+00
4	.616340E+04	.648499E-04 .000000E+00
5	.616322E+04	.441551E-03 .000000E+00
6	.616296E+04	-.101089E-02 .000000E+00
7	.616262E+04	.148773E-03 .000000E+00
8	.616247E+04	-.784874E-03 .000000E+00
9	.616254E+04	.546455E-03 .000000E+00
10	.616264E+04	.333786E-04 .000000E+00
0	ITERATION NUMBER=	7
0	CONVERGENCE CODE=	1 NORM OF RESIDUAL SUM RATIO= .125317E+01
0	NODE	DISPL. REACTION DISPL. REACTION
1	.802791E+02	.000000E+00 .000000E+00
2	.802791E+02	.000000E+00 -.698274E-09
3	.802791E+02	.000000E+00 -.572686E-08
4	.802791E+02	.000000E+00 -.168139E-07
5	.802791E+02	.000000E+00 -.256671E-07
6	.802791E+02	.000000E+00 -.311599E-07
7	.802791E+02	.000000E+00 -.314843E-07
8	.802791E+02	.000000E+00 -.247539E-07
9	.802791E+02	.000000E+00 -.149693E-07
10	.802791E+02	.000000E+00 -.638014E-08
11	.802791E+02	.000000E+00 .000000E+00
0	ELEMENT	STRESSES PL STRAIN
1	.719015E+04	.141144E-03 .000000E+00
2	.719036E+04	.130844E-02 .000000E+00
3	.719065E+04	.705719E-03 .000000E+00
4	.719054E+04	-.413895E-03 .000000E+00
5	.719038E+04	-.820160E-04 .000000E+00
6	.719013E+04	-.148869E-02 .000000E+00
7	.718979E+04	-.149918E-02 .000000E+00
8	.718965E+04	-.976563E-03 .000000E+00
9	.718970E+04	.461578E-03 .000000E+00
10	.718981E+04	.381470E-05 .000000E+00
0	ITERATION NUMBER=	8
0	CONVERGENCE CODE=	1 NORM OF RESIDUAL SUM RATIO= .109664E+01
0	NODE	DISPL. REACTION DISPL. REACTION
1	.917475E+02	.000000E+00 .000000E+00
2	.917475E+02	.000000E+00 -.927704E-09
3	.917475E+02	.000000E+00 -.617686E-08
4	.917475E+02	.000000E+00 -.174216E-07
5	.917475E+02	.000000E+00 -.264433E-07
6	.917475E+02	.000000E+00 -.319107E-07
7	.917475E+02	.000000E+00 -.321646E-07
8	.917475E+02	.000000E+00 -.252451E-07
9	.917475E+02	.000000E+00 -.150635E-07
10	.917475E+02	.000000E+00 -.645382E-08
11	.917475E+02	.000000E+00 .000000E+00
0	ELEMENT	STRESSES PL STRAIN

1 .821732E+04 .187874E-03 .000000E+00  
 2 .821753E+04 .152588E-03 .000000E+00  
 3 .821782E+04 .920296E-03 .000000E+00  
 4 .821771E+04 -.132561E-03 .000000E+00  
 5 .821754E+04 .228882E-03 .000000E+00  
 6 .821729E+04 -.119781E-02 .000000E+00  
 7 .821695E+04 .343323E-04 .000000E+00  
 8 .821679E+04 -.857353E-03 .000000E+00  
 9 .821686E+04 .494957E-03 .000000E+00  
 10 .821697E+04 .181198E-04 .000000E+00  
 0 ITERATION NUMBER= 9  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .974871E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .103216E+03 .000000E+00 .000000E+00 .924940E+04  
 2 .103216E+03 .000000E+00 -.870899E-09 .000000E+00  
 3 .103216E+03 .000000E+00 -.607351E-08 .000000E+00  
 4 .103216E+03 .000000E+00 -.172885E-07 .000000E+00  
 5 .103216E+03 .000000E+00 -.262949E-07 .000000E+00  
 6 .103216E+03 .000000E+00 -.318646E-07 .000000E+00  
 7 .103216E+03 .000000E+00 -.321572E-07 .000000E+00  
 8 .103216E+03 .000000E+00 -.254216E-07 .000000E+00  
 9 .103216E+03 .000000E+00 -.153709E-07 .000000E+00  
 10 .103216E+03 .000000E+00 -.652458E-08 .000000E+00  
 11 .103216E+03 .000000E+00 .000000E+00 -.924920E+04  
 0 ELEMENT STRESSES PL STRAIN  
 1 .924448E+04 .176430E-03 .000000E+00  
 2 .924469E+04 .120163E-03 .000000E+00  
 3 .924498E+04 .871658E-03 .000000E+00  
 4 .924487E+04 -.189781E-03 .000000E+00  
 5 .924471E+04 .189781E-03 .000000E+00  
 6 .924445E+04 -.120831E-02 .000000E+00  
 7 .924411E+04 -.122643E-02 .000000E+00  
 8 .924395E+04 -.759125E-03 .000000E+00  
 9 .924401E+04 -.721931E-03 .000000E+00  
 10 .924412E+04 .324249E-04 .000000E+00  
 0 ITERATION NUMBER= 10  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .877441E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .114684E+03 .000000E+00 .000000E+00 .102766E+05  
 2 .114684E+03 .000000E+00 -.108366E-08 .000000E+00  
 3 .114684E+03 .000000E+00 -.646953E-08 .000000E+00  
 4 .114684E+03 .000000E+00 -.177724E-07 .000000E+00  
 5 .114684E+03 .000000E+00 -.267319E-07 .000000E+00  
 6 .114684E+03 .000000E+00 -.321484E-07 .000000E+00  
 7 .114684E+03 .000000E+00 -.323526E-07 .000000E+00  
 8 .114684E+03 .000000E+00 -.255517E-07 .000000E+00  
 9 .114684E+03 .000000E+00 -.156089E-07 .000000E+00  
 10 .114684E+03 .000000E+00 -.681870E-08 .000000E+00  
 11 .114684E+03 .000000E+00 .000000E+00 -.102764E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .102717E+05 .219345E-03 .000000E+00  
 2 .102719E+05 .153923E-02 .000000E+00  
 3 .102721E+05 .105095E-02 .000000E+00  
 4 .102720E+05 -.190735E-05 .000000E+00  
 5 .102719E+05 .336647E-03 .000000E+00  
 6 .102716E+05 -.111008E-02 .000000E+00  
 7 .102713E+05 .135422E-03 .000000E+00  
 8 .102711E+05 -.683784E-03 .000000E+00  
 9 .102712E+05 -.614166E-03 .000000E+00  
 10 .102713E+05 .925064E-04 .000000E+00

0 ITERATION NUMBER= 11  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .797710E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .126153E+03 .000000E+00 .000000E+00 .113037E+05  
   2 .126153E+03 .000000E+00 -.748009E-09 .000000E+00  
   3 .126153E+03 .000000E+00 -.588695E-08 .000000E+00  
   4 .126153E+03 .000000E+00 -.170281E-07 .000000E+00  
   5 .126153E+03 .000000E+00 -.258914E-07 .000000E+00  
   6 .126153E+03 .000000E+00 -.313166E-07 .000000E+00  
   7 .126153E+03 .000000E+00 -.315826E-07 .000000E+00  
   8 .126153E+03 .000000E+00 -.246263E-07 .000000E+00  
   9 .126153E+03 .000000E+00 -.146113E-07 .000000E+00  
 10 .126153E+03 .000000E+00 -.623396E-08 .000000E+00  
 11 .126153E+03 .000000E+00 .000000E+00 -.113035E+05  
 0 ELEMENT STRESSES PL STRAIN  
   1 .112988E+05 .151634E-03 .000000E+00  
   2 .112990E+05 .135231E-02 .000000E+00  
   3 .112993E+05 .781059E-03 .000000E+00  
   4 .112992E+05 -.325203E-03 .000000E+00  
   5 .112990E+05 -.381470E-05 .000000E+00  
   6 .112988E+05 -.143623E-02 .000000E+00  
   7 .112984E+05 -.150490E-02 .000000E+00  
   8 .112983E+05 -.107574E-02 .000000E+00  
   9 .112984E+05 .358582E-03 .000000E+00  
 10 .112985E+05 -.267029E-04 .000000E+00  
 0 ITERATION NUMBER= 12  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .731262E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .137621E+03 .000000E+00 .000000E+00 .123309E+05  
   2 .137621E+03 .000000E+00 -.102279E-08 .000000E+00  
   3 .137621E+03 .000000E+00 -.638731E-08 .000000E+00  
   4 .137621E+03 .000000E+00 -.177130E-07 .000000E+00  
   5 .137621E+03 .000000E+00 -.267759E-07 .000000E+00  
   6 .137621E+03 .000000E+00 -.323834E-07 .000000E+00  
   7 .137621E+03 .000000E+00 -.325367E-07 .000000E+00  
   8 .137621E+03 .000000E+00 -.255131E-07 .000000E+00  
   9 .137621E+03 .000000E+00 -.152966E-07 .000000E+00  
 10 .137621E+03 .000000E+00 -.652808E-08 .000000E+00  
 11 .137621E+03 .000000E+00 .000000E+00 -.123307E+05  
 0 ELEMENT STRESSES PL STRAIN  
   1 .123260E+05 .207901E-03 .000000E+00  
   2 .123262E+05 .215530E-03 .000000E+00  
   3 .123265E+05 .102234E-02 .000000E+00  
   4 .123264E+05 -.572205E-05 .000000E+00  
   5 .123262E+05 .393867E-03 .000000E+00  
   6 .123259E+05 -.102520E-02 .000000E+00  
   7 .123256E+05 .164032E-03 .000000E+00  
   8 .123254E+05 -.756264E-03 .000000E+00  
   9 .123255E+05 .557899E-03 .000000E+00  
 10 .123256E+05 .333786E-04 .000000E+00  
 0 ITERATION NUMBER= 13  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .675031E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .149090E+03 .000000E+00 .000000E+00 .133580E+05  
   2 .149090E+03 .000000E+00 -.870586E-09 .000000E+00  
   3 .149090E+03 .000000E+00 -.611350E-08 .000000E+00  
   4 .149090E+03 .000000E+00 -.173597E-07 .000000E+00  
   5 .149090E+03 .000000E+00 -.264013E-07 .000000E+00  
   6 .149090E+03 .000000E+00 -.320260E-07 .000000E+00  
   7 .149090E+03 .000000E+00 -.324305E-07 .000000E+00

	STRESSES	PL STRAIN		
8	.149090E+03 .000000E+00 -.255469E-07	.000000E+00		
9	.149090E+03 .000000E+00 -.153908E-07	.000000E+00		
10	.149090E+03 .000000E+00 -.660176E-08	.000000E+00		
11	.149090E+03 .000000E+00 .000000E+00	-.133578E+05		
0 ELEMENT	STRESSES	PL STRAIN		
1	.133531E+05 .176430E-03 .000000E+00			
2	.133533E+05 .142384E-02 .000000E+00			
3	.133536E+05 -.400543E-03 .000000E+00			
4	.133535E+05 -.153542E-03 .000000E+00			
5	.133533E+05 .244141E-03 .000000E+00			
6	.133531E+05 -.111961E-02 .000000E+00			
7	.133527E+05 -.114536E-02 .000000E+00			
8	.133526E+05 -.730515E-03 .000000E+00			
9	.133527E+05 .591278E-03 .000000E+00			
10	.133528E+05 .476837E-04 .000000E+00			
0 ITERATION NUMBER= 14				
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .626836E+00				
0 NODE	DISPL.	REACTION	DISPL.	REACTION
1	.160558E+03 .000000E+00 .000000E+00		.143852E+05	
2	.160558E+03 .000000E+00 -.109239E-08		.000000E+00	
3	.160558E+03 .000000E+00 -.652875E-08		.000000E+00	
4	.160558E+03 .000000E+00 -.179802E-07		.000000E+00	
5	.160558E+03 .000000E+00 -.270461E-07		.000000E+00	
6	.160558E+03 .000000E+00 -.324290E-07		.000000E+00	
7	.160558E+03 .000000E+00 -.324558E-07		.000000E+00	
8	.160558E+03 .000000E+00 -.254312E-07		.000000E+00	
9	.160558E+03 .000000E+00 -.152614E-07		.000000E+00	
10	.160558E+03 .000000E+00 -.667544E-08		.000000E+00	
11	.160558E+03 .000000E+00 .000000E+00		-.143850E+05	
0 ELEMENT	STRESSES	PL STRAIN		
1	.143803E+05 .221252E-03 .000000E+00			
2	.143805E+05 .258446E-03 .000000E+00			
3	.143808E+05 .110435E-02 .000000E+00			
4	.143807E+05 -.119114E-02 .000000E+00			
5	.143805E+05 -.837326E-03 .000000E+00			
6	.143802E+05 -.103283E-02 .000000E+00			
7	.143799E+05 .130653E-03 .000000E+00			
8	.143797E+05 -.781059E-03 .000000E+00			
9	.143798E+05 .580788E-03 .000000E+00			
10	.143799E+05 .619888E-04 .000000E+00			
0 ITERATION NUMBER= 15				
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .585061E+00				
0 NODE	DISPL.	REACTION	DISPL.	REACTION
1	.172027E+03 .000000E+00 .000000E+00		.154124E+05	
2	.172027E+03 .000000E+00 -.843453E-09		.000000E+00	
3	.172027E+03 .000000E+00 -.608078E-08		.000000E+00	
4	.172027E+03 .000000E+00 -.173600E-07		.000000E+00	
5	.172027E+03 .000000E+00 -.263798E-07		.000000E+00	
6	.172027E+03 .000000E+00 -.318369E-07		.000000E+00	
7	.172027E+03 .000000E+00 -.320212E-07		.000000E+00	
8	.172027E+03 .000000E+00 -.249905E-07		.000000E+00	
9	.172027E+03 .000000E+00 -.149882E-07		.000000E+00	
10	.172027E+03 .000000E+00 -.652867E-08		.000000E+00	
11	.172027E+03 .000000E+00 .000000E+00		-.154122E+05	
0 ELEMENT	STRESSES	PL STRAIN		
1	.154074E+05 .170708E-03 .000000E+00			
2	.154076E+05 .141144E-02 .000000E+00			
3	.154079E+05 -.408173E-03 .000000E+00			
4	.154078E+05 -.145340E-02 .000000E+00			
5	.154077E+05 -.109386E-02 .000000E+00			

6 .154074E+05 -.124168E-02 .000000E+00  
 7 .154071E+05 -.134182E-02 .000000E+00  
 8 .154069E+05 -.926971E-03 .000000E+00  
 9 .154070E+05 .495911E-03 .000000E+00  
 10 .154071E+05 .324249E-04 .000000E+00  
 0 ITERATION NUMBER= 16  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .548509E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .183495E+03 .000000E+00 .000000E+00 .164395E+05  
 2 .183495E+03 .000000E+00 -.129151E-08 .000000E+00  
 3 .183495E+03 .000000E+00 -.688677E-08 .000000E+00  
 4 .183495E+03 .000000E+00 -.183775E-07 .000000E+00  
 5 .183495E+03 .000000E+00 -.273839E-07 .000000E+00  
 6 .183495E+03 .000000E+00 -.327344E-07 .000000E+00  
 7 .183495E+03 .000000E+00 -.327385E-07 .000000E+00  
 8 .183495E+03 .000000E+00 -.255351E-07 .000000E+00  
 9 .183495E+03 .000000E+00 -.151622E-07 .000000E+00  
 10 .183495E+03 .000000E+00 -.638190E-08 .000000E+00  
 11 .183495E+03 .000000E+00 .000000E+00 -.164393E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .164346E+05 .262260E-03 .000000E+00  
 2 .164348E+05 .371933E-03 .000000E+00  
 3 .164351E+05 .125790E-02 .000000E+00  
 4 .164350E+05 -.104237E-02 .000000E+00  
 5 .164348E+05 .588417E-03 .000000E+00  
 6 .164346E+05 -.912666E-03 .000000E+00  
 7 .164342E+05 .209808E-03 .000000E+00  
 8 .164341E+05 -.781059E-03 .000000E+00  
 9 .164341E+05 .500679E-03 .000000E+00  
 10 .164342E+05 .286102E-05 .000000E+00  
 0 ITERATION NUMBER= 17  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .516253E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .194964E+03 .000000E+00 .000000E+00 .174667E+05  
 2 .194964E+03 .000000E+00 -.803796E-09 .000000E+00  
 3 .194964E+03 .000000E+00 -.604019E-08 .000000E+00  
 4 .194964E+03 .000000E+00 -.173108E-07 .000000E+00  
 5 .194964E+03 .000000E+00 -.263393E-07 .000000E+00  
 6 .194964E+03 .000000E+00 -.317885E-07 .000000E+00  
 7 .194963E+03 .000000E+00 -.319773E-07 .000000E+00  
 8 .194963E+03 .000000E+00 -.249621E-07 .000000E+00  
 9 .194963E+03 .000000E+00 -.150328E-07 .000000E+00  
 10 .194963E+03 .000000E+00 -.645558E-08 .000000E+00  
 11 .194963E+03 .000000E+00 .000000E+00 -.174665E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .174618E+05 .163078E-03 .000000E+00  
 2 .174620E+05 .100136E-03 .000000E+00  
 3 .174623E+05 -.426292E-03 .000000E+00  
 4 .174621E+05 -.147247E-02 .000000E+00  
 5 .174620E+05 .183105E-03 .000000E+00  
 6 .174617E+05 -.126076E-02 .000000E+00  
 7 .174614E+05 -.135612E-02 .000000E+00  
 8 .174612E+05 -.923157E-03 .000000E+00  
 9 .174613E+05 .490189E-03 .000000E+00  
 10 .174614E+05 .171661E-04 .000000E+00  
 0 ITERATION NUMBER= 18  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .487579E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .206432E+03 .000000E+00 .000000E+00 .184939E+05  
 2 .206432E+03 .000000E+00 -.118948E-08 .000000E+00

3	.206432E+03	.000000E+00	-.678514E-08	.000000E+00
4	.206432E+03	.000000E+00	-.183955E-07	.000000E+00
5	.206432E+03	.000000E+00	-.276516E-07	.000000E+00
6	.206432E+03	.000000E+00	-.332648E-07	.000000E+00
7	.206432E+03	.000000E+00	-.335495E-07	.000000E+00
8	.206432E+03	.000000E+00	-.264024E-07	.000000E+00
9	.206432E+03	.000000E+00	-.158619E-07	.000000E+00
10	.206432E+03	.000000E+00	-.697015E-08	.000000E+00
11	.206432E+03	.000000E+00	.000000E+00	-.184936E+05
0	ELEMENT	STRESSES	PL STRAIN	
1	.184889E+05	.242233E-03	.000000E+00	
2	.184891E+05	.329971E-03	.000000E+00	
3	.184894E+05	.124073E-02	.000000E+00	
4	.184893E+05	-.985146E-03	.000000E+00	
5	.184891E+05	-.543594E-03	.000000E+00	
6	.184889E+05	-.639915E-03	.000000E+00	
7	.184885E+05	-.742912E-03	.000000E+00	
8	.184884E+05	-.460625E-03	.000000E+00	
9	.184884E+05	.763893E-03	.000000E+00	
10	.184885E+05	.121117E-03	.000000E+00	
0	IINCS= 2	NITER= 100	NOUTP= 2	FACTO= .200000E+00
0	TOLER= .500000E+00			
0	ITERATION NUMBER= 1			
0	CONVERGENCE CODE= 1	NORM OF RESIDUAL SUM RATIO=	.743641E+00	
0	NODE	DISPL.	REACTION	DISPL.
1	.225546E+03	.000000E+00	.000000E+00	.202090E+05
2	.225546E+03	.000000E+00	.414710E-09	.000000E+00
3	.225546E+03	.000000E+00	-.659645E-08	.000000E+00
4	.225546E+03	.000000E+00	-.239561E-07	.000000E+00
5	.225546E+03	.000000E+00	-.378516E-07	.000000E+00
6	.225546E+03	.000000E+00	-.466150E-07	.000000E+00
7	.225546E+03	.000000E+00	-.473447E-07	.000000E+00
8	.225546E+03	.000000E+00	-.367590E-07	.000000E+00
9	.225546E+03	.000000E+00	-.214978E-07	.000000E+00
10	.225546E+03	.000000E+00	-.867546E-08	.000000E+00
11	.225546E+03	.000000E+00	.000000E+00	-.202088E+05
0	ELEMENT	STRESSES	PL STRAIN	
1	.202008E+05	-.839233E-04	.000000E+00	
2	.202011E+05	-.343323E-04	.000000E+00	
3	.202016E+05	-.254631E-03	.000000E+00	
4	.202015E+05	-.295544E-02	.000000E+00	
5	.202012E+05	.166321E-02	.000000E+00	
6	.202008E+05	-.292778E-03	.000000E+00	
7	.202003E+05	-.100422E-02	.000000E+00	
8	.202001E+05	-.238514E-02	.000000E+00	
9	.202002E+05	-.330925E-03	.000000E+00	
10	.202004E+05	.468254E-03	.000000E+00	
0	ITERATION NUMBER= 2			
0	CONVERGENCE CODE= 1	NORM OF RESIDUAL SUM RATIO=	.685563E+00	
0	NODE	DISPL.	REACTION	DISPL.
1	.244660E+03	.000000E+00	.000000E+00	.219210E+05
2	.244660E+03	.000000E+00	-.873477E-09	.000000E+00
3	.244660E+03	.000000E+00	-.898687E-08	.000000E+00
4	.244660E+03	.000000E+00	-.271243E-07	.000000E+00
5	.244660E+03	.000000E+00	-.414850E-07	.000000E+00
6	.244660E+03	.000000E+00	-.503082E-07	.000000E+00
7	.244660E+03	.000000E+00	-.509066E-07	.000000E+00
8	.244660E+03	.000000E+00	-.399942E-07	.000000E+00
9	.244660E+03	.000000E+00	-.237995E-07	.000000E+00
10	.244660E+03	.000000E+00	-.996326E-08	.000000E+00
11	.244660E+03	.000000E+00	.000000E+00	-.219207E+05

0 ELEMENT STRESSES PL STRAIN  
 1 .219128E+05 .179291E-03 .000000E+00  
 2 .219131E+05 .713348E-03 .000000E+00  
 3 .219136E+05 .878334E-03 .000000E+00  
 4 .219134E+05 -.157070E-02 .000000E+00  
 5 .219132E+05 .566483E-03 .000000E+00  
 6 .219128E+05 -.140476E-02 .000000E+00  
 7 .219122E+05 .380516E-03 .000000E+00  
 8 .219120E+05 -.125790E-02 .000000E+00  
 9 .219121E+05 .399590E-03 .000000E+00  
 10 .219123E+05 .729561E-03 .000000E+00  
 0 ITERATION NUMBER= 3  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .635902E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .263774E+03 .000000E+00 .000000E+00 .236330E+05  
 2 .263774E+03 .000000E+00 -.166870E-08 .000000E+00  
 3 .263774E+03 .000000E+00 -.105040E-07 .000000E+00  
 4 .263774E+03 .000000E+00 -.293152E-07 .000000E+00  
 5 .263774E+03 .000000E+00 -.443444E-07 .000000E+00  
 6 .263774E+03 .000000E+00 -.533195E-07 .000000E+00  
 7 .263774E+03 .000000E+00 -.537613E-07 .000000E+00  
 8 .263774E+03 .000000E+00 -.421584E-07 .000000E+00  
 9 .263774E+03 .000000E+00 -.253244E-07 .000000E+00  
 10 .263774E+03 .000000E+00 -.107985E-07 .000000E+00  
 11 .263774E+03 .000000E+00 .000000E+00 -.236326E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .236248E+05 .341415E-03 .000000E+00  
 2 .236251E+05 .118446E-02 .000000E+00  
 3 .236256E+05 .163364E-02 .000000E+00  
 4 .236254E+05 -.542641E-03 .000000E+00  
 5 .236251E+05 -.827789E-03 .000000E+00  
 6 .236247E+05 -.210762E-03 .000000E+00  
 7 .236241E+05 -.118732E-02 .000000E+00  
 8 .236239E+05 -.508308E-03 .000000E+00  
 9 .236240E+05 .880241E-03 .000000E+00  
 10 .236242E+05 .899315E-03 .000000E+00  
 0 ITERATION NUMBER= 4  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .592952E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .282888E+03 .000000E+00 .000000E+00 .253449E+05  
 2 .282888E+03 .000000E+00 -.151777E-08 .000000E+00  
 3 .282888E+03 .000000E+00 -.102424E-07 .000000E+00  
 4 .282888E+03 .000000E+00 -.289695E-07 .000000E+00  
 5 .282888E+03 .000000E+00 -.438419E-07 .000000E+00  
 6 .282888E+03 .000000E+00 -.526548E-07 .000000E+00  
 7 .282888E+03 .000000E+00 -.530005E-07 .000000E+00  
 8 .282888E+03 .000000E+00 -.413792E-07 .000000E+00  
 9 .282888E+03 .000000E+00 -.249744E-07 .000000E+00  
 10 .282888E+03 .000000E+00 -.107636E-07 .000000E+00  
 11 .282888E+03 .000000E+00 .000000E+00 -.253445E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .253367E+05 .310898E-03 .000000E+00  
 2 .253370E+05 .110054E-02 .000000E+00  
 3 .253375E+05 .150967E-02 .000000E+00  
 4 .253373E+05 -.714302E-03 .000000E+00  
 5 .253370E+05 -.106430E-02 .000000E+00  
 6 .253366E+05 -.500679E-03 .000000E+00  
 7 .253360E+05 -.150013E-02 .000000E+00  
 8 .253358E+05 -.737190E-03 .000000E+00  
 9 .253359E+05 -.178814E-02 .000000E+00

10 .253361E+05 .891685E-03 .000000E+00  
 0 ITERATION NUMBER= 5  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .555434E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .302002E+03 .000000E+00 .000000E+00 .270568E+05  
 2 .302002E+03 .000000E+00 -.120299E-08 .000000E+00  
 3 .302002E+03 .000000E+00 -.965115E-08 .000000E+00  
 4 .302002E+03 .000000E+00 -.282009E-07 .000000E+00  
 5 .302002E+03 .000000E+00 -.430769E-07 .000000E+00  
 6 .302002E+03 .000000E+00 -.519626E-07 .000000E+00  
 7 .302002E+03 .000000E+00 -.525380E-07 .000000E+00  
 8 .302002E+03 .000000E+00 -.413706E-07 .000000E+00  
 9 .302002E+03 .000000E+00 -.250927E-07 .000000E+00  
 10 .302002E+03 .000000E+00 -.107346E-07 .000000E+00  
 11 .302002E+03 .000000E+00 .000000E+00 -.270565E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .270486E+05 .246048E-03 .000000E+00  
 2 .270489E+05 .915527E-03 .000000E+00  
 3 .270494E+05 .123310E-02 .000000E+00  
 4 .270493E+05 -.102711E-02 .000000E+00  
 5 .270490E+05 -.136185E-02 .000000E+00  
 6 .270486E+05 -.735283E-03 .000000E+00  
 7 .270480E+05 -.159550E-02 .000000E+00  
 8 .270478E+05 -.714302E-03 .000000E+00  
 9 .270478E+05 -.176907E-02 .000000E+00  
 10 .270480E+05 .885963E-03 .000000E+00  
 0 ITERATION NUMBER= 6  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .522384E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .321116E+03 .000000E+00 .000000E+00 .287687E+05  
 2 .321116E+03 .000000E+00 -.137860E-08 .000000E+00  
 3 .321116E+03 .000000E+00 -.996473E-08 .000000E+00  
 4 .321116E+03 .000000E+00 -.286545E-07 .000000E+00  
 5 .321116E+03 .000000E+00 -.435306E-07 .000000E+00  
 6 .321116E+03 .000000E+00 -.522802E-07 .000000E+00  
 7 .321116E+03 .000000E+00 -.524779E-07 .000000E+00  
 8 .321116E+03 .000000E+00 -.405850E-07 .000000E+00  
 9 .321116E+03 .000000E+00 -.240498E-07 .000000E+00  
 10 .321116E+03 .000000E+00 -.102705E-07 .000000E+00  
 11 .321116E+03 .000000E+00 .000000E+00 -.287684E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .287605E+05 .282288E-03 .000000E+00  
 2 .287609E+05 .101471E-02 .000000E+00  
 3 .287614E+05 .138950E-02 .000000E+00  
 4 .287612E+05 -.842094E-03 .000000E+00  
 5 .287609E+05 -.120544E-02 .000000E+00  
 6 .287605E+05 -.681877E-03 .000000E+00  
 7 .287599E+05 -.176716E-02 .000000E+00  
 8 .287597E+05 -.108624E-02 .000000E+00  
 9 .287598E+05 .514030E-03 .000000E+00  
 10 .287600E+05 .790596E-03 .000000E+00  
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 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .493045E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .340230E+03 .000000E+00 .000000E+00 .304807E+05  
 2 .340230E+03 .000000E+00 -.128259E-08 .000000E+00  
 3 .340230E+03 .000000E+00 -.977270E-08 .000000E+00  
 4 .340230E+03 .000000E+00 -.283333E-07 .000000E+00  
 5 .340230E+03 .000000E+00 -.430625E-07 .000000E+00  
 6 .340230E+03 .000000E+00 -.519967E-07 .000000E+00

7 .340230E+03 .000000E+00 -.522505E-07 .000000E+00  
 8 .340230E+03 .000000E+00 -.405764E-07 .000000E+00  
 9 .340230E+03 .000000E+00 -.241681E-07 .000000E+00  
 10 .340230E+03 .000000E+00 -.102414E-07 .000000E+00  
 11 .340230E+03 .000000E+00 .000000E+00 -.304804E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .304725E+05 .263214E-03 .000000E+00  
 2 .304728E+05 .955582E-03 .000000E+00  
 3 .304733E+05 .128460E-02 .000000E+00  
 4 .304731E+05 -.100231E-02 .000000E+00  
 5 .304728E+05 -.135803E-02 .000000E+00  
 6 .304724E+05 -.784874E-03 .000000E+00  
 7 .304718E+05 -.181484E-02 .000000E+00  
 8 .304716E+05 -.106335E-02 .000000E+00  
 9 .304717E+05 .533104E-03 .000000E+00  
 10 .304719E+05 .784874E-03 .000000E+00  
 0 IINCS= 3 NITER= 100 NOUTP= 2 FACTO= .100000E+00 TOLER= .500000E+00  
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 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .554298E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .363167E+03 .000000E+00 .000000E+00 .325366E+05  
 2 .363167E+03 .000000E+00 -.720775E-09 .000000E+00  
 3 .363167E+03 .000000E+00 -.101769E-07 .000000E+00  
 4 .363167E+03 .000000E+00 -.318791E-07 .000000E+00  
 5 .363167E+03 .000000E+00 -.492414E-07 .000000E+00  
 6 .363167E+03 .000000E+00 -.598670E-07 .000000E+00  
 7 .363167E+03 .000000E+00 -.604107E-07 .000000E+00  
 8 .363167E+03 .000000E+00 -.470656E-07 .000000E+00  
 9 .363167E+03 .000000E+00 -.280815E-07 .000000E+00  
 10 .363167E+03 .000000E+00 -.121173E-07 .000000E+00  
 11 .363167E+03 .000000E+00 .000000E+00 -.325363E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .325268E+05 .148773E-03 .000000E+00  
 2 .325272E+05 .923157E-03 .000000E+00  
 3 .325278E+05 .208759E-02 .000000E+00  
 4 .325276E+05 -.161266E-02 .000000E+00  
 5 .325272E+05 -.108719E-02 .000000E+00  
 6 .325268E+05 -.109673E-03 .000000E+00  
 7 .325261E+05 -.142193E-02 .000000E+00  
 8 .325258E+05 -.153446E-02 .000000E+00  
 9 .325260E+05 -.876427E-03 .000000E+00  
 10 .325261E+05 -.142193E-02 .000000E+00  
 0 ITERATION NUMBER= 2  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .521346E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .386104E+03 .000000E+00 .000000E+00 .345910E+05  
 2 .386104E+03 .000000E+00 -.186528E-08 .000000E+00  
 3 .386104E+03 .000000E+00 -.124583E-07 .000000E+00  
 4 .386104E+03 .000000E+00 -.352364E-07 .000000E+00  
 5 .386104E+03 .000000E+00 -.535010E-07 .000000E+00  
 6 .386104E+03 .000000E+00 -.647613E-07 .000000E+00  
 7 .386104E+03 .000000E+00 -.657545E-07 .000000E+00  
 8 .386104E+03 .000000E+00 -.522020E-07 .000000E+00  
 9 .386104E+03 .000000E+00 -.320235E-07 .000000E+00  
 10 .386104E+03 .000000E+00 -.140107E-07 .000000E+00  
 11 .386104E+03 .000000E+00 .000000E+00 -.345905E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .345811E+05 .383377E-03 .000000E+00  
 2 .345816E+05 .161934E-02 .000000E+00  
 3 .345821E+05 .323391E-02 .000000E+00

4 .345819E+05 -.619888E-04 .000000E+00  
 5 .345816E+05 -.181198E-02 .000000E+00  
 6 .345811E+05 -.615120E-03 .000000E+00  
 7 .345804E+05 -.187778E-02 .000000E+00  
 8 .345801E+05 -.227642E-02 .000000E+00  
 9 .345802E+05 .311852E-03 .000000E+00  
 10 .345804E+05 .155354E-02 .000000E+00  
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 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .409041E+03 .000000E+00 .000000E+00 .366453E+05  
 2 .409041E+03 .000000E+00 -.221239E-08 .000000E+00  
 3 .409041E+03 .000000E+00 -.130926E-07 .000000E+00  
 4 .409041E+03 .000000E+00 -.359375E-07 .000000E+00  
 5 .409041E+03 .000000E+00 -.542992E-07 .000000E+00  
 6 .409041E+03 .000000E+00 -.655587E-07 .000000E+00  
 7 .409041E+03 .000000E+00 -.660397E-07 .000000E+00  
 8 .409041E+03 .000000E+00 -.519210E-07 .000000E+00  
 9 .409041E+03 .000000E+00 -.311476E-07 .000000E+00  
 10 .409041E+03 .000000E+00 -.132646E-07 .000000E+00  
 11 .409041E+03 .000000E+00 .000000E+00 -.366449E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .366355E+05 .453949E-03 .000000E+00  
 2 .366359E+05 .181961E-02 .000000E+00  
 3 .366365E+05 .916481E-03 .000000E+00  
 4 .366362E+05 .243187E-03 .000000E+00  
 5 .366359E+05 .110245E-02 .000000E+00  
 6 .366354E+05 -.298405E-02 .000000E+00  
 7 .366347E+05 -.187588E-02 .000000E+00  
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 9 .366345E+05 -.181198E-04 .000000E+00  
 10 .366347E+05 .140095E-02 .000000E+00  
 0 IINCS= 4 NITER= 100 NOUTP= 2 FACTO= .100000E+00 TOLER= .500000E+00  
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 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .538871E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .435801E+03 .000000E+00 .000000E+00 .390436E+05  
 2 .435801E+03 .000000E+00 -.184406E-08 .000000E+00  
 3 .435801E+03 .000000E+00 -.137758E-07 .000000E+00  
 4 .435801E+03 .000000E+00 -.397242E-07 .000000E+00  
 5 .435801E+03 .000000E+00 -.602523E-07 .000000E+00  
 6 .435801E+03 .000000E+00 -.725305E-07 .000000E+00  
 7 .435801E+03 .000000E+00 -.728637E-07 .000000E+00  
 8 .435801E+03 .000000E+00 -.562906E-07 .000000E+00  
 9 .435801E+03 .000000E+00 -.333569E-07 .000000E+00  
 10 .435801E+03 .000000E+00 -.139941E-07 .000000E+00  
 11 .435801E+03 .000000E+00 .000000E+00 -.390432E+05  
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 1 .390322E+05 .377655E-03 .000000E+00  
 2 .390326E+05 .447273E-02 .000000E+00  
 3 .390333E+05 .182629E-02 .000000E+00  
 4 .390331E+05 -.295353E-02 .000000E+00  
 5 .390327E+05 .114441E-02 .000000E+00  
 6 .390321E+05 -.174522E-03 .000000E+00  
 7 .390313E+05 -.218678E-02 .000000E+00  
 8 .390310E+05 -.117016E-02 .000000E+00  
 9 .390311E+05 .578880E-03 .000000E+00  
 10 .390314E+05 .154972E-02 .000000E+00  
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 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .507706E+00

0 NODE DISPL. REACTION DISPL. REACTION  
 1 .462561E+03 .000000E+00 .000000E+00 .414404E+05  
 2 .462561E+03 .000000E+00 -.236147E-08 .000000E+00  
 3 .462561E+03 .000000E+00 -.148060E-07 .000000E+00  
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 0 ELEMENT STRESSES PL STRAIN  
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 2 .414294E+05 .219727E-02 .000000E+00  
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 5 .414294E+05 -.648499E-03 .000000E+00  
 6 .414288E+05 .771523E-03 .000000E+00  
 7 .414280E+05 -.106716E-02 .000000E+00  
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 9 .414278E+05 .123310E-02 .000000E+00  
 10 .414280E+05 .178814E-02 .000000E+00  
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 1 .489320E+03 .000000E+00 .000000E+00 .438371E+05  
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 1 .438256E+05 .511169E-03 .000000E+00  
 2 .438261E+05 .225830E-02 .000000E+00  
 3 .438268E+05 .239468E-02 .000000E+00  
 4 .438265E+05 .420570E-03 .000000E+00  
 5 .438261E+05 -.392914E-03 .000000E+00  
 6 .438255E+05 -.415516E-02 .000000E+00  
 7 .438247E+05 -.937462E-03 .000000E+00  
 8 .438243E+05 -.266361E-02 .000000E+00  
 9 .438245E+05 .132275E-02 .000000E+00  
 10 .438247E+05 -.742912E-03 .000000E+00  
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 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .517991E+03 .000000E+00 .000000E+00 .464057E+05  
 2 .517991E+03 .000000E+00 -.150016E-08 .000000E+00  
 3 .517991E+03 .000000E+00 -.138032E-07 .000000E+00  
 4 .517991E+03 .000000E+00 -.412807E-07 .000000E+00  
 5 .517991E+03 .000000E+00 -.634064E-07 .000000E+00  
 6 .517991E+03 .000000E+00 -.767419E-07 .000000E+00  
 7 .517991E+03 .000000E+00 -.770674E-07 .000000E+00  
 8 .517991E+03 .000000E+00 -.599900E-07 .000000E+00

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9 .517991E+03 .000000E+00 -.358032E-07 .000000E+00
10 .517991E+03 .000000E+00 -.151864E-07 .000000E+00
11 .517991E+03 .000000E+00 .000000E+00 -.464053E+05
0 ELEMENT STRESSES PL STRAIN
1 .463935E+05 -.228119E-02 .000000E+00
2 .463940E+05 .181770E-02 .000000E+00
3 .463947E+05 .214863E-02 .000000E+00
4 .463944E+05 -.199413E-02 .000000E+00
5 .463940E+05 .534058E-04 .000000E+00
6 .463934E+05 -.364017E-02 .000000E+00
7 .463926E+05 -.578880E-03 .000000E+00
8 .463922E+05 -.250912E-02 .000000E+00
9 .463924E+05 -.127125E-02 .000000E+00
10 .463926E+05 -.796318E-03 .000000E+00
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2 .548574E+03 .000000E+00 -.173059E-08 .000000E+00
3 .548574E+03 .000000E+00 -.149329E-07 .000000E+00
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10 .548574E+03 .000000E+00 -.165508E-07 .000000E+00
11 .548574E+03 .000000E+00 .000000E+00 -.491452E+05
0 ELEMENT STRESSES PL STRAIN
1 .491326E+05 -.223351E-02 .000000E+00
2 .491331E+05 .209427E-02 .000000E+00
3 .491339E+05 .386238E-03 .000000E+00
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5 .491331E+05 -.617981E-03 .000000E+00
6 .491325E+05 .104046E-02 .000000E+00
7 .491316E+05 .136852E-02 .000000E+00
8 .491312E+05 -.108433E-02 .000000E+00
9 .491314E+05 -.456810E-03 .000000E+00
10 .491317E+05 -.519753E-03 .000000E+00
0 IINCS= 7 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .490776E+00
0 NODE DISPL. REACTION DISPL. REACTION
1 .581068E+03 .000000E+00 .000000E+00 .520568E+05
2 .581068E+03 .000000E+00 -.248667E-08 .000000E+00
3 .581068E+03 .000000E+00 -.170415E-07 .000000E+00
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5 .581068E+03 .000000E+00 -.733522E-07 .000000E+00
6 .581068E+03 .000000E+00 -.879133E-07 .000000E+00
7 .581068E+03 .000000E+00 -.876518E-07 .000000E+00
8 .581068E+03 .000000E+00 -.682234E-07 .000000E+00
9 .581068E+03 .000000E+00 -.405830E-07 .000000E+00
10 .581068E+03 .000000E+00 -.173186E-07 .000000E+00
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0 ELEMENT STRESSES PL STRAIN
1 .520429E+05 -.207901E-02 .000000E+00
2 .520435E+05 .267792E-02 .000000E+00
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4 .520440E+05 .149441E-02 .000000E+00

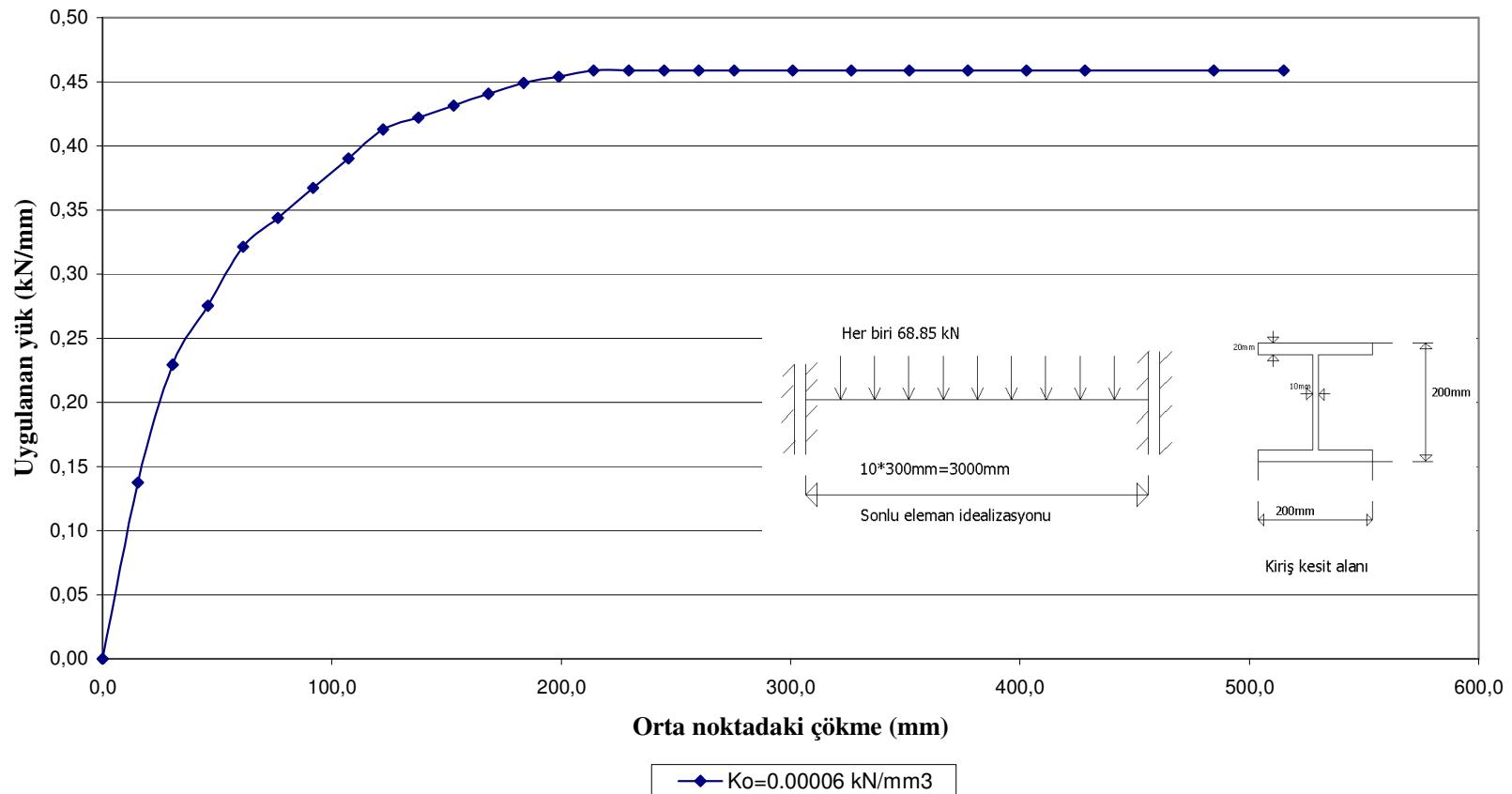
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 6 .520427E+05 -.179958E-02 .000000E+00  
 7 .520418E+05 .325108E-02 .000000E+00  
 8 .520414E+05 .142097E-03 .000000E+00  
 9 .520416E+05 .136375E-03 .000000E+00  
 10 .520419E+05 -.365257E-03 .000000E+00  
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 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .490591E+00  
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 2 .615473E+03 .000000E+00 -.200487E-08 .000000E+00  
 3 .615473E+03 .000000E+00 -.169635E-07 .000000E+00  
 4 .615473E+03 .000000E+00 -.503131E-07 .000000E+00  
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 7 .615473E+03 .000000E+00 -.930759E-07 .000000E+00  
 8 .615473E+03 .000000E+00 -.728622E-07 .000000E+00  
 9 .615473E+03 .000000E+00 -.433170E-07 .000000E+00  
 10 .615473E+03 .000000E+00 -.183835E-07 .000000E+00  
 11 .615473E+03 .000000E+00 .000000E+00 -.551386E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .551243E+05 -.217628E-02 .000000E+00  
 2 .551250E+05 .256538E-02 .000000E+00  
 3 .551258E+05 .204182E-02 .000000E+00  
 4 .551255E+05 -.261974E-02 .000000E+00  
 5 .551250E+05 -.176239E-02 .000000E+00  
 6 .551243E+05 .267982E-03 .000000E+00  
 7 .551233E+05 .121117E-03 .000000E+00  
 8 .551228E+05 -.353527E-02 .000000E+00  
 9 .551230E+05 .908852E-03 .000000E+00  
 10 .551233E+05 -.149727E-03 .000000E+00  
 0 IINCS= 9 NITER= 100 NOUTP= 2 FACTO= .200000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .474386E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .650643E+03 .000000E+00 .000000E+00 .582894E+05  
 2 .650643E+03 .000000E+00 -.257591E-08 .000000E+00  
 3 .650643E+03 .000000E+00 -.182812E-07 .000000E+00  
 4 .650643E+03 .000000E+00 -.525195E-07 .000000E+00  
 5 .650643E+03 .000000E+00 -.797100E-07 .000000E+00  
 6 .650643E+03 .000000E+00 -.962541E-07 .000000E+00  
 7 .650643E+03 .000000E+00 -.967163E-07 .000000E+00  
 8 .650643E+03 .000000E+00 -.757692E-07 .000000E+00  
 9 .650643E+03 .000000E+00 -.451718E-07 .000000E+00  
 10 .650643E+03 .000000E+00 -.194118E-07 .000000E+00  
 11 .650643E+03 .000000E+00 .000000E+00 -.582888E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .582743E+05 -.205994E-02 .000000E+00  
 2 .582750E+05 .294876E-02 .000000E+00  
 3 .582758E+05 .275898E-02 .000000E+00  
 4 .582755E+05 -.156498E-02 .000000E+00  
 5 .582750E+05 -.423431E-03 .000000E+00  
 6 .582742E+05 -.343609E-02 .000000E+00  
 7 .582732E+05 .145435E-02 .000000E+00  
 8 .582727E+05 -.256634E-02 .000000E+00  
 9 .582729E+05 .149632E-02 .000000E+00  
 10 .582733E+05 .600815E-04 .000000E+00  
 0 IINCS= 10 NITER= 100 NOUTP= 2 FACTO= .200000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1

0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .459337E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .686577E+03 .000000E+00 .000000E+00 .615082E+05  
 2 .686577E+03 .000000E+00 -.344739E-08 .000000E+00  
 3 .686577E+03 .000000E+00 -.203069E-07 .000000E+00  
 4 .686577E+03 .000000E+00 -.562686E-07 .000000E+00  
 5 .686577E+03 .000000E+00 -.849193E-07 .000000E+00  
 6 .686577E+03 .000000E+00 -.101814E-06 .000000E+00  
 7 .686577E+03 .000000E+00 -.102213E-06 .000000E+00  
 8 .686577E+03 .000000E+00 -.800679E-07 .000000E+00  
 9 .686577E+03 .000000E+00 -.478181E-07 .000000E+00  
 10 .686577E+03 .000000E+00 -.203801E-07 .000000E+00  
 11 .686577E+03 .000000E+00 .000000E+00 -.615075E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .614928E+05 .329971E-02 .000000E+00  
 2 .614934E+05 -.164032E-02 .000000E+00  
 3 .614944E+05 .393391E-02 .000000E+00  
 4 .614940E+05 -.491810E-02 .000000E+00  
 5 .614934E+05 -.341034E-02 .000000E+00  
 6 .614926E+05 -.118542E-02 .000000E+00  
 7 .614916E+05 -.173092E-02 .000000E+00  
 8 .614911E+05 -.115108E-02 .000000E+00  
 9 .614913E+05 .223255E-02 .000000E+00  
 10 .614916E+05 .543499E-02 .000000E+00  
 0 IINCS= 11 NITER= 100 NOUTP= 2 FACTO= .200000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .445344E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .723276E+03 .000000E+00 .000000E+00 .647954E+05  
 2 .723276E+03 .000000E+00 -.289005E-08 .000000E+00  
 3 .723276E+03 .000000E+00 -.195615E-07 .000000E+00  
 4 .723276E+03 .000000E+00 -.557359E-07 .000000E+00  
 5 .723276E+03 .000000E+00 -.843223E-07 .000000E+00  
 6 .723276E+03 .000000E+00 -.102013E-06 .000000E+00  
 7 .723276E+03 .000000E+00 -.103419E-06 .000000E+00  
 8 .723276E+03 .000000E+00 -.819256E-07 .000000E+00  
 9 .723276E+03 .000000E+00 -.496119E-07 .000000E+00  
 10 .723276E+03 .000000E+00 -.213003E-07 .000000E+00  
 11 .723276E+03 .000000E+00 .000000E+00 -.647947E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .647797E+05 .318909E-02 .000000E+00  
 2 .647803E+05 .327301E-02 .000000E+00  
 3 .647813E+05 .367451E-02 .000000E+00  
 4 .647809E+05 -.515079E-02 .000000E+00  
 5 .647804E+05 .168610E-02 .000000E+00  
 6 .647796E+05 -.899315E-03 .000000E+00  
 7 .647785E+05 -.110912E-02 .000000E+00  
 8 .647780E+05 -.558758E-02 .000000E+00  
 9 .647782E+05 -.239086E-02 .000000E+00  
 10 .647785E+05 .445366E-03 .000000E+00  
 0 IINCS= 12 NITER= 100 NOUTP= 2 FACTO= .200000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .432205E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .760740E+03 .000000E+00 .000000E+00 .681511E+05  
 2 .760740E+03 .000000E+00 -.271328E-08 .000000E+00  
 3 .760740E+03 .000000E+00 -.195176E-07 .000000E+00  
 4 .760740E+03 .000000E+00 -.561930E-07 .000000E+00  
 5 .760740E+03 .000000E+00 -.855829E-07 .000000E+00  
 6 .760740E+03 .000000E+00 -.103643E-06 .000000E+00

7 .760740E+03 .000000E+00 -.105568E-06 .000000E+00  
 8 .760740E+03 .000000E+00 -.841470E-07 .000000E+00  
 9 .760740E+03 .000000E+00 -.513446E-07 .000000E+00  
 10 .760740E+03 .000000E+00 -.221722E-07 .000000E+00  
 11 .760740E+03 .000000E+00 .000000E+00 -.681504E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .681351E+05 -.202560E-02 .000000E+00  
 2 .681357E+05 .322723E-02 .000000E+00  
 3 .681367E+05 .375843E-02 .000000E+00  
 4 .681363E+05 .376701E-03 .000000E+00  
 5 .681358E+05 -.290298E-02 .000000E+00  
 6 .681350E+05 -.128746E-03 .000000E+00  
 7 .681339E+05 -.539684E-02 .000000E+00  
 8 .681334E+05 -.478268E-02 .000000E+00  
 9 .681335E+05 -.186062E-02 .000000E+00  
 10 .681339E+05 .620842E-03 .000000E+00  
 0 IINCS= 13 NITER= 100 NOUTP= 2 FACTO= .100000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .415953E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .798586E+03 .000000E+00 .000000E+00 .715409E+05  
 2 .798586E+03 .000000E+00 -.324405E-08 .000000E+00  
 3 .798586E+03 .000000E+00 -.206627E-07 .000000E+00  
 4 .798586E+03 .000000E+00 -.582902E-07 .000000E+00  
 5 .798586E+03 .000000E+00 -.882569E-07 .000000E+00  
 6 .798586E+03 .000000E+00 -.106655E-06 .000000E+00  
 7 .798586E+03 .000000E+00 -.107932E-06 .000000E+00  
 8 .798586E+03 .000000E+00 -.850141E-07 .000000E+00  
 9 .798586E+03 .000000E+00 -.514347E-07 .000000E+00  
 10 .798586E+03 .000000E+00 -.225792E-07 .000000E+00  
 11 .798586E+03 .000000E+00 .000000E+00 -.715402E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .715247E+05 .326157E-02 .000000E+00  
 2 .715254E+05 .357056E-02 .000000E+00  
 3 .715264E+05 .441837E-02 .000000E+00  
 4 .715260E+05 -.383091E-02 .000000E+00  
 5 .715254E+05 -.174332E-02 .000000E+00  
 6 .715246E+05 -.421429E-02 .000000E+00  
 7 .715234E+05 -.474072E-02 .000000E+00  
 8 .715229E+05 -.458813E-02 .000000E+00  
 9 .715232E+05 .342274E-02 .000000E+00  
 10 .715235E+05 .704765E-03 .000000E+00  
 0 IINCS= 14 NITER= 100 NOUTP= 2 FACTO= .100000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .400966E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .836814E+03 .000000E+00 .000000E+00 .749650E+05  
 2 .836814E+03 .000000E+00 -.402446E-08 .000000E+00  
 3 .836814E+03 .000000E+00 -.224762E-07 .000000E+00  
 4 .836814E+03 .000000E+00 -.610799E-07 .000000E+00  
 5 .836814E+03 .000000E+00 -.913456E-07 .000000E+00  
 6 .836814E+03 .000000E+00 -.109725E-06 .000000E+00  
 7 .836814E+03 .000000E+00 -.110184E-06 .000000E+00  
 8 .836814E+03 .000000E+00 -.864822E-07 .000000E+00  
 9 .836814E+03 .000000E+00 -.525237E-07 .000000E+00  
 10 .836814E+03 .000000E+00 -.225094E-07 .000000E+00  
 11 .836814E+03 .000000E+00 .000000E+00 -.749643E+05  
 0 ELEMENT STRESSES PL STRAIN  
 1 .749486E+05 .342178E-02 .000000E+00  
 2 .749493E+05 .409698E-02 .000000E+00

3	.749503E+05	.176430E-03	.000000E+00
4	.749499E+05	-.263309E-02	.000000E+00
5	.749493E+05	-.488281E-03	.000000E+00
6	.749484E+05	-.313091E-02	.000000E+00
7	.749473E+05	.119495E-02	.000000E+00
8	.749468E+05	.111103E-02	.000000E+00
9	.749470E+05	-.154781E-02	.000000E+00
10	.749473E+05	.689507E-03	.000000E+00

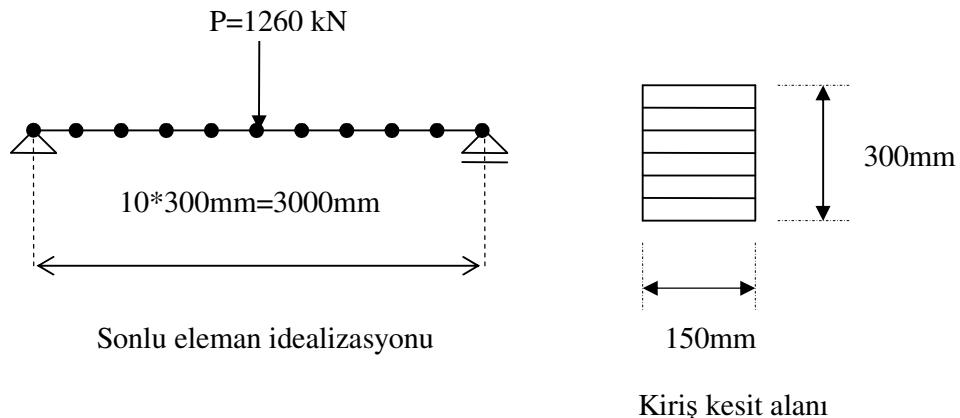


**Şekil 5.8:** Elastik zemine oturan uniform yayılı yüklü tabakasız Timoshenko kırışı örneği

## 5.2 Tabakalı Elastoplastik Timoshenko Kiriş Örnekleri

Tabakalı kiriş örneklerinde elastik zemin durumu ve kayma şekil değiştirmelerini içeren sistem rijitlik matrisi kullanılmamıştır.

### 5.2.1 Tekil yüklü tabakalı Timoshenko kirişleri örneği



**Şekil 5.9:** Tabakalı Timoshenko kirişinde sabit tekil yük hali

Tabakasız kiriş örneklerindeki kiriş kesitin 6 tabakaya bölünerek hesap yapıldığı bu durumda, kiriş katmanları en üstteki tabakadan aşağıya doğru numaralandırılır.

$b_1$	$h_1$
$b_2$	$h_2$
$b_3$	$h_3$
$b_4$	$h_4$
$b_5$	$h_5$
$b_6$	$h_6$

**Şekil 5.10:** Tabakalı kirişte tabakalara ait boyutların simgesel gösterimi

### **Kirişin malzeme özellikleri;**

E (Elastisite modülü)=210 kN/mm<sup>2</sup>

v (Poisson oranı) = 0.3

$\sigma_0$  (Akma gerilmesi) = 0.25 kN/mm<sup>2</sup>

H<sup>I</sup> (Pekleşme parametresi) = 0.0

### **Kirişin kesit özellikleri;**

b<sub>1</sub>=b<sub>2</sub>=b<sub>3</sub>=b<sub>4</sub>=b<sub>5</sub>=b<sub>6</sub>= 150mm

h<sub>1</sub>=h<sub>2</sub>=h<sub>3</sub>=h<sub>4</sub>=h<sub>5</sub>=h<sub>6</sub>= 50mm

l=3000mm

### **Probleme ait bilgilerin programa giriş listesi;**

Burada girilen verilerin açıklaması yapıldığı için formatlı girişteki düzen gözükmemektedir. Açıklamaların hemen altına formatlı veri giriş biçimi ilave edilmiştir.

11 10 2 1 **17(NPROP)** 2 14 2 2 **6**(Tabaka sayısı)

1

<b>210.</b> (E)	<b>53.846</b> (G/1.5)	<b>0.25</b> ( $\sigma_0$ )	<b>0.</b> (H <sup>I</sup> )
300.(h)	150.(b <sub>1</sub> )	50.(h <sub>1</sub> )	150.(b <sub>2</sub> )
50.(h <sub>2</sub> )	150.(b <sub>3</sub> )	50.(h <sub>3</sub> )	150.(b <sub>4</sub> )
50.(h <sub>4</sub> )	150.(b <sub>5</sub> )	50.(h <sub>5</sub> )	150.(b <sub>6</sub> )
50.(h <sub>6</sub> )			

Diğer veriler Örnek 5.1.1'deki gibidir.

### **Veri girişi sonrası alınan sonuçlar;**

NPOIN= 11 NELEM= 10 NBOUN= 2 NMATS= 1

NPROP= 17 NNODE= 2 NINCS= 14 NALGO= 2

NDOFN= 2 NLAYR= 6

0 MATERIAL PROPERTIES  
 1  
 210.00000 53.84600 .25000 .00000  
 300.00000 150.00000 50.00000 150.00000  
 50.00000 150.00000 50.00000 150.00000  
 50.00000 150.00000 50.00000 150.00000  
 50.00000  
 0 EL NODES MAT.  
 1 1 2 1  
 2 2 3 1  
 3 3 4 1  
 4 4 5 1  
 5 5 6 1  
 6 6 7 1  
 7 7 8 1  
 8 8 9 1  
 9 9 10 1  
 10 10 11 1  
 0 NODE COORD.  
 1 .00000  
 2 300.00000  
 3 600.00000  
 4 900.00000  
 5 1200.00000  
 6 1500.00000  
 7 1800.00000  
 8 2100.00000  
 9 2400.00000  
 10 2700.00000  
 11 3000.00000  
 0 RES.NODE CODE PRES.VALUES CODE PRES.VALUES  
 1 1 .00000 0 .00000  
 11 1 .00000 0 .00000  
 0 ELEMENT NODAL LOADS  
 1 .00000 .00000 .00000 .00000  
 2 .00000 .00000 .00000 .00000  
 3 .00000 .00000 .00000 .00000  
 4 .00000 .00000 .00000 .00000  
 5 .00000 .00000 .00000 .00000  
 6 1260.00000 .00000 .00000 .00000  
 7 .00000 .00000 .00000 .00000  
 8 .00000 .00000 .00000 .00000  
 9 .00000 .00000 .00000 .00000  
 10 .00000 .00000 .00000 .00000  
 0 IINCS= 1 NITER= 100 NOUTP= 2 FACTO= .300000E+00 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .368134E+01  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.189001E+03 .308648E-02 .000000E+00  
 2 .930828E+00 .000000E+00 .296301E-02 .000000E+00  
 3 .178758E+01 .000000E+00 .259262E-02 .000000E+00  
 4 .249617E+01 .000000E+00 .197531E-02 .000000E+00  
 5 .298253E+01 .000000E+00 .111109E-02 .000000E+00  
 6 .317260E+01 .000000E+00 -.280374E-08 .000000E+00  
 7 .298253E+01 .000000E+00 -.111110E-02 .000000E+00  
 8 .249617E+01 .000000E+00 -.197531E-02 .000000E+00  
 9 .178758E+01 .000000E+00 -.259262E-02 .000000E+00  
 10 .930827E+00 .000000E+00 -.296301E-02 .000000E+00  
 11 .000000E+00 -.189000E+03 -.308648E-02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN

```

1 .283585E+05 .189031E+03 .000000E+00
2 .850746E+05 .189028E+03 .000000E+00
3 .141789E+06 .189022E+03 .000000E+00
4 .198499E+06 .189017E+03 .000000E+00
5 .255205E+06 .189005E+03 .000000E+00
6 .255205E+06 -.189006E+03 .000000E+00
7 .198499E+06 -.189014E+03 .000000E+00
8 .141788E+06 -.189022E+03 .000000E+00
9 .850743E+05 -.189027E+03 .000000E+00
10 .283583E+05 -.189030E+03 .000000E+00

0 ITERATION NUMBER= 2
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .114459E-01
0 NODE DISPL. REACTION DISPL. REACTION
 1 .000000E+00 -.189000E+03 .308571E-02 .000000E+00
 2 .930600E+00 .000000E+00 .296229E-02 .000000E+00
 3 .178714E+01 .000000E+00 .259200E-02 .000000E+00
 4 .249557E+01 .000000E+00 .197486E-02 .000000E+00
 5 .298183E+01 .000000E+00 .111086E-02 .000000E+00
 6 .317186E+01 .000000E+00 -.376121E-11 .000000E+00
 7 .298183E+01 .000000E+00 -.111086E-02 .000000E+00
 8 .249557E+01 .000000E+00 -.197486E-02 .000000E+00
 9 .178714E+01 .000000E+00 -.259200E-02 .000000E+00
10 .930600E+00 .000000E+00 -.296229E-02 .000000E+00
11 .000000E+00 -.189000E+03 -.308571E-02 .000000E+00

0 ELEMENT STRESSES PL STRAIN
 1 .283500E+05 .189000E+03 .000000E+00
 2 .850500E+05 .189000E+03 .000000E+00
 3 .141750E+06 .189000E+03 .000000E+00
 4 .198450E+06 .189000E+03 .000000E+00
 5 .255150E+06 .189000E+03 .000000E+00
 6 .255150E+06 -.189000E+03 .000000E+00
 7 .198450E+06 -.189000E+03 .000000E+00
 8 .141750E+06 -.189000E+03 .000000E+00
 9 .850500E+05 -.189000E+03 .000000E+00
10 .283500E+05 -.189000E+03 .000000E+00

0 IINCS= 2 NITER= 100 NOUTP= 2 FACTO= .200000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .143241E+01
0 NODE DISPL. REACTION DISPL. REACTION
 1 .000000E+00 -.315001E+03 .514337E-02 .000000E+00
 2 .155115E+01 .000000E+00 .493763E-02 .000000E+00
 3 .297886E+01 .000000E+00 .432041E-02 .000000E+00
 4 .415969E+01 .000000E+00 .329173E-02 .000000E+00
 5 .497018E+01 .000000E+00 .185159E-02 .000000E+00
 6 .528692E+01 .000000E+00 -.175840E-08 .000000E+00
 7 .497018E+01 .000000E+00 -.185159E-02 .000000E+00
 8 .415968E+01 .000000E+00 -.329173E-02 .000000E+00
 9 .297886E+01 .000000E+00 -.432041E-02 .000000E+00
10 .155115E+01 .000000E+00 -.493763E-02 .000000E+00
11 .000000E+00 -.315000E+03 -.514336E-02 .000000E+00

0 ELEMENT STRESSES PL STRAIN
 1 .472556E+05 .315021E+03 .000000E+00
 2 .141766E+06 .315019E+03 .000000E+00
 3 .236276E+06 .315015E+03 .000000E+00
 4 .330783E+06 .315011E+03 .000000E+00
 5 .425287E+06 .315003E+03 .000000E+00
 6 .425287E+06 -.315004E+03 .000000E+00
 7 .330782E+06 -.315011E+03 .000000E+00
 8 .236275E+06 -.315016E+03 .000000E+00
 9 .141766E+06 -.315019E+03 .000000E+00

```

10 .472555E+05 -.315020E+03 .000000E+00  
 0 ITERATION NUMBER= 2  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .859152E-02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.315000E+03 .514286E-02 .000000E+00  
 2 .155100E+01 .000000E+00 .493714E-02 .000000E+00  
 3 .297857E+01 .000000E+00 .432000E-02 .000000E+00  
 4 .415929E+01 .000000E+00 .329143E-02 .000000E+00  
 5 .496971E+01 .000000E+00 .185143E-02 .000000E+00  
 6 .528643E+01 .000000E+00 .489608E-11 .000000E+00  
 7 .496971E+01 .000000E+00 -.185143E-02 .000000E+00  
 8 .415929E+01 .000000E+00 -.329143E-02 .000000E+00  
 9 .297857E+01 .000000E+00 -.432000E-02 .000000E+00  
 10 .155100E+01 .000000E+00 -.493714E-02 .000000E+00  
 11 .000000E+00 -.315000E+03 -.514286E-02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .472500E+05 .315000E+03 .000000E+00  
 2 .141750E+06 .315000E+03 .000000E+00  
 3 .236250E+06 .315000E+03 .000000E+00  
 4 .330750E+06 .315000E+03 .000000E+00  
 5 .425250E+06 .315000E+03 .000000E+00  
 6 .425250E+06 -.315000E+03 .000000E+00  
 7 .330750E+06 -.315000E+03 .000000E+00  
 8 .236250E+06 -.315000E+03 .000000E+00  
 9 .141750E+06 -.315000E+03 .000000E+00  
 10 .472500E+05 -.315000E+03 .000000E+00  
 0 IINCS= 3 NITER= 100 NOUTP= 2 FACTO= .100000E+00 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .597672E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.378000E+03 .617168E-02 .000000E+00  
 2 .186128E+01 .000000E+00 .592481E-02 .000000E+00  
 3 .357443E+01 .000000E+00 .518421E-02 .000000E+00  
 4 .499134E+01 .000000E+00 .394987E-02 .000000E+00  
 5 .596389E+01 .000000E+00 .222179E-02 .000000E+00  
 6 .634396E+01 .000000E+00 -.924345E-09 .000000E+00  
 7 .596389E+01 .000000E+00 -.222180E-02 .000000E+00  
 8 .499134E+01 .000000E+00 -.394987E-02 .000000E+00  
 9 .357443E+01 .000000E+00 -.518421E-02 .000000E+00  
 10 .186128E+01 .000000E+00 -.592481E-02 .000000E+00  
 11 .000000E+00 -.378000E+03 -.617168E-02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .567028E+05 .378010E+03 .000000E+00  
 2 .170108E+06 .378010E+03 .000000E+00  
 3 .283513E+06 .378008E+03 .000000E+00  
 4 .396917E+06 .378005E+03 .000000E+00  
 5 .510318E+06 .378002E+03 .000000E+00  
 6 .510318E+06 -.378003E+03 .000000E+00  
 7 .396916E+06 -.378005E+03 .000000E+00  
 8 .283513E+06 -.378008E+03 .000000E+00  
 9 .170108E+06 -.378009E+03 .000000E+00  
 10 .567027E+05 -.378010E+03 .000000E+00  
 0 ITERATION NUMBER= 2  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .776480E-02  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.378000E+03 .617143E-02 .000000E+00  
 2 .186120E+01 .000000E+00 .592457E-02 .000000E+00  
 3 .357429E+01 .000000E+00 .518400E-02 .000000E+00  
 4 .499114E+01 .000000E+00 .394971E-02 .000000E+00  
 5 .596366E+01 .000000E+00 .222171E-02 .000000E+00

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6 .634372E+01 .000000E+00 -.196708E-09 .000000E+00
7 .596366E+01 .000000E+00 -.222171E-02 .000000E+00
8 .499114E+01 .000000E+00 -.394971E-02 .000000E+00
9 .357429E+01 .000000E+00 -.518400E-02 .000000E+00
10 .186120E+01 .000000E+00 -.592457E-02 .000000E+00
11 .000000E+00 -.378000E+03 -.617143E-02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .567000E+05 .378000E+03 .000000E+00
2 .170100E+06 .378000E+03 .000000E+00
3 .283500E+06 .378000E+03 .000000E+00
4 .396900E+06 .378000E+03 .000000E+00
5 .510300E+06 .378000E+03 .000000E+00
6 .510300E+06 -.378000E+03 .000000E+00
7 .396900E+06 -.378000E+03 .000000E+00
8 .283500E+06 -.378000E+03 .000000E+00
9 .170100E+06 -.378000E+03 .000000E+00
10 .567000E+05 -.378000E+03 .000000E+00
0 IINCS= 4 NITER= 100 NOUTP= 2 FACTO= .100000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .515248E+00
0 NODE DISPL. REACTION DISPL. REACTION
1 .000000E+00 -.441000E+03 .720026E-02 .000000E+00
2 .217148E+01 .000000E+00 .691224E-02 .000000E+00
3 .417015E+01 .000000E+00 .604821E-02 .000000E+00
4 .582320E+01 .000000E+00 .460815E-02 .000000E+00
5 .695784E+01 .000000E+00 .259208E-02 .000000E+00
6 .740125E+01 .000000E+00 -.977916E-09 .000000E+00
7 .695783E+01 .000000E+00 -.259208E-02 .000000E+00
8 .582320E+01 .000000E+00 -.460815E-02 .000000E+00
9 .417014E+01 .000000E+00 -.604821E-02 .000000E+00
10 .217148E+01 .000000E+00 -.691224E-02 .000000E+00
11 .000000E+00 -.441000E+03 -.720025E-02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .661528E+05 .441010E+03 .000000E+00
2 .198458E+06 .441010E+03 .000000E+00
3 .330763E+06 .441007E+03 .000000E+00
4 .463066E+06 .441005E+03 .000000E+00
5 .595368E+06 .441002E+03 .000000E+00
6 .595368E+06 -.441002E+03 .000000E+00
7 .463066E+06 -.441005E+03 .000000E+00
8 .330763E+06 -.441008E+03 .000000E+00
9 .198458E+06 -.441009E+03 .000000E+00
10 .661528E+05 -.441010E+03 .000000E+00
0 ITERATION NUMBER= 2
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .105389E-01
0 NODE DISPL. REACTION DISPL. REACTION
1 .000000E+00 -.441000E+03 .720000E-02 .000000E+00
2 .217140E+01 .000000E+00 .691200E-02 .000000E+00
3 .417000E+01 .000000E+00 .604800E-02 .000000E+00
4 .582300E+01 .000000E+00 .460800E-02 .000000E+00
5 .695760E+01 .000000E+00 .259200E-02 .000000E+00
6 .740100E+01 .000000E+00 -.271079E-09 .000000E+00
7 .695760E+01 .000000E+00 -.259200E-02 .000000E+00
8 .582300E+01 .000000E+00 -.460800E-02 .000000E+00
9 .417000E+01 .000000E+00 -.604800E-02 .000000E+00
10 .217140E+01 .000000E+00 -.691200E-02 .000000E+00
11 .000000E+00 -.441000E+03 -.720000E-02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .661500E+05 .441000E+03 .000000E+00
2 .198450E+06 .441000E+03 .000000E+00

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3 .330750E+06 .441000E+03 .000000E+00  
 4 .463050E+06 .441000E+03 .000000E+00  
 5 .595350E+06 .441000E+03 .000000E+00  
 6 .595350E+06 -.441000E+03 .000000E+00  
 7 .463050E+06 -.441000E+03 .000000E+00  
 8 .330750E+06 -.441000E+03 .000000E+00  
 9 .198450E+06 -.441000E+03 .000000E+00  
 10 .661500E+05 -.441000E+03 .000000E+00  
 0 IINCS= 5 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .238967E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.472500E+03 .771441E-02 .000000E+00  
 2 .232654E+01 .000000E+00 .740584E-02 .000000E+00  
 3 .446793E+01 .000000E+00 .648010E-02 .000000E+00  
 4 .623903E+01 .000000E+00 .493722E-02 .000000E+00  
 5 .745469E+01 .000000E+00 .277718E-02 .000000E+00  
 6 .792977E+01 .000000E+00 -.539610E-09 .000000E+00  
 7 .745469E+01 .000000E+00 -.277718E-02 .000000E+00  
 8 .623903E+01 .000000E+00 -.493722E-02 .000000E+00  
 9 .446793E+01 .000000E+00 -.648010E-02 .000000E+00  
 10 .232654E+01 .000000E+00 -.740583E-02 .000000E+00  
 11 .000000E+00 -.472500E+03 -.771441E-02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .708764E+05 .472505E+03 .000000E+00  
 2 .212629E+06 .472505E+03 .000000E+00  
 3 .354381E+06 .472504E+03 .000000E+00  
 4 .496133E+06 .472503E+03 .000000E+00  
 5 .637884E+06 .472501E+03 .000000E+00  
 6 .637884E+06 -.472501E+03 .000000E+00  
 7 .496133E+06 -.472503E+03 .000000E+00  
 8 .354381E+06 -.472504E+03 .000000E+00  
 9 .212629E+06 -.472505E+03 .000000E+00  
 10 .708764E+05 -.472505E+03 .000000E+00  
 0 IINCS= 6 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .197674E+04  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.504000E+03 .822870E-02 .000000E+00  
 2 .248164E+01 .000000E+00 .789955E-02 .000000E+00  
 3 .476579E+01 .000000E+00 .691210E-02 .000000E+00  
 4 .665496E+01 .000000E+00 .526636E-02 .000000E+00  
 5 .795166E+01 .000000E+00 .296233E-02 .000000E+00  
 6 .845841E+01 .000000E+00 -.615301E-09 .000000E+00  
 7 .795166E+01 .000000E+00 -.296233E-02 .000000E+00  
 8 .665496E+01 .000000E+00 -.526636E-02 .000000E+00  
 9 .476579E+01 .000000E+00 -.691210E-02 .000000E+00  
 10 .248164E+01 .000000E+00 -.789955E-02 .000000E+00  
 11 .000000E+00 -.504000E+03 -.822870E-02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .756014E+05 .504005E+03 .000000E+00  
 2 .226804E+06 .504005E+03 .000000E+00  
 3 .378006E+06 .504004E+03 .000000E+00  
 4 .529208E+06 .504003E+03 .000000E+00  
 5 .663153E+06 .504001E+03 .000000E+00  
 6 .663153E+06 -.504001E+03 .000000E+00  
 7 .529208E+06 -.504002E+03 .000000E+00  
 8 .378006E+06 -.504004E+03 .000000E+00  
 9 .226804E+06 -.504005E+03 .000000E+00  
 10 .756014E+05 -.504005E+03 .000000E+00

0 ITERATION NUMBER= 2  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .147266E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .000000E+00 -.504000E+03 .849157E-02 .000000E+00  
   2 .256050E+01 .000000E+00 .816243E-02 .000000E+00  
   3 .492351E+01 .000000E+00 .717499E-02 .000000E+00  
   4 .689155E+01 .000000E+00 .552926E-02 .000000E+00  
   5 .826712E+01 .000000E+00 .322524E-02 .000000E+00  
   6 .881331E+01 .000000E+00 -.148287E-09 .000000E+00  
   7 .826713E+01 .000000E+00 -.322524E-02 .000000E+00  
   8 .689155E+01 .000000E+00 -.552926E-02 .000000E+00  
   9 .492351E+01 .000000E+00 -.717499E-02 .000000E+00  
 10 .256050E+01 .000000E+00 -.816242E-02 .000000E+00  
 11 .000000E+00 -.504000E+03 -.849157E-02 .000000E+00  
 0 ELEMENT STRESSES PL.STRAIN  
   1 .756007E+05 .504003E+03 .000000E+00  
   2 .226802E+06 .504003E+03 .000000E+00  
   3 .378004E+06 .504003E+03 .000000E+00  
   4 .529205E+06 .504003E+03 .000000E+00  
   5 .680406E+06 .504001E+03 .000000E+00  
   6 .680406E+06 -.504001E+03 .000000E+00  
   7 .529205E+06 -.504003E+03 .000000E+00  
   8 .378004E+06 -.504003E+03 .000000E+00  
   9 .226802E+06 -.504003E+03 .000000E+00  
 10 .756007E+05 -.504003E+03 .000000E+00  
 0 IINCS= 7 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .458286E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .000000E+00 -.535500E+03 .946905E-02 .000000E+00  
   2 .285456E+01 .000000E+00 .911933E-02 .000000E+00  
   3 .549928E+01 .000000E+00 .807015E-02 .000000E+00  
   4 .772433E+01 .000000E+00 .632152E-02 .000000E+00  
   5 .931988E+01 .000000E+00 .387345E-02 .000000E+00  
   6 .996720E+01 .000000E+00 -.956933E-09 .000000E+00  
   7 .931988E+01 .000000E+00 -.387345E-02 .000000E+00  
   8 .772433E+01 .000000E+00 -.632152E-02 .000000E+00  
   9 .549928E+01 .000000E+00 -.807015E-02 .000000E+00  
 10 .285456E+01 .000000E+00 -.911933E-02 .000000E+00  
 11 .000000E+00 -.535500E+03 -.946905E-02 .000000E+00  
 0 ELEMENT STRESSES PL.STRAIN  
   1 .803277E+05 .535510E+03 .000000E+00  
   2 .240983E+06 .535509E+03 .000000E+00  
   3 .401638E+06 .535508E+03 .000000E+00  
   4 .562292E+06 .535507E+03 .000000E+00  
   5 .722945E+06 .535503E+03 .000000E+00  
   6 .722945E+06 -.535504E+03 .000000E+00  
   7 .562292E+06 -.535507E+03 .000000E+00  
   8 .401638E+06 -.535508E+03 .000000E+00  
   9 .240983E+06 -.535509E+03 .000000E+00  
 10 .803276E+05 -.535510E+03 .000000E+00  
 0 IINCS= 8 NITER= 100 NOUTP= 2 FACTO= .500000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .425359E+00  
 0 NODE DISPL. REACTION DISPL. REACTION  
   1 .000000E+00 -.567000E+03 .104462E-01 .000000E+00  
   2 .314852E+01 .000000E+00 .100759E-01 .000000E+00  
   3 .607485E+01 .000000E+00 .896501E-02 .000000E+00  
   4 .855683E+01 .000000E+00 .711352E-02 .000000E+00  
   5 .103723E+02 .000000E+00 .452145E-02 .000000E+00

6	.111207E+02	.000000E+00	-.596281E-09	.000000E+00	
7	.103723E+02	.000000E+00	-.452145E-02	.000000E+00	
8	.855683E+01	.000000E+00	-.711352E-02	.000000E+00	
9	.607485E+01	.000000E+00	-.896501E-02	.000000E+00	
10	.314852E+01	.000000E+00	-.100759E-01	.000000E+00	
11	.000000E+00	-.567000E+03	-.104462E-01	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.850527E+05	.567010E+03	.000000E+00		
2	.255158E+06	.567009E+03	.000000E+00		
3	.425263E+06	.567008E+03	.000000E+00		
4	.595367E+06	.567008E+03	.000000E+00		
5	.765470E+06	.567002E+03	.000000E+00		
6	.765470E+06	-.567004E+03	.000000E+00		
7	.595367E+06	-.567007E+03	.000000E+00		
8	.425263E+06	-.567009E+03	.000000E+00		
9	.255158E+06	-.567009E+03	.000000E+00		
10	.850526E+05	-.567010E+03	.000000E+00		
0	IINCS= 9	NITER= 100	NOUTP= 2	FACTO= .200000E-01	
0	TOLER= .500000E+00				
0	ITERATION NUMBER= 1				
0	CONVERGENCE CODE= 1	NORM OF RESIDUAL SUM RATIO= .109134E+03			
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.000000E+00	-.579600E+03	.108368E-01	.000000E+00	
2	.326601E+01	.000000E+00	.104582E-01	.000000E+00	
3	.630491E+01	.000000E+00	.932269E-02	.000000E+00	
4	.888959E+01	.000000E+00	.743009E-02	.000000E+00	
5	.107929E+02	.000000E+00	.478047E-02	.000000E+00	
6	.115818E+02	.000000E+00	-.115786E-08	.000000E+00	
7	.107929E+02	.000000E+00	-.478047E-02	.000000E+00	
8	.888959E+01	.000000E+00	-.743010E-02	.000000E+00	
9	.630491E+01	.000000E+00	-.932269E-02	.000000E+00	
10	.326601E+01	.000000E+00	-.104582E-01	.000000E+00	
11	.000000E+00	-.579600E+03	-.108368E-01	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.869411E+05	.579604E+03	.000000E+00		
2	.260823E+06	.579604E+03	.000000E+00		
3	.434705E+06	.579604E+03	.000000E+00		
4	.608587E+06	.579603E+03	.000000E+00		
5	.781372E+06	.579601E+03	.000000E+00		
6	.781372E+06	-.579601E+03	.000000E+00		
7	.608587E+06	-.579603E+03	.000000E+00		
8	.434705E+06	-.579603E+03	.000000E+00		
9	.260823E+06	-.579604E+03	.000000E+00		
10	.869411E+05	-.579604E+03	.000000E+00		
0	ITERATION NUMBER= 2				
0	CONVERGENCE CODE= 0	NORM OF RESIDUAL SUM RATIO= .783295E-01			
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.000000E+00	-.579600E+03	.110031E-01	.000000E+00	
2	.331592E+01	.000000E+00	.106246E-01	.000000E+00	
3	.640474E+01	.000000E+00	.948907E-02	.000000E+00	
4	.903933E+01	.000000E+00	.759649E-02	.000000E+00	
5	.109926E+02	.000000E+00	.494687E-02	.000000E+00	
6	.118064E+02	.000000E+00	-.186900E-08	.000000E+00	
7	.109926E+02	.000000E+00	-.494687E-02	.000000E+00	
8	.903933E+01	.000000E+00	-.759649E-02	.000000E+00	
9	.640474E+01	.000000E+00	-.948907E-02	.000000E+00	
10	.331592E+01	.000000E+00	-.106246E-01	.000000E+00	
11	.000000E+00	-.579600E+03	-.110031E-01	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.869405E+05	.579602E+03	.000000E+00		
2	.260821E+06	.579602E+03	.000000E+00		

3 .434702E+06 .579602E+03 .000000E+00  
 4 .608583E+06 .579602E+03 .000000E+00  
 5 .782464E+06 .579601E+03 .000000E+00  
 6 .782464E+06 -.579601E+03 .000000E+00  
 7 .608583E+06 -.579602E+03 .000000E+00  
 8 .434702E+06 -.579602E+03 .000000E+00  
 9 .260821E+06 -.579602E+03 .000000E+00  
 10 .869404E+05 -.579602E+03 .000000E+00  
 0 IINCS= 10 NITER= 100 NOUTP= 2 FACTO= .200000E-01 TOLER= .500000E+00  
 0 ITERATION NUMBER= 1  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .125104E+01  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.592201E+03 .137362E-01 .000000E+00  
 2 .413617E+01 .000000E+00 .133494E-01 .000000E+00  
 3 .804028E+01 .000000E+00 .121891E-01 .000000E+00  
 4 .114803E+02 .000000E+00 .102552E-01 .000000E+00  
 5 .142240E+02 .000000E+00 .754781E-02 .000000E+00  
 6 .154295E+02 .000000E+00 -.264980E-07 .000000E+00  
 7 .142240E+02 .000000E+00 -.754781E-02 .000000E+00  
 8 .114803E+02 .000000E+00 -.102552E-01 .000000E+00  
 9 .804028E+01 .000000E+00 -.121891E-01 .000000E+00  
 10 .413617E+01 .000000E+00 -.133494E-01 .000000E+00  
 11 .000000E+00 -.592200E+03 -.137362E-01 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .888376E+05 .592228E+03 .000000E+00  
 2 .266513E+06 .592228E+03 .000000E+00  
 3 .444188E+06 .592227E+03 .000000E+00  
 4 .621862E+06 .592228E+03 .000000E+00  
 5 .799533E+06 .592212E+03 .000000E+00  
 6 .799532E+06 -.592214E+03 .000000E+00  
 7 .621862E+06 -.592229E+03 .000000E+00  
 8 .444187E+06 -.592226E+03 .000000E+00  
 9 .266512E+06 -.592227E+03 .000000E+00  
 10 .888373E+05 -.592227E+03 .000000E+00  
 0 ITERATION NUMBER= 2  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .208280E+03  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.592200E+03 .137261E-01 .000000E+00  
 2 .413314E+01 .000000E+00 .133394E-01 .000000E+00  
 3 .803424E+01 .000000E+00 .121791E-01 .000000E+00  
 4 .114713E+02 .000000E+00 .102454E-01 .000000E+00  
 5 .142121E+02 .000000E+00 .753824E-02 .000000E+00  
 6 .154162E+02 .000000E+00 .256866E-08 .000000E+00  
 7 .142121E+02 .000000E+00 -.753824E-02 .000000E+00  
 8 .114713E+02 .000000E+00 -.102454E-01 .000000E+00  
 9 .803424E+01 .000000E+00 -.121792E-01 .000000E+00  
 10 .413314E+01 .000000E+00 -.133394E-01 .000000E+00  
 11 .000000E+00 -.592200E+03 -.137261E-01 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .888300E+05 .592200E+03 .000000E+00  
 2 .266490E+06 .592200E+03 .000000E+00  
 3 .444150E+06 .592200E+03 .000000E+00  
 4 .621810E+06 .592200E+03 .000000E+00  
 5 .797327E+06 .592200E+03 .000000E+00  
 6 .797340E+06 -.592200E+03 .000000E+00  
 7 .621810E+06 -.592200E+03 .000000E+00  
 8 .444150E+06 -.592200E+03 .000000E+00  
 9 .266490E+06 -.592200E+03 .000000E+00  
 10 .888300E+05 -.592200E+03 .000000E+00  
 0 ITERATION NUMBER= 3

0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .208335E+03  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.592200E+03 .140530E-01 .000000E+00  
 2 .423122E+01 .000000E+00 .136663E-01 .000000E+00  
 3 .823038E+01 .000000E+00 .125060E-01 .000000E+00  
 4 .117655E+02 .000000E+00 .105723E-01 .000000E+00  
 5 .146044E+02 .000000E+00 .786507E-02 .000000E+00  
 6 .158573E+02 .000000E+00 -.922331E-06 .000000E+00  
 7 .146041E+02 .000000E+00 -.786487E-02 .000000E+00  
 8 .117653E+02 .000000E+00 -.105721E-01 .000000E+00  
 9 .823026E+01 .000000E+00 -.125058E-01 .000000E+00  
 10 .423115E+01 .000000E+00 -.136661E-01 .000000E+00  
 11 .000000E+00 -.592200E+03 -.140528E-01 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .888309E+05 .592203E+03 .000000E+00  
 2 .266493E+06 .592203E+03 .000000E+00  
 3 .444155E+06 .592203E+03 .000000E+00  
 4 .621816E+06 .592203E+03 .000000E+00  
 5 .801621E+06 .592201E+03 .000000E+00  
 6 .801607E+06 -.592202E+03 .000000E+00  
 7 .621816E+06 -.592203E+03 .000000E+00  
 8 .444154E+06 -.592203E+03 .000000E+00  
 9 .266493E+06 -.592203E+03 .000000E+00  
 10 .888309E+05 -.592203E+03 .000000E+00  
 0 ITERATION NUMBER= 4  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .713193E+04  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.592200E+03 .137249E-01 .000000E+00  
 2 .413279E+01 .000000E+00 .133382E-01 .000000E+00  
 3 .803354E+01 .000000E+00 .121780E-01 .000000E+00  
 4 .114702E+02 .000000E+00 .102443E-01 .000000E+00  
 5 .142107E+02 .000000E+00 .753712E-02 .000000E+00  
 6 .154146E+02 .000000E+00 .502786E-08 .000000E+00  
 7 .142107E+02 .000000E+00 -.753712E-02 .000000E+00  
 8 .114702E+02 .000000E+00 -.102443E-01 .000000E+00  
 9 .803354E+01 .000000E+00 -.121780E-01 .000000E+00  
 10 .413279E+01 .000000E+00 -.133382E-01 .000000E+00  
 11 .000000E+00 -.592200E+03 -.137249E-01 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .888291E+05 .592196E+03 .000000E+00  
 2 .266487E+06 .592197E+03 .000000E+00  
 3 .444145E+06 .592197E+03 .000000E+00  
 4 .621804E+06 .592197E+03 .000000E+00  
 5 .726081E+06 .592198E+03 .000000E+00  
 6 .726540E+06 -.592198E+03 .000000E+00  
 7 .621804E+06 -.592197E+03 .000000E+00  
 8 .444146E+06 -.592197E+03 .000000E+00  
 9 .266487E+06 -.592197E+03 .000000E+00  
 10 .888291E+05 -.592197E+03 .000000E+00  
 0 ITERATION NUMBER= 5  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .429344E+04  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.592205E+03 .249185E-01 .000000E+00  
 2 .749085E+01 .000000E+00 .245316E-01 .000000E+00  
 3 .147496E+02 .000000E+00 .233710E-01 .000000E+00  
 4 .215440E+02 .000000E+00 .214366E-01 .000000E+00  
 5 .276421E+02 .000000E+00 .187284E-01 .000000E+00  
 6 .305200E+02 .000000E+00 -.316307E-04 .000000E+00  
 7 .276337E+02 .000000E+00 -.187214E-01 .000000E+00  
 8 .215377E+02 .000000E+00 -.214296E-01 .000000E+00

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9 .147453E+02 .000000E+00 -.233639E-01 .000000E+00
10 .748874E+01 .000000E+00 -.245246E-01 .000000E+00
11 .000000E+00 -.592200E+03 -.249114E-01 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .888609E+05 .592317E+03 .000000E+00
2 .266583E+06 .592317E+03 .000000E+00
3 .444305E+06 .592310E+03 .000000E+00
4 .622027E+06 .592312E+03 .000000E+00
5 .843750E+06 .592255E+03 .000000E+00
6 .843750E+06 -.592270E+03 .000000E+00
7 .622024E+06 -.592308E+03 .000000E+00
8 .444303E+06 -.592317E+03 .000000E+00
9 .266581E+06 -.592308E+03 .000000E+00
10 .888601E+05 -.592312E+03 .000000E+00
0 ITERATION NUMBER= 6
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .898786E+03
0 NODE DISPL. REACTION DISPL. REACTION
1 .000000E+00 -.593061E+03 .187375E+01 .000000E+00
2 .562139E+03 .000000E+00 .187334E+01 .000000E+00
3 .112403E+04 .000000E+00 .187211E+01 .000000E+00
4 .168543E+04 .000000E+00 .187007E+01 .000000E+00
5 .224610E+04 .000000E+00 .186720E+01 .000000E+00
6 .252372E+04 .000000E+00 -.168719E-01 .000000E+00
7 .224160E+04 .000000E+00 -.186345E+01 .000000E+00
8 .168206E+04 .000000E+00 -.186632E+01 .000000E+00
9 .112178E+04 .000000E+00 -.186836E+01 .000000E+00
10 .561014E+03 .000000E+00 -.186959E+01 .000000E+00
11 .000000E+00 -.592758E+03 -.187000E+01 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .939812E+05 .611537E+03 .000000E+00
2 .281916E+06 .611955E+03 .000000E+00
3 .469851E+06 .611161E+03 .000000E+00
4 .656689E+06 .611141E+03 .000000E+00
5 .843750E+06 .601170E+03 .000000E+00
6 .843750E+06 -.600514E+03 .000000E+00
7 .656673E+06 -.611422E+03 .000000E+00
8 .469849E+06 -.611741E+03 .000000E+00
9 .281832E+06 -.610982E+03 .000000E+00
10 .939256E+05 -.611289E+03 .000000E+00
0 ITERATION NUMBER= 7
0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .942732E+03
0 NODE DISPL. REACTION DISPL. REACTION
1 .000000E+00 -.594414E+03 .357820E+01 .000000E+00
2 .107347E+04 .000000E+00 .357779E+01 .000000E+00
3 .214670E+04 .000000E+00 .357657E+01 .000000E+00
4 .321944E+04 .000000E+00 .357453E+01 .000000E+00
5 .429144E+04 .000000E+00 .357165E+01 .000000E+00
6 .482696E+04 .000000E+00 -.205089E-02 .000000E+00
7 .429090E+04 .000000E+00 -.357120E+01 .000000E+00
8 .321903E+04 .000000E+00 -.357407E+01 .000000E+00
9 .214643E+04 .000000E+00 -.357611E+01 .000000E+00
10 .107334E+04 .000000E+00 -.357733E+01 .000000E+00
11 .000000E+00 -.593303E+03 -.357774E+01 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .937621E+05 .611518E+03 .000000E+00
2 .281122E+06 .610536E+03 .000000E+00
3 .468510E+06 .610801E+03 .000000E+00
4 .657174E+06 .610687E+03 .000000E+00
5 .843750E+06 .600417E+03 .000000E+00
6 .843750E+06 -.601277E+03 .000000E+00

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7 .656931E+06 -.610007E+03 .000000E+00  
 8 .468233E+06 -.611123E+03 .000000E+00  
 9 .280847E+06 -.610281E+03 .000000E+00  
 10 .936518E+05 -.610331E+03 .000000E+00  
 0 ITERATION NUMBER= 8  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .940630E+03  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.593603E+03 .528265E+01 .000000E+00  
 2 .158481E+04 .000000E+00 .528224E+01 .000000E+00  
 3 .316937E+04 .000000E+00 .528102E+01 .000000E+00  
 4 .475345E+04 .000000E+00 .527898E+01 .000000E+00  
 5 .633679E+04 .000000E+00 .527611E+01 .000000E+00  
 6 .713019E+04 .000000E+00 .127737E-01 .000000E+00  
 7 .634019E+04 .000000E+00 -.527895E+01 .000000E+00  
 8 .475600E+04 .000000E+00 -.528182E+01 .000000E+00  
 9 .317108E+04 .000000E+00 -.528385E+01 .000000E+00  
 10 .158566E+04 .000000E+00 -.528508E+01 .000000E+00  
 11 .000000E+00 -.593303E+03 -.528549E+01 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .937621E+05 .610752E+03 .000000E+00  
 2 .281122E+06 .610755E+03 .000000E+00  
 3 .468537E+06 .611658E+03 .000000E+00  
 4 .657147E+06 .610558E+03 .000000E+00  
 5 .843750E+06 .601274E+03 .000000E+00  
 6 .843750E+06 -.599763E+03 .000000E+00  
 7 .656903E+06 -.610098E+03 .000000E+00  
 8 .468233E+06 -.610372E+03 .000000E+00  
 9 .280874E+06 -.611357E+03 .000000E+00  
 10 .936244E+05 -.610421E+03 .000000E+00  
 0 ITERATION NUMBER= 9  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .947162E+03  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.593542E+03 .698710E+01 .000000E+00  
 2 .209614E+04 .000000E+00 .698669E+01 .000000E+00  
 3 .419204E+04 .000000E+00 .698547E+01 .000000E+00  
 4 .628745E+04 .000000E+00 .698343E+01 .000000E+00  
 5 .838213E+04 .000000E+00 .698056E+01 .000000E+00  
 6 .943343E+04 .000000E+00 .276080E-01 .000000E+00  
 7 .838949E+04 .000000E+00 -.698670E+01 .000000E+00  
 8 .629297E+04 .000000E+00 -.698956E+01 .000000E+00  
 9 .419572E+04 .000000E+00 -.699160E+01 .000000E+00  
 10 .209798E+04 .000000E+00 -.699283E+01 .000000E+00  
 11 .000000E+00 -.593303E+03 -.699323E+01 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .936800E+05 .610665E+03 .000000E+00  
 2 .281150E+06 .610873E+03 .000000E+00  
 3 .468537E+06 .610687E+03 .000000E+00  
 4 .657205E+06 .610310E+03 .000000E+00  
 5 .843750E+06 .600223E+03 .000000E+00  
 6 .843750E+06 -.600710E+03 .000000E+00  
 7 .656946E+06 -.610955E+03 .000000E+00  
 8 .468233E+06 -.610795E+03 .000000E+00  
 9 .280874E+06 -.610302E+03 .000000E+00  
 10 .936244E+05 -.610352E+03 .000000E+00  
 0 ITERATION NUMBER= 10  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .961740E+03  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.593975E+03 .869155E+01 .000000E+00  
 2 .260748E+04 .000000E+00 .869114E+01 .000000E+00  
 3 .521471E+04 .000000E+00 .868992E+01 .000000E+00

	STRESSES	PL STRAIN		
4	.782146E+04	.000000E+00	.868788E+01	
5	.104275E+05	.000000E+00	.868501E+01	
6	.117367E+05	.000000E+00	.424508E-01	
7	.104388E+05	.000000E+00	-.869444E+01	
8	.782995E+04	.000000E+00	-.869731E+01	
9	.522037E+04	.000000E+00	-.869935E+01	
10	.261031E+04	.000000E+00	-.870057E+01	
11	.000000E+00	-.593303E+03	-.870098E+01	
0 ELEMENT	STRESSES	PL STRAIN		
1	.937621E+05	.611010E+03	.000000E+00	
2	.281204E+06	.610953E+03	.000000E+00	
3	.468592E+06	.609867E+03	.000000E+00	
4	.657068E+06	.610042E+03	.000000E+00	
5	.843750E+06	.601287E+03	.000000E+00	
6	.843750E+06	-.599279E+03	.000000E+00	
7	.656892E+06	-.610512E+03	.000000E+00	
8	.468233E+06	-.609655E+03	.000000E+00	
9	.280874E+06	-.610641E+03	.000000E+00	
10	.936518E+05	-.610546E+03	.000000E+00	
0 ITERATION NUMBER=	11			
0 CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.946988E+03	
0 NODE	DISPL.	REACTION	DISPL.	REACTION
1	.000000E+00	-.593858E+03	.103960E+02	.000000E+00
2	.311881E+04	.000000E+00	.103956E+02	.000000E+00
3	.623738E+04	.000000E+00	.103944E+02	.000000E+00
4	.935546E+04	.000000E+00	.103923E+02	.000000E+00
5	.124728E+05	.000000E+00	.103895E+02	.000000E+00
6	.140399E+05	.000000E+00	.572994E-01	.000000E+00
7	.124881E+05	.000000E+00	-.104022E+02	.000000E+00
8	.936692E+04	.000000E+00	-.104051E+02	.000000E+00
9	.624502E+04	.000000E+00	-.104071E+02	.000000E+00
10	.312263E+04	.000000E+00	-.104083E+02	.000000E+00
11	.000000E+00	-.593303E+03	-.104087E+02	.000000E+00
0 ELEMENT	STRESSES	PL STRAIN		
1	.937347E+05	.611058E+03	.000000E+00	
2	.281150E+06	.610568E+03	.000000E+00	
3	.468537E+06	.611122E+03	.000000E+00	
4	.657260E+06	.610277E+03	.000000E+00	
5	.843750E+06	.601372E+03	.000000E+00	
6	.843750E+06	-.601036E+03	.000000E+00	
7	.656970E+06	-.610521E+03	.000000E+00	
8	.468233E+06	-.609929E+03	.000000E+00	
9	.280874E+06	-.610421E+03	.000000E+00	
10	.936244E+05	-.610471E+03	.000000E+00	
0 ITERATION NUMBER=	12			
0 CONVERGENCE CODE=	1	NORM OF RESIDUAL SUM RATIO=	.940865E+03	
0 NODE	DISPL.	REACTION	DISPL.	REACTION
1	.000000E+00	-.593909E+03	.121005E+02	.000000E+00
2	.363015E+04	.000000E+00	.121000E+02	.000000E+00
3	.726006E+04	.000000E+00	.120988E+02	.000000E+00
4	.108895E+05	.000000E+00	.120968E+02	.000000E+00
5	.145182E+05	.000000E+00	.120939E+02	.000000E+00
6	.163431E+05	.000000E+00	.721170E-01	.000000E+00
7	.145374E+05	.000000E+00	-.121099E+02	.000000E+00
8	.109039E+05	.000000E+00	-.121128E+02	.000000E+00
9	.726967E+04	.000000E+00	-.121148E+02	.000000E+00
10	.363496E+04	.000000E+00	-.121161E+02	.000000E+00
11	.000000E+00	-.593303E+03	-.121165E+02	.000000E+00
0 ELEMENT	STRESSES	PL STRAIN		
1	.937074E+05	.611067E+03	.000000E+00	

2 .281095E+06 .611131E+03 .000000E+00  
 3 .468537E+06 .610410E+03 .000000E+00  
 4 .656932E+06 .610789E+03 .000000E+00  
 5 .843750E+06 .600913E+03 .000000E+00  
 6 .843750E+06 -.601097E+03 .000000E+00  
 7 .656833E+06 -.610681E+03 .000000E+00  
 8 .468233E+06 -.609825E+03 .000000E+00  
 9 .280874E+06 -.610810E+03 .000000E+00  
 10 .936518E+05 -.610716E+03 .000000E+00  
 0 ITERATION NUMBER= 13  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .969131E+03  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.593943E+03 .138049E+02 .000000E+00  
 2 .414149E+04 .000000E+00 .138045E+02 .000000E+00  
 3 .828273E+04 .000000E+00 .138033E+02 .000000E+00  
 4 .124235E+05 .000000E+00 .138012E+02 .000000E+00  
 5 .165635E+05 .000000E+00 .137984E+02 .000000E+00  
 6 .186464E+05 .000000E+00 .869437E-01 .000000E+00  
 7 .165867E+05 .000000E+00 -.138177E+02 .000000E+00  
 8 .124409E+05 .000000E+00 -.138206E+02 .000000E+00  
 9 .829432E+04 .000000E+00 -.138226E+02 .000000E+00  
 10 .414728E+04 .000000E+00 -.138238E+02 .000000E+00  
 11 .000000E+00 -.593303E+03 -.138242E+02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .937347E+05 .611050E+03 .000000E+00  
 2 .281122E+06 .610909E+03 .000000E+00  
 3 .468592E+06 .610375E+03 .000000E+00  
 4 .657409E+06 .609605E+03 .000000E+00  
 5 .843750E+06 .601023E+03 .000000E+00  
 6 .843750E+06 -.599180E+03 .000000E+00  
 7 .657032E+06 -.609786E+03 .000000E+00  
 8 .468233E+06 -.610010E+03 .000000E+00  
 9 .280874E+06 -.610502E+03 .000000E+00  
 10 .936244E+05 -.610552E+03 .000000E+00  
 0 ITERATION NUMBER= 14  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .939722E+03  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.593979E+03 .155094E+02 .000000E+00  
 2 .465282E+04 .000000E+00 .155089E+02 .000000E+00  
 3 .930540E+04 .000000E+00 .155077E+02 .000000E+00  
 4 .139575E+05 .000000E+00 .155057E+02 .000000E+00  
 5 .186088E+05 .000000E+00 .155028E+02 .000000E+00  
 6 .209496E+05 .000000E+00 .101773E+00 .000000E+00  
 7 .186360E+05 .000000E+00 -.155254E+02 .000000E+00  
 8 .139778E+05 .000000E+00 -.155283E+02 .000000E+00  
 9 .931896E+04 .000000E+00 -.155303E+02 .000000E+00  
 10 .465960E+04 .000000E+00 -.155316E+02 .000000E+00  
 11 .000000E+00 -.593303E+03 -.155320E+02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .937074E+05 .611133E+03 .000000E+00  
 2 .281122E+06 .610848E+03 .000000E+00  
 3 .468565E+06 .609923E+03 .000000E+00  
 4 .656587E+06 .611084E+03 .000000E+00  
 5 .843750E+06 .600853E+03 .000000E+00  
 6 .843750E+06 -.600371E+03 .000000E+00  
 7 .656676E+06 -.610643E+03 .000000E+00  
 8 .468206E+06 -.610917E+03 .000000E+00  
 9 .280847E+06 -.610712E+03 .000000E+00  
 10 .936518E+05 -.610762E+03 .000000E+00  
 0 ITERATION NUMBER= 15

0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .945441E+03  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.594327E+03 .172138E+02 .000000E+00  
 2 .516416E+04 .000000E+00 .172134E+02 .000000E+00  
 3 .103281E+05 .000000E+00 .172122E+02 .000000E+00  
 4 .154915E+05 .000000E+00 .172101E+02 .000000E+00  
 5 .206542E+05 .000000E+00 .172073E+02 .000000E+00  
 6 .232528E+05 .000000E+00 .116604E+00 .000000E+00  
 7 .206853E+05 .000000E+00 -.172332E+02 .000000E+00  
 8 .155148E+05 .000000E+00 -.172360E+02 .000000E+00  
 9 .103436E+05 .000000E+00 -.172381E+02 .000000E+00  
 10 .517193E+04 .000000E+00 -.172393E+02 .000000E+00  
 11 .000000E+00 -.593303E+03 -.172397E+02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .937895E+05 .611381E+03 .000000E+00  
 2 .281150E+06 .610688E+03 .000000E+00  
 3 .468510E+06 .610604E+03 .000000E+00  
 4 .657753E+06 .611319E+03 .000000E+00  
 5 .843750E+06 .601806E+03 .000000E+00  
 6 .843750E+06 -.601775E+03 .000000E+00  
 7 .657189E+06 -.609528E+03 .000000E+00  
 8 .468233E+06 -.609821E+03 .000000E+00  
 9 .280874E+06 -.610806E+03 .000000E+00  
 10 .936518E+05 -.610712E+03 .000000E+00  
 0 ITERATION NUMBER= 16  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .943476E+03  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.594268E+03 .189183E+02 .000000E+00  
 2 .567549E+04 .000000E+00 .189179E+02 .000000E+00  
 3 .113507E+05 .000000E+00 .189166E+02 .000000E+00  
 4 .170255E+05 .000000E+00 .189146E+02 .000000E+00  
 5 .226995E+05 .000000E+00 .189117E+02 .000000E+00  
 6 .255561E+05 .000000E+00 .131438E+00 .000000E+00  
 7 .227346E+05 .000000E+00 -.189409E+02 .000000E+00  
 8 .170518E+05 .000000E+00 -.189438E+02 .000000E+00  
 9 .113683E+05 .000000E+00 -.189458E+02 .000000E+00  
 10 .568425E+04 .000000E+00 -.189471E+02 .000000E+00  
 11 .000000E+00 -.593303E+03 -.189475E+02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
 1 .937347E+05 .611454E+03 .000000E+00  
 2 .281095E+06 .610676E+03 .000000E+00  
 3 .468537E+06 .610695E+03 .000000E+00  
 4 .655754E+06 .610870E+03 .000000E+00  
 5 .843750E+06 .601573E+03 .000000E+00  
 6 .843750E+06 -.601673E+03 .000000E+00  
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 8 .468233E+06 -.610245E+03 .000000E+00  
 9 .280874E+06 -.610737E+03 .000000E+00  
 10 .936244E+05 -.610787E+03 .000000E+00  
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 2 .618683E+04 .000000E+00 .206223E+02 .000000E+00  
 3 .123734E+05 .000000E+00 .206211E+02 .000000E+00  
 4 .185595E+05 .000000E+00 .206190E+02 .000000E+00  
 5 .247449E+05 .000000E+00 .206161E+02 .000000E+00  
 6 .278593E+05 .000000E+00 .146275E+00 .000000E+00  
 7 .247839E+05 .000000E+00 -.206487E+02 .000000E+00  
 8 .185888E+05 .000000E+00 -.206515E+02 .000000E+00

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9 .123929E+05 .000000E+00 -.206536E+02 .000000E+00
10 .619658E+04 .000000E+00 -.206548E+02 .000000E+00
11 .000000E+00 -.593303E+03 -.206552E+02 .000000E+00
0 ELEMENT STRESSES PL STRAIN
1 .937621E+05 .611040E+03 .000000E+00
2 .281122E+06 .611044E+03 .000000E+00
3 .468537E+06 .610714E+03 .000000E+00
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5 .843750E+06 .600594E+03 .000000E+00
6 .843750E+06 -.599236E+03 .000000E+00
7 .657596E+06 -.610306E+03 .000000E+00
8 .468233E+06 -.609991E+03 .000000E+00
9 .280874E+06 -.610483E+03 .000000E+00
10 .936518E+05 -.610388E+03 .000000E+00
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1 .000000E+00 -.593683E+03 .223272E+02 .000000E+00
2 .669816E+04 .000000E+00 .223268E+02 .000000E+00
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4 .200935E+05 .000000E+00 .223235E+02 .000000E+00
5 .267902E+05 .000000E+00 .223206E+02 .000000E+00
6 .301625E+05 .000000E+00 .161103E+00 .000000E+00
7 .268332E+05 .000000E+00 -.223564E+02 .000000E+00
8 .201257E+05 .000000E+00 -.223593E+02 .000000E+00
9 .134176E+05 .000000E+00 -.223613E+02 .000000E+00
10 .670890E+04 .000000E+00 -.223626E+02 .000000E+00
11 .000000E+00 -.593303E+03 -.223630E+02 .000000E+00
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1 .936800E+05 .610730E+03 .000000E+00
2 .281177E+06 .611083E+03 .000000E+00
3 .468537E+06 .611288E+03 .000000E+00
4 .653575E+06 .609840E+03 .000000E+00
5 .843750E+06 .600900E+03 .000000E+00
6 .843750E+06 -.600738E+03 .000000E+00
7 .655268E+06 -.608771E+03 .000000E+00
8 .468233E+06 -.609887E+03 .000000E+00
9 .280874E+06 -.611365E+03 .000000E+00
10 .936244E+05 -.610429E+03 .000000E+00
0 ITERATION NUMBER= 19
0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .102590E+04
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1 .000000E+00 -.593985E+03 .240316E+02 .000000E+00
2 .720950E+04 .000000E+00 .240312E+02 .000000E+00
3 .144188E+05 .000000E+00 .240300E+02 .000000E+00
4 .216275E+05 .000000E+00 .240280E+02 .000000E+00
5 .288356E+05 .000000E+00 .240250E+02 .000000E+00
6 .324658E+05 .000000E+00 .175940E+00 .000000E+00
7 .288825E+05 .000000E+00 -.240642E+02 .000000E+00
8 .216627E+05 .000000E+00 -.240670E+02 .000000E+00
9 .144422E+05 .000000E+00 -.240691E+02 .000000E+00
10 .722123E+04 .000000E+00 -.240703E+02 .000000E+00
11 .000000E+00 -.593303E+03 -.240707E+02 .000000E+00
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2 .281122E+06 .610543E+03 .000000E+00
3 .468592E+06 .610995E+03 .000000E+00
4 .660773E+06 .609720E+03 .000000E+00
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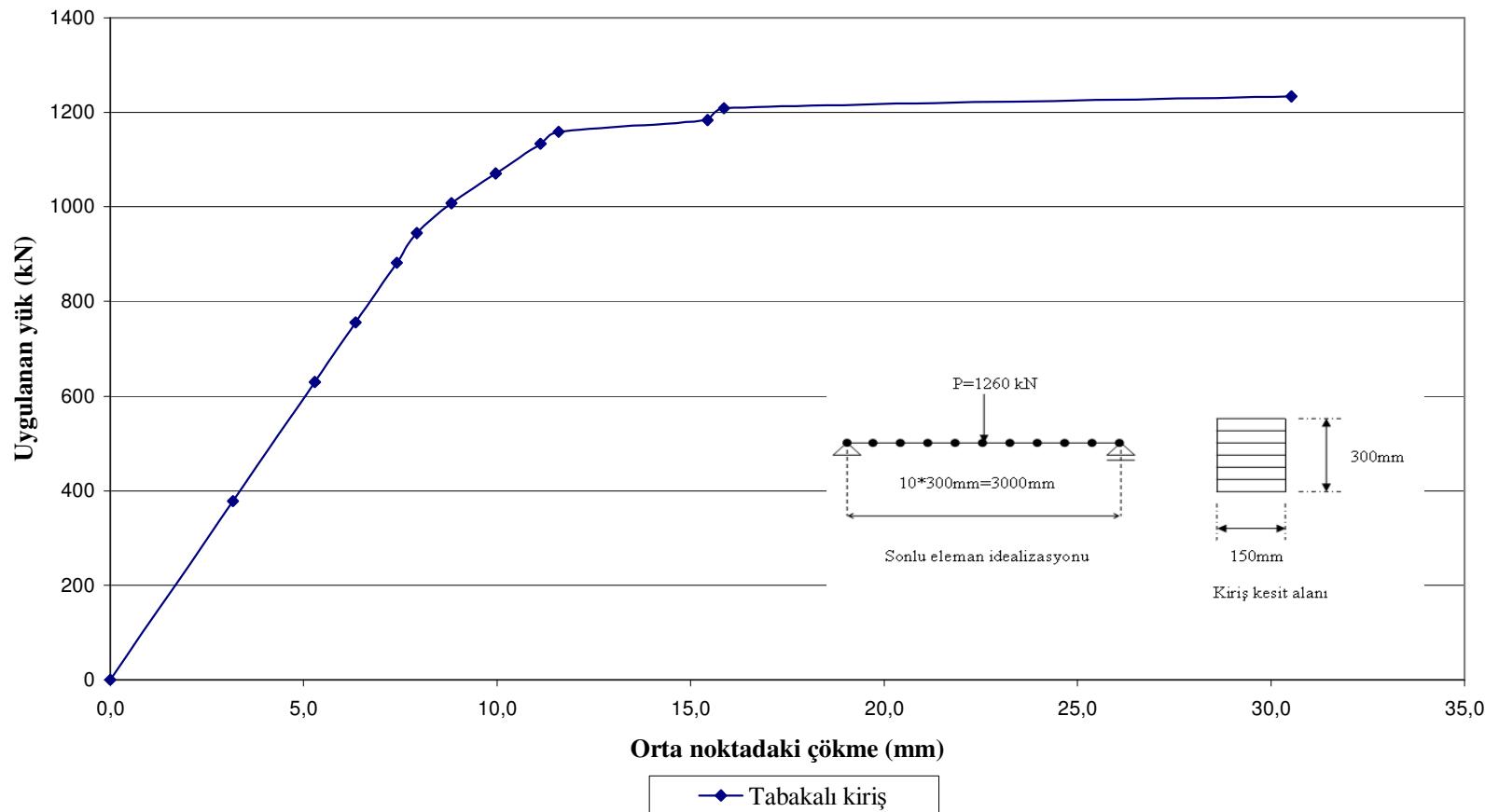
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 7 .652765E+06 -.609637E+03 .000000E+00  
 8 .468206E+06 -.610898E+03 .000000E+00  
 9 .280847E+06 -.610200E+03 .000000E+00  
 10 .936518E+05 -.610250E+03 .000000E+00  
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 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .138270E+04  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.594054E+03 .274405E+02 .000000E+00  
 2 .823218E+04 .000000E+00 .274401E+02 .000000E+00  
 3 .164641E+05 .000000E+00 .274389E+02 .000000E+00  
 4 .246956E+05 .000000E+00 .274369E+02 .000000E+00  
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 8 .247367E+05 .000000E+00 -.274825E+02 .000000E+00  
 9 .164915E+05 .000000E+00 -.274846E+02 .000000E+00  
 10 .824588E+04 .000000E+00 -.274858E+02 .000000E+00  
 11 .000000E+00 -.593303E+03 -.274862E+02 .000000E+00  
 0 ELEMENT STRESSES PL STRAIN  
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 2 .281204E+06 .610622E+03 .000000E+00  
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 5 .843750E+06 .599732E+03 .000000E+00  
 6 .843750E+06 -.600335E+03 .000000E+00  
 7 .661093E+06 -.610076E+03 .000000E+00  
 8 .468233E+06 -.610276E+03 .000000E+00  
 9 .280874E+06 -.610768E+03 .000000E+00  
 10 .936518E+05 -.610673E+03 .000000E+00  
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 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .257394E+04  
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 2 .874350E+04 .000000E+00 .291446E+02 .000000E+00  
 3 .174868E+05 .000000E+00 .291433E+02 .000000E+00

4	.262295E+05	.000000E+00	.291413E+02	.000000E+00	
5	.349716E+05	.000000E+00	.291384E+02	.000000E+00	
6	.393755E+05	.000000E+00	.220430E+00	.000000E+00	
7	.350304E+05	.000000E+00	-.291874E+02	.000000E+00	
8	.262736E+05	.000000E+00	-.291903E+02	.000000E+00	
9	.175162E+05	.000000E+00	-.291923E+02	.000000E+00	
10	.875820E+04	.000000E+00	-.291935E+02	.000000E+00	
11	.000000E+00	-.593303E+03	-.291939E+02	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.936800E+05	.611008E+03	.000000E+00		
2	.281150E+06	.611215E+03	.000000E+00		
3	.468537E+06	.610537E+03	.000000E+00		
4	.634632E+06	.609726E+03	.000000E+00		
5	.843750E+06	.600396E+03	.000000E+00		
6	.843750E+06	-.600143E+03	.000000E+00		
7	.646526E+06	-.609499E+03	.000000E+00		
8	.468206E+06	-.611745E+03	.000000E+00		
9	.280847E+06	-.610554E+03	.000000E+00		
10	.936518E+05	-.610604E+03	.000000E+00		
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1	.000000E+00	-.594224E+03	.308495E+02	.000000E+00	
2	.925486E+04	.000000E+00	.308491E+02	.000000E+00	
3	.185095E+05	.000000E+00	.308479E+02	.000000E+00	
4	.277636E+05	.000000E+00	.308458E+02	.000000E+00	
5	.370169E+05	.000000E+00	.308426E+02	.000000E+00	
6	.416787E+05	.000000E+00	.235343E+00	.000000E+00	
7	.370797E+05	.000000E+00	-.308950E+02	.000000E+00	
8	.278106E+05	.000000E+00	-.308981E+02	.000000E+00	
9	.185408E+05	.000000E+00	-.309001E+02	.000000E+00	
10	.927054E+04	.000000E+00	-.309013E+02	.000000E+00	
11	.000000E+00	-.593303E+03	-.309017E+02	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.937347E+05	.611254E+03	.000000E+00		
2	.281150E+06	.610272E+03	.000000E+00		
3	.468565E+06	.610477E+03	.000000E+00		
4	.679720E+06	.610818E+03	.000000E+00		
5	.843750E+06	.600044E+03	.000000E+00		
6	.843750E+06	-.600261E+03	.000000E+00		
7	.667335E+06	-.609079E+03	.000000E+00		
8	.468206E+06	-.610512E+03	.000000E+00		
9	.280847E+06	-.610308E+03	.000000E+00		
10	.936518E+05	-.610358E+03	.000000E+00		
0	ITERATION NUMBER=	24			
0	CONVERGENCE CODE=	999	NORM OF RESIDUAL SUM RATIO=	.609336E+04	
0	NODE	DISPL.	REACTION	DISPL.	REACTION
1	.000000E+00	-.593804E+03	.325539E+02	.000000E+00	
2	.976618E+04	.000000E+00	.325535E+02	.000000E+00	
3	.195321E+05	.000000E+00	.325522E+02	.000000E+00	
4	.292975E+05	.000000E+00	.325502E+02	.000000E+00	
5	.390623E+05	.000000E+00	.325473E+02	.000000E+00	
6	.439819E+05	.000000E+00	.250097E+00	.000000E+00	
7	.391289E+05	.000000E+00	-.326029E+02	.000000E+00	
8	.293476E+05	.000000E+00	-.326058E+02	.000000E+00	
9	.195655E+05	.000000E+00	-.326078E+02	.000000E+00	
10	.978285E+04	.000000E+00	-.326090E+02	.000000E+00	
11	.000000E+00	-.593303E+03	-.326094E+02	.000000E+00	
0	ELEMENT	STRESSES	PL STRAIN		
1	.937347E+05	.610911E+03	.000000E+00		

2 .281232E+06 .610855E+03 .000000E+00  
 3 .468565E+06 .610508E+03 .000000E+00  
 4 .600781E+06 .610046E+03 .000000E+00  
 5 .843750E+06 .600602E+03 .000000E+00  
 6 .843750E+06 -.600784E+03 .000000E+00  
 7 .630919E+06 -.609191E+03 .000000E+00  
 8 .468233E+06 -.610306E+03 .000000E+00  
 9 .280874E+06 -.610306E+03 .000000E+00  
 10 .936518E+05 -.610211E+03 .000000E+00  
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 2 .102776E+05 .000000E+00 .342581E+02 .000000E+00  
 3 .205549E+05 .000000E+00 .342568E+02 .000000E+00  
 4 .308317E+05 .000000E+00 .342548E+02 .000000E+00  
 5 .411077E+05 .000000E+00 .342511E+02 .000000E+00  
 6 .462852E+05 .000000E+00 .265129E+00 .000000E+00  
 7 .411783E+05 .000000E+00 -.343104E+02 .000000E+00  
 8 .308846E+05 .000000E+00 -.343136E+02 .000000E+00  
 9 .205902E+05 .000000E+00 -.343157E+02 .000000E+00  
 10 .102952E+05 .000000E+00 -.343169E+02 .000000E+00  
 11 .000000E+00 -.593303E+03 -.343173E+02 .000000E+00  
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 1 .937347E+05 .611062E+03 .000000E+00  
 2 .281122E+06 .610428E+03 .000000E+00  
 3 .468537E+06 .610591E+03 .000000E+00  
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 5 .843750E+06 .600072E+03 .000000E+00  
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 9 .280874E+06 -.610552E+03 .000000E+00  
 10 .936518E+05 -.610458E+03 .000000E+00  
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 2 .107888E+05 .000000E+00 .359624E+02 .000000E+00  
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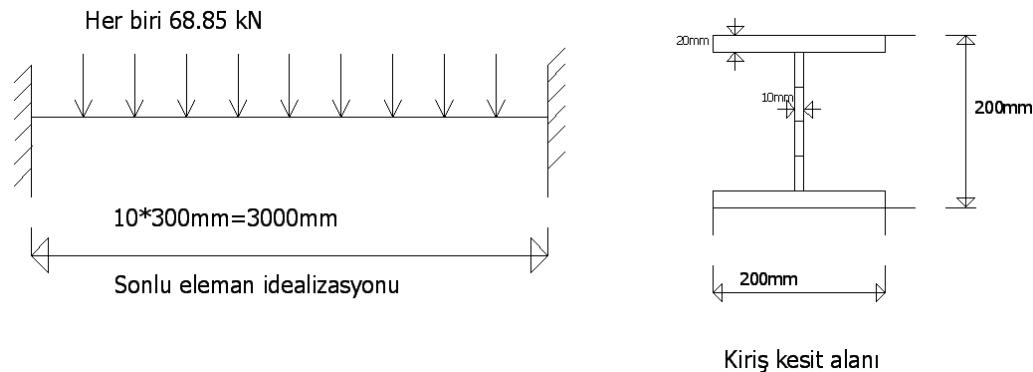
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 1 .000000E+00 -.594413E+03 .413696E+02 .000000E+00  
 2 .124109E+05 .000000E+00 .413692E+02 .000000E+00  
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 7 .495694E+05 .000000E+00 -.413011E+02 .000000E+00  
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9	.247858E+05	.000000E+00	-.413085E+02	.000000E+00
10	.123930E+05	.000000E+00	-.413097E+02	.000000E+00
11	.000000E+00	-.591804E+03	-.413101E+02	.000000E+00
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1	.943645E+05	.613621E+03	.000000E+00	
2	.283094E+06	.612904E+03	.000000E+00	
3	.471823E+06	.613684E+03	.000000E+00	
4	.140948E+09	.609455E+03	.000000E+00	
5	.843750E+06	.599533E+03	.000000E+00	
6	.843750E+06	-.599496E+03	.000000E+00	
7	.785143E+06	-.611887E+03	.000000E+00	
8	.468480E+06	-.609892E+03	.000000E+00	
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10	.936518E+05	-.609722E+03	.000000E+00	
0 ITERATION NUMBER=	30			
0 CONVERGENCE CODE=	999	NORM OF RESIDUAL SUM RATIO=	.103968E+12	
0 NODE	DISPL.	REACTION	DISPL.	REACTION
1	.000000E+00	-.207091E+05	.128723E+05	.000000E+00
2	.386169E+07	.000000E+00	.128721E+05	.000000E+00
3	.772328E+07	.000000E+00	.128717E+05	.000000E+00
4	.115847E+08	.000000E+00	.128708E+05	.000000E+00
5	.392777E+07	.000000E+00	-.639166E+05	.000000E+00
6	-.782481E+06	.000000E+00	.325150E+05	.000000E+00
7	.364067E+07	.000000E+00	-.302748E+04	.000000E+00
8	.273135E+07	.000000E+00	-.303465E+04	.000000E+00
9	.182093E+07	.000000E+00	-.303480E+04	.000000E+00
10	.910474E+06	.000000E+00	-.303489E+04	.000000E+00
11	.000000E+00	.842968E+04	-.303492E+04	.000000E+00
0 ELEMENT	STRESSES	PL STRAIN		
1	.843749E+06	.149673E+06	-.677470E-01	
2	.843750E+06	.147007E+06	-.401720E-01	
3	.843753E+06	.149752E+06	-.125970E-01	
4	.140948E+09	-.235703E+06	.125970E-01	
5	-.164605E+14	-.145952E+06	.401720E-01	
6	.843750E+06	.159207E+06	.677470E-01	
7	.843749E+06	-.211275E+05	-.206029E+00	
8	.843750E+06	-.222574E+05	-.123141E+00	
9	.843750E+06	-.223716E+05	-.402534E-01	
10	.843750E+06	-.218629E+05	.402534E-01	



Şekil 5.11: Tekil yüklü tabakalı kırış örneği

### 5.2.2 Uniform yayılı yüklü tabakalı Timoshenko kırışı örneği



**Şekil 5.12:** Tabakalı Timoshenko kırışında uniform yayılı yük hali.

Şekil 5.12'te görüldüğü gibi kiriş kesitinde 10mm kalınlığındaki kısım 4'e bölünmüştür.

**Probleme ait bilgilerin programa giriş listesi;**

11	10	2	1	17	2	14	2	2	6
1									
210.	53.846		0.25		0.				
200.	200.		20.		10.				
40.	10.		40.		10.				
40.	10.		40.		10.				
40.									
1	1	2	1						
2	2	3	1						
3	3	4	1						
4	4	5	1						
5	5	6	1						
6	6	7	1						
7	7	8	1						

8	8	9	1		
9	9	10	1		
10	10	11	1		
	1		0.		
	2		300.		
	3		600.		
	4		900.		
	5		1200.		
	6		1500.		
	7		1800.		
	8		2100.		
	9		2400.		
	10		2700.		
	11		3000.		
	1	1	0.	1	0.
	11	1	0.	1	0.
	1	68.85	0.	68.85	0.
	2	68.85	0.	68.85	0.
	3	68.85	0.	68.85	0.
	4	68.85	0.	68.85	0.
	5	68.85	0.	68.85	0.
	6	68.85	0.	68.85	0.
	7	68.85	0.	68.85	0.
	8	68.85	0.	68.85	0.
	9	68.85	0.	68.85	0.
	10	68.85	0.	68.85	0.
100	2	0.30	0.5		
100	2	0.20	0.5		
100	2	0.10	0.5		
100	2	0.10	0.5		
100	2	0.05	0.5		
100	2	0.05	0.5		
100	2	0.05	0.5		
100	2	0.05	0.5		

100	2	0.02	0.5
100	2	0.02	0.5
100	2	0.02	0.5
100	2	0.02	0.5
100	2	0.01	0.5
100	2	0.01	0.5

**Veri girişi sonrası alınan sonuçlar;**

```

NPOIN= 11 NELEM= 10 NBOUN= 2 NMATS= 1
NPROP= 17 NNODE= 2 NINCS= 14 NALGO= 2
NDOFN= 2 NLAYR= 6
0 MATERIAL PROPERTIES
    1
    210.00000 53.84600 .25000 .00000
    200.00000 200.00000 20.00000 10.00000
    40.00000 10.00000 40.00000 10.00000
    40.00000 10.00000 40.00000 10.00000
    40.00000
0 EL NODES MAT.
    1 1 2 1
    2 2 3 1
    3 3 4 1
    4 4 5 1
    5 5 6 1
    6 6 7 1
    7 7 8 1
    8 8 9 1
    9 9 10 1
    10 10 11 1
0 NODE COORD.
    1 .00000
    2 300.00000
    3 600.00000
    4 900.00000
    5 1200.00000
    6 1500.00000
    7 1800.00000
    8 2100.00000
    9 2400.00000
    10 2700.00000
    11 3000.00000
0 RES.NODE CODE PRES.VALUES CODE PRES.VALUES
    1 1 .00000 1 .00000
    11 1 .00000 1 .00000
0 ELEMENT NODAL LOADS
    1 68.85000 .00000 68.85000 .00000
    2 68.85000 .00000 68.85000 .00000
    3 68.85000 .00000 68.85000 .00000
    4 68.85000 .00000 68.85000 .00000
    5 68.85000 .00000 68.85000 .00000
    6 68.85000 .00000 68.85000 .00000

```

```

7   68.85000   .00000   68.85000   .00000
8   68.85000   .00000   68.85000   .00000
9   68.85000   .00000   68.85000   .00000
10  68.85000   .00000   68.85000   .00000
0 IINCS= 1 NITER= 100 NOUTP= 2 FACTO= .300000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .961086E-04
0 NODE  DISPL.      REACTION    DISPL.      REACTION
1 .000000E+00   -.206550E+03  .000000E+00   -.102242E+06
2 .574987E+00   .000000E+00   .268247E-02   .000000E+00
3 .164811E+01   .000000E+00   .357662E-02   .000000E+00
4 .274993E+01   .000000E+00   .312954E-02   .000000E+00
5 .354515E+01   .000000E+00   .178831E-02   .000000E+00
6 .383257E+01   .000000E+00   .872816E-09   .000000E+00
7 .354515E+01   .000000E+00   -.178831E-02   .000000E+00
8 .274993E+01   .000000E+00   -.312954E-02   .000000E+00
9 .164811E+01   .000000E+00   -.357662E-02   .000000E+00
10 .574987E+00   .000000E+00   -.268247E-02   .000000E+00
11 .000000E+00   -.206550E+03  .000000E+00   .102242E+06
0 ELEMENT  STRESSES     PL STRAIN
1 -.743579E+05   .185895E+03  .000000E+00
2 -.247860E+05   .144585E+03  .000000E+00
3 .123930E+05   .103275E+03  .000000E+00
4 .371790E+05   .619650E+02  .000000E+00
5 .495720E+05   .206554E+02  .000000E+00
6 .495720E+05   -.206548E+02  .000000E+00
7 .371790E+05   -.619649E+02  .000000E+00
8 .123930E+05   -.103275E+03  .000000E+00
9 -.247860E+05   -.144585E+03  .000000E+00
10 -.743580E+05   -.185895E+03  .000000E+00
0 IINCS= 2 NITER= 100 NOUTP= 2 FACTO= .200000E+00 TOLER= .500000E+00
0 ITERATION NUMBER= 1
0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .115487E+02
0 NODE  DISPL.      REACTION    DISPL.      REACTION
1 .000000E+00   -.344250E+03  .000000E+00   -.170404E+06
2 .958312E+00   .000000E+00   .447078E-02   .000000E+00
3 .274685E+01   .000000E+00   .596104E-02   .000000E+00
4 .458322E+01   .000000E+00   .521591E-02   .000000E+00
5 .590858E+01   .000000E+00   .298052E-02   .000000E+00
6 .638763E+01   .000000E+00   .657992E-09   .000000E+00
7 .590858E+01   .000000E+00   -.298052E-02   .000000E+00
8 .458322E+01   .000000E+00   -.521591E-02   .000000E+00
9 .274685E+01   .000000E+00   -.596104E-02   .000000E+00
10 .958312E+00   .000000E+00   -.447078E-02   .000000E+00
11 .000000E+00   -.344250E+03  .000000E+00   .170404E+06
0 ELEMENT  STRESSES     PL STRAIN
1 -.110015E+06   .309825E+03  .150757E-03
2 -.413100E+05   .240975E+03  .000000E+00
3 .206550E+05   .172125E+03  .000000E+00
4 .619650E+05   .103275E+03  .000000E+00
5 .826200E+05   .344252E+02  .000000E+00
6 .826200E+05   -.344249E+02  -.299783E-03
7 .619650E+05   -.103275E+03  .000000E+00
8 .206550E+05   -.172125E+03  .000000E+00
9 -.413100E+05   -.240975E+03  .000000E+00
10 -.110015E+06   -.309825E+03  .000000E+00
0 ITERATION NUMBER= 2
0 CONVERGENCE CODE= 0 NORM OF RESIDUAL SUM RATIO= .640159E-01
0 NODE  DISPL.      REACTION    DISPL.      REACTION
1 .000000E+00   -.344250E+03  .000000E+00   -.159888E+06

```

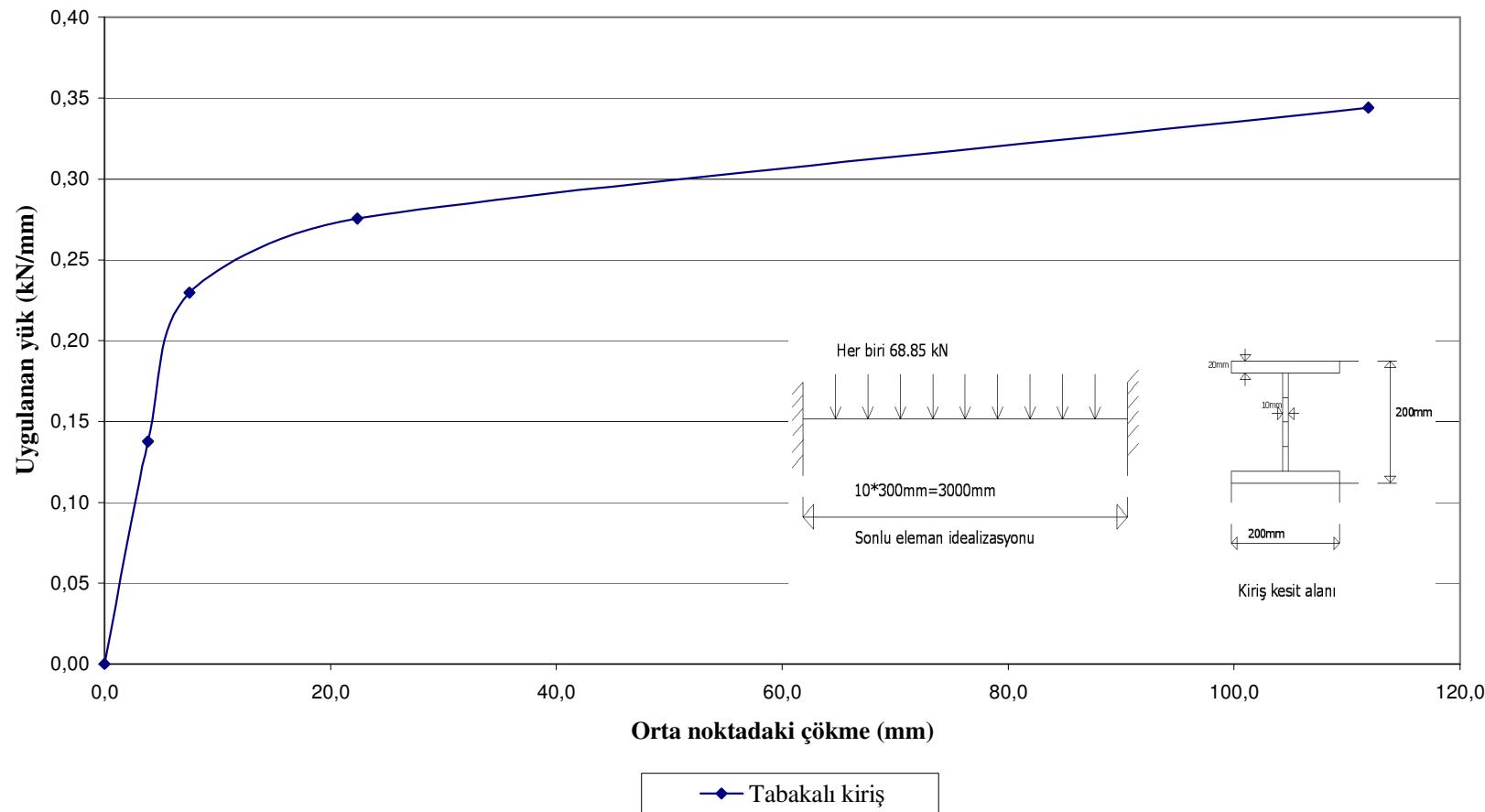
2	.118594E+01	.000000E+00	.598828E-02	.000000E+00
3	.337282E+01	.000000E+00	.709916E-02	.000000E+00
4	.549372E+01	.000000E+00	.597466E-02	.000000E+00
5	.698980E+01	.000000E+00	.335989E-02	.000000E+00
6	.752575E+01	.000000E+00	.495058E-10	.000000E+00
7	.698980E+01	.000000E+00	-.335989E-02	.000000E+00
8	.549372E+01	.000000E+00	-.597466E-02	.000000E+00
9	.337282E+01	.000000E+00	-.709916E-02	.000000E+00
10	.118594E+01	.000000E+00	-.598828E-02	.000000E+00
11	.000000E+00	-.344250E+03	.000000E+00	.159888E+06
0	ELEMENT STRESSES PL STRAIN			
1	-.113341E+06	.309825E+03	.606007E-03	
2	-.307938E+05	.240975E+03	.717924E-05	
3	.311713E+05	.172125E+03	.000000E+00	
4	.724813E+05	.103275E+03	.000000E+00	
5	.931363E+05	.344250E+02	-.717924E-05	
6	.931363E+05	-.344251E+02	-.805616E-03	
7	.724813E+05	-.103275E+03	.000000E+00	
8	.311713E+05	-.172125E+03	.000000E+00	
9	-.307937E+05	-.240975E+03	.000000E+00	
10	-.113341E+06	-.309825E+03	.000000E+00	
0	IINCS= 3 NITER= 100 NOUTP= 2 FACTO= .100000E+00 TOLER= .500000E+00			
0	ITERATION NUMBER= 1			
0	CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .128120E+02			
0	NODE DISPL. REACTION DISPL. REACTION			
1	.000000E+00	-.413100E+03	.000000E+00	-.170082E+06
2	.189461E+01	.000000E+00	.103292E-01	.000000E+00
3	.534397E+01	.000000E+00	.108764E-01	.000000E+00
4	.847841E+01	.000000E+00	.874121E-02	.000000E+00
5	.106273E+02	.000000E+00	.481768E-02	.000000E+00
6	.113883E+02	.000000E+00	.162957E-08	.000000E+00
7	.106273E+02	.000000E+00	-.481768E-02	.000000E+00
8	.847841E+01	.000000E+00	-.874121E-02	.000000E+00
9	.534397E+01	.000000E+00	-.108764E-01	.000000E+00
10	.189461E+01	.000000E+00	-.103292E-01	.000000E+00
11	.000000E+00	-.413100E+03	.000000E+00	.170082E+06
0	ELEMENT STRESSES PL STRAIN			
1	-.114314E+06	.371790E+03	.190828E-02	
2	-.151698E+05	.289170E+03	.875358E-03	
3	.591882E+05	.206550E+03	.000000E+00	
4	.107774E+06	.123930E+03	.000000E+00	
5	.110792E+06	.413098E+02	-.875358E-03	
6	.110792E+06	-.413099E+02	-.225258E-02	
7	.107774E+06	-.123930E+03	.000000E+00	
8	.591882E+05	-.206550E+03	.000000E+00	
9	-.151697E+05	-.289170E+03	.000000E+00	
10	-.114314E+06	-.371790E+03	.000000E+00	
0	ITERATION NUMBER= 2			
0	CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .944435E+01			
0	NODE DISPL. REACTION DISPL. REACTION			
1	.000000E+00	-.413100E+03	.000000E+00	-.172113E+06
2	.325417E+01	.000000E+00	.193929E-01	.000000E+00
3	.943362E+01	.000000E+00	.200134E-01	.000000E+00
4	.153201E+02	.000000E+00	.179514E-01	.000000E+00
5	.202384E+02	.000000E+00	.140697E-01	.000000E+00
6	.223872E+02	.000000E+00	-.720083E-07	.000000E+00
7	.202384E+02	.000000E+00	-.140697E-01	.000000E+00
8	.153201E+02	.000000E+00	-.179514E-01	.000000E+00
9	.943361E+01	.000000E+00	-.200133E-01	.000000E+00
10	.325416E+01	.000000E+00	-.193929E-01	.000000E+00

11 .000000E+00 -.413100E+03 .000000E+00 .172112E+06  
 0 ELEMENT STRESSES PL STRAIN  
 1 -.116000E+06 .371790E+03 .462739E-02  
 2 -.171999E+05 .289170E+03 .268810E-02  
 3 .571582E+05 .206550E+03 .102382E-03  
 4 .106613E+06 .123930E+03 -.102382E-03  
 5 .115152E+06 .413103E+02 -.268810E-02  
 6 .115152E+06 -.413103E+02 -.527382E-02  
 7 .106613E+06 -.123930E+03 .000000E+00  
 8 .571580E+05 -.206550E+03 .000000E+00  
 9 -.172000E+05 -.289170E+03 .000000E+00  
 10 -.116000E+06 -.371790E+03 .000000E+00  
 0 ITERATION NUMBER= 3  
 0 CONVERGENCE CODE= 1 NORM OF RESIDUAL SUM RATIO= .926178E+01  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.413097E+03 .000000E+00 -.171768E+06  
 2 .144469E+02 .000000E+00 .940113E-01 .000000E+00  
 3 .430100E+02 .000000E+00 .946194E-01 .000000E+00  
 4 .712765E+02 .000000E+00 .925451E-01 .000000E+00  
 5 .985701E+02 .000000E+00 .886451E-01 .000000E+00  
 6 .111905E+03 .000000E+00 .132569E-05 .000000E+00  
 7 .985705E+02 .000000E+00 -.886454E-01 .000000E+00  
 8 .712768E+02 .000000E+00 -.925454E-01 .000000E+00  
 9 .430102E+02 .000000E+00 -.946197E-01 .000000E+00  
 10 .144470E+02 .000000E+00 -.940116E-01 .000000E+00  
 11 .000000E+00 -.413098E+03 .000000E+00 .171768E+06  
 0 ELEMENT STRESSES PL STRAIN  
 1 -.116000E+06 .371786E+03 .270129E-01  
 2 -.168573E+05 .289164E+03 .176118E-01  
 3 .574994E+05 .206550E+03 .507694E-02  
 4 .107122E+06 .123933E+03 -.507694E-02  
 5 .116000E+06 .413106E+02 -.176118E-01  
 6 .116000E+06 -.413081E+02 -.301466E-01  
 7 .107123E+06 -.123932E+03 .000000E+00  
 8 .575000E+05 -.206549E+03 .000000E+00  
 9 -.168567E+05 -.289171E+03 .000000E+00  
 10 -.116000E+06 -.371788E+03 .000000E+00  
 0 ITERATION NUMBER= 4  
 0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .135229E+09  
 0 NODE DISPL. REACTION DISPL. REACTION  
 1 .000000E+00 -.479563E+03 .000000E+00 -.174186E+06  
 2 .813898E+06 .000000E+00 .542599E+04 .000000E+00  
 3 .244169E+07 .000000E+00 .542599E+04 .000000E+00  
 4 .406949E+07 .000000E+00 .542599E+04 .000000E+00  
 5 .569729E+07 .000000E+00 .542599E+04 .000000E+00  
 6 .484165E+07 .000000E+00 -.111303E+05 .000000E+00  
 7 .277560E+07 .000000E+00 -.264342E+04 .000000E+00  
 8 .198257E+07 .000000E+00 -.264342E+04 .000000E+00  
 9 .118954E+07 .000000E+00 -.264342E+04 .000000E+00  
 10 .396514E+06 .000000E+00 -.264342E+04 .000000E+00  
 11 .000000E+00 -.426317E+03 .000000E+00 .173751E+06  
 0 ELEMENT STRESSES PL STRAIN  
 1 -.116000E+06 .382303E+03 .162779E+04  
 2 -.439276E+05 .152445E+03 .108520E+04  
 3 .335876E+04 .135036E+03 .361731E+03  
 4 .259107E+05 .609809E+03 -.361731E+03  
 5 .116000E+06 -.217403E+03 -.108520E+04  
 6 -.235257E+12 .380937E+02 -.180866E+04  
 7 .800531E+05 .137936E+03 .000000E+00  
 8 .507325E+05 -.141871E+03 .000000E+00

```

9 -.168567E+05 -.263931E+03 .000000E+00
10 -.116000E+06 -.359167E+03 .000000E+00
0 ITERATION NUMBER= 5
0 CONVERGENCE CODE= 999 NORM OF RESIDUAL SUM RATIO= .424689E+12
0 NODE  DISPL.      REACTION    DISPL.      REACTION
  1 .000000E+00   -.567864E+08 .000000E+00   .877179E+09
  2 .107387E+13   .000000E+00 .715914E+10   .000000E+00
  3 .322161E+13   .000000E+00 .715914E+10   .000000E+00
  4 .536936E+13   .000000E+00 .715914E+10   .000000E+00
  5 .751710E+13   .000000E+00 .715914E+10   .000000E+00
  6 .160584E+14   .000000E+00 .497826E+11   .000000E+00
  7 .205850E+14   .000000E+00 -.196048E+11   .000000E+00
  8 .147036E+14   .000000E+00 -.196048E+11   .000000E+00
  9 .882215E+13   .000000E+00 -.196048E+11   .000000E+00
 10 .294072E+13   .000000E+00 -.196048E+11   .000000E+00
 11 .000000E+00   -.426317E+03 .000000E+00   .173751E+06
0 ELEMENT      STRESSES      PL STRAIN
  1 -.116000E+06 .231585E+08 .214774E+10
  2 .115948E+06 -.153284E+09 .143183E+10
  3 -.115843E+06 .463163E+08 .477276E+09
  4 -.114581E+06 .280103E+09 -.477276E+09
  5 -.108605E+19 -.242609E+09 -.143183E+10
  6 .192342E+19 -.463162E+09 -.238638E+10
  7 -.110382E+06 -.529326E+08 -.153598E+03
  8 -.111785E+06 .688126E+09 -.102398E+02
  9 -.168567E+05 -.255842E+09 -.341320E+02
 10 -.116000E+06 .295541E+09 .341320E+02

```



Şekil 5.13: Uniform yayılı yüklü tabakalı Timoshenko kırışı örneği



## **6. SONUÇ ve ÖNERİLER**

Bu çalışmada Timoshenko kırışının sonlu elemanlar yöntemi ile elastoplastik analizi yapılmıştır. Bu amaçla daha önce Fortran dilinde kodlanmış olan kapsamlı bir sonlu eleman programı Windows altında tekrar yazılarak derlenmiştir.

Kullanılan yazılımda iki serbestlikli çubuk eleman (Hughes elemanı) kullanılarak yapılan yaklaşımaya karşılık tezde kayma şekil değiştirmesini dikkate alan kırış sonlu eleman rijitlik matrisi kullanılmıştır. Kırışın elastik zemine oturma hali de incelenmiştir. Bu amaçla tek parametrelî zemine (Winkler zemini) ait rijitlik matrisi kayma şekil değiştirmesini de içeren matrise eklenmiştir. Mevcut program bu şekilde değiştirilmiştir.

Aynı yazılım kullanılarak en kesitin tabakalı olması haline karşı gelen hal de incelenmiştir. Tabakalı halde, enkesit yükseklik boyunca yeteri sayıda tabakaya ayrılmakta her tabakanın orta noktasında oluşan eğilme momenti plastikleşme momentine eriştiğinde o tabakanın plastikleştiği varsayılmaktadır. En dış tabakadan içe doğru tüm tabakalar plastikleştiğinde kesit tümüyle plastikleşmiş olmaktadır. Tabaka sayısı arttıkça sonuçların daha da iyileştiği açıkları.

Malzemenin ideal elastoplastik olduğu varsayılmıştır. Aynı yazılımda pekleşme de dikkate alınabilmektedir.

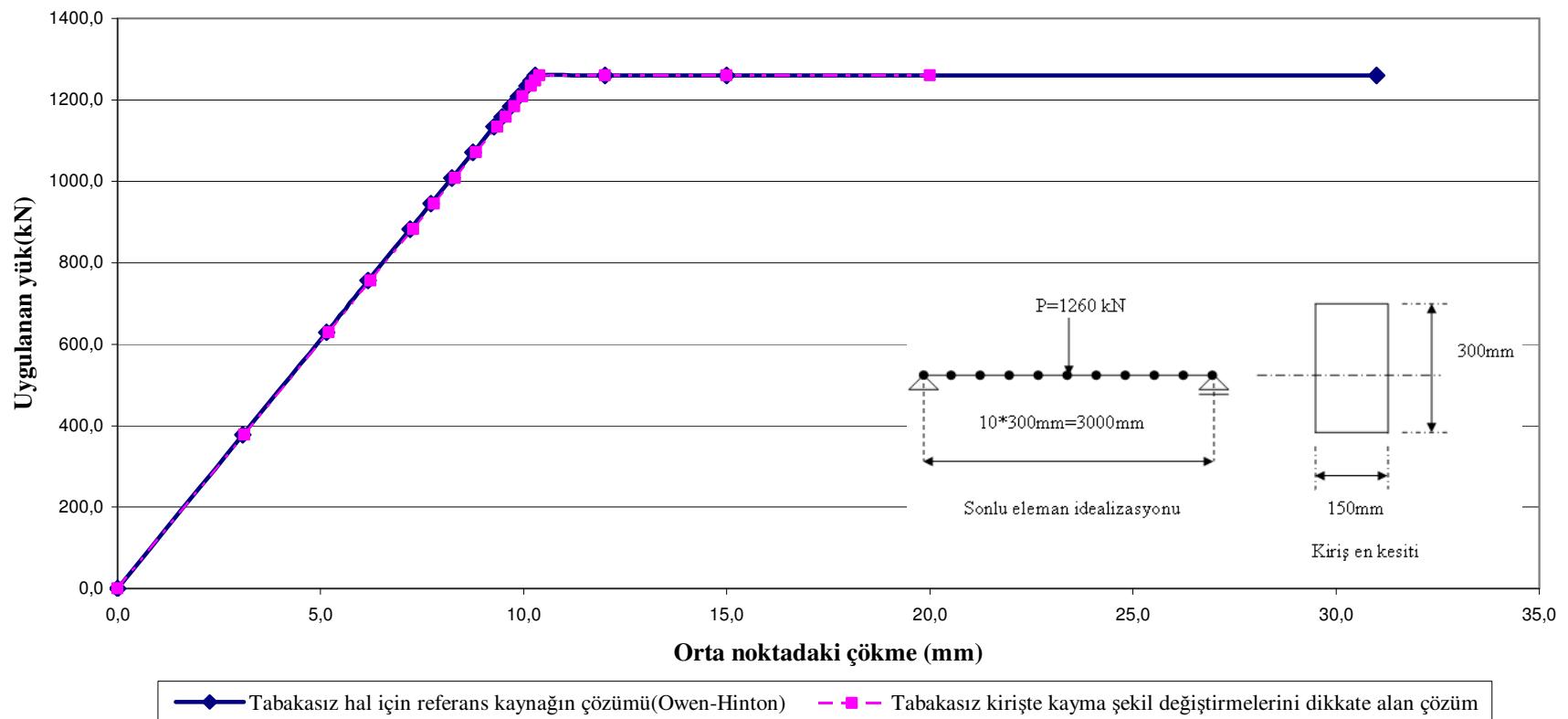
Derlenen yazılım tekil yük etkisindeki basit kırış ve yayılı yük etkisindeki ankastre kırış örnekleri tabakasız ve tabakalı haller için kullanılmış, sonuçlar çıktı ve diyagramlar halinde karşılaştırılmalı olarak sunulmuştur. Basit kırış örneğinde dikdörtgen kesit, yayılı yük halinde ise (I) kesit alınmıştır. Basit kırış örneğinde 3

farklı elastik zemin için yapılan uygulamalar, verilen örnek için, değerlerin çok fazla fark etmediğini göstermektedir.

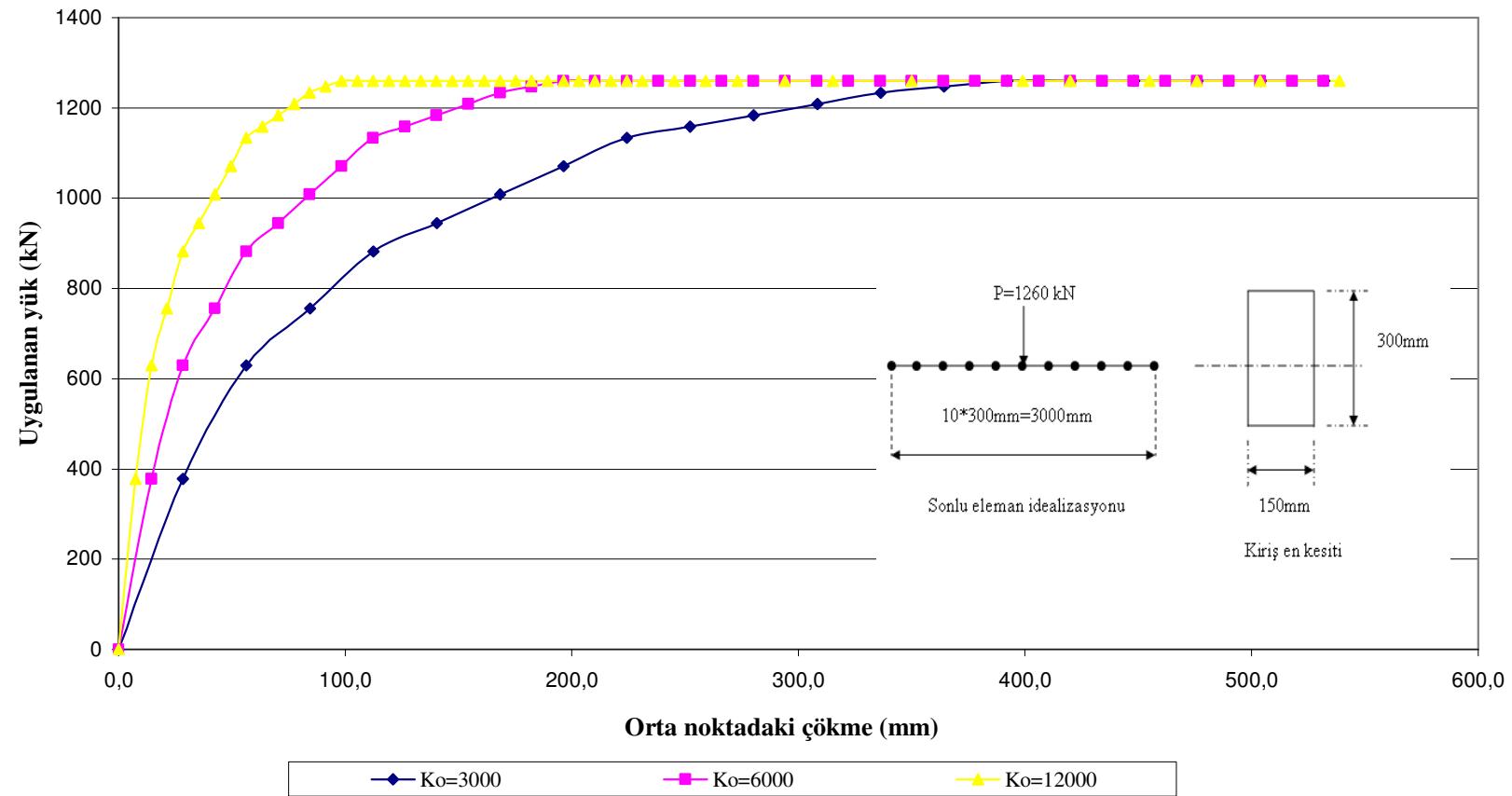
Tabakalı halde yük yer değiştirme diyagramının keskin köşeler yerine, tabaka tabaka plastikleşme olduğu için, beklendiği üzere yumuşak eğriler şeklinde olduğu görülmektedir. Bu halde diyagram tabakasız hale çok yakın, ama onun biraz altında seyretmektedir.

Bu geliştirilmiş yazılım sayesinde Timoshenko kırışının elastik zemine oturma halini de kapsayacak şekilde elastoplastik analizi yapılmaktadır. Tez kapsamı içerisinde iyileştirilmiş yazılıma ait program listesi ve giriş bilgileri ayrıntılı olarak açıklanmış ve araştırmacıların programı kolayca kullanımı sağlanmıştır. Sayısal hesaplardan elde edilen sonuçlar kaynaklardakiler ile örtüşmektedir. Toplu sonuçlar (Şekil 6.1-6.5) de diyagramları ile karşılaştırılmalı olarak verilmiştir.

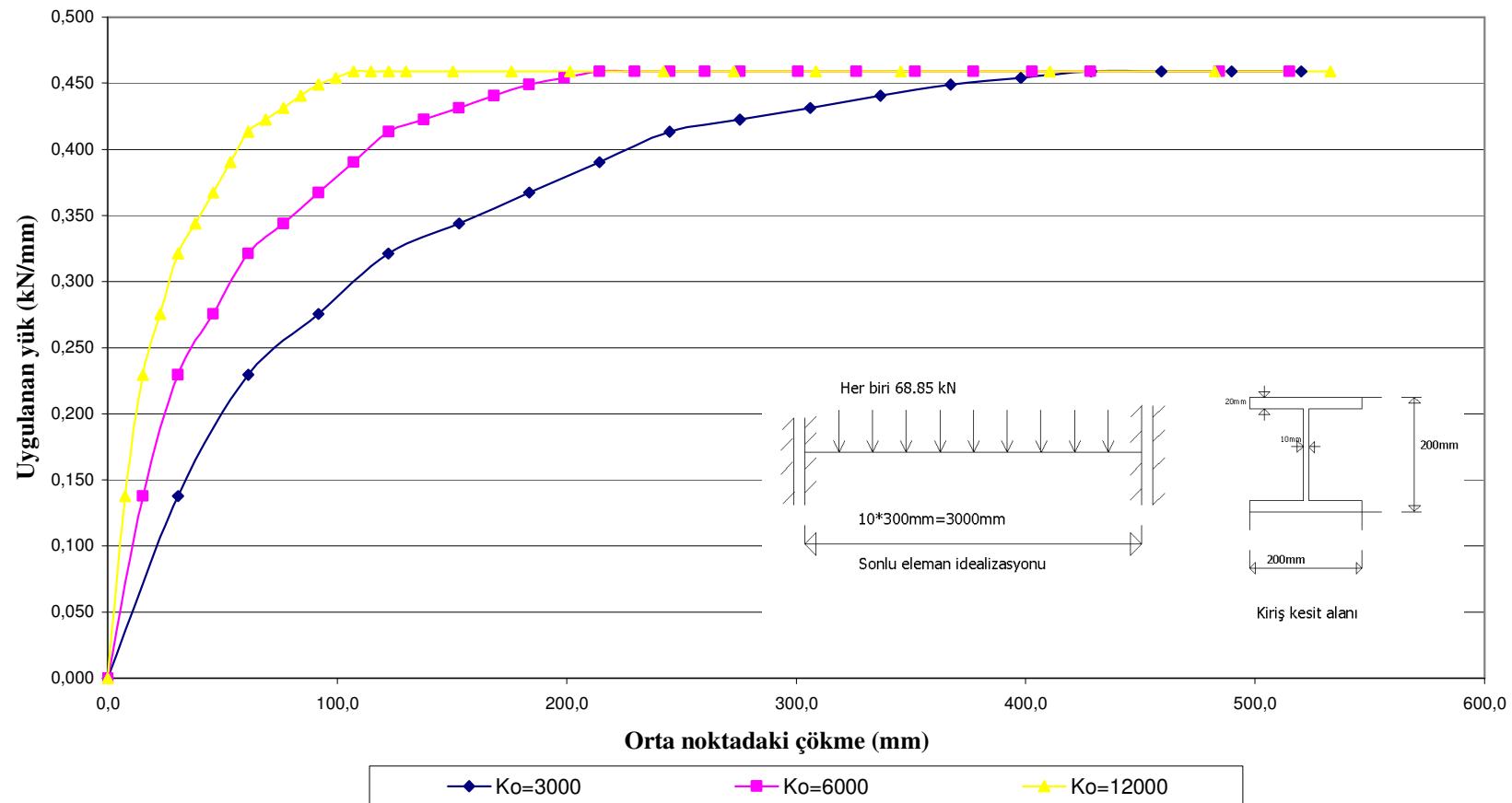
İleri bir adım olarak aynı yol izlenerek iki parametreli zeminler için de analiz yapılabilir.



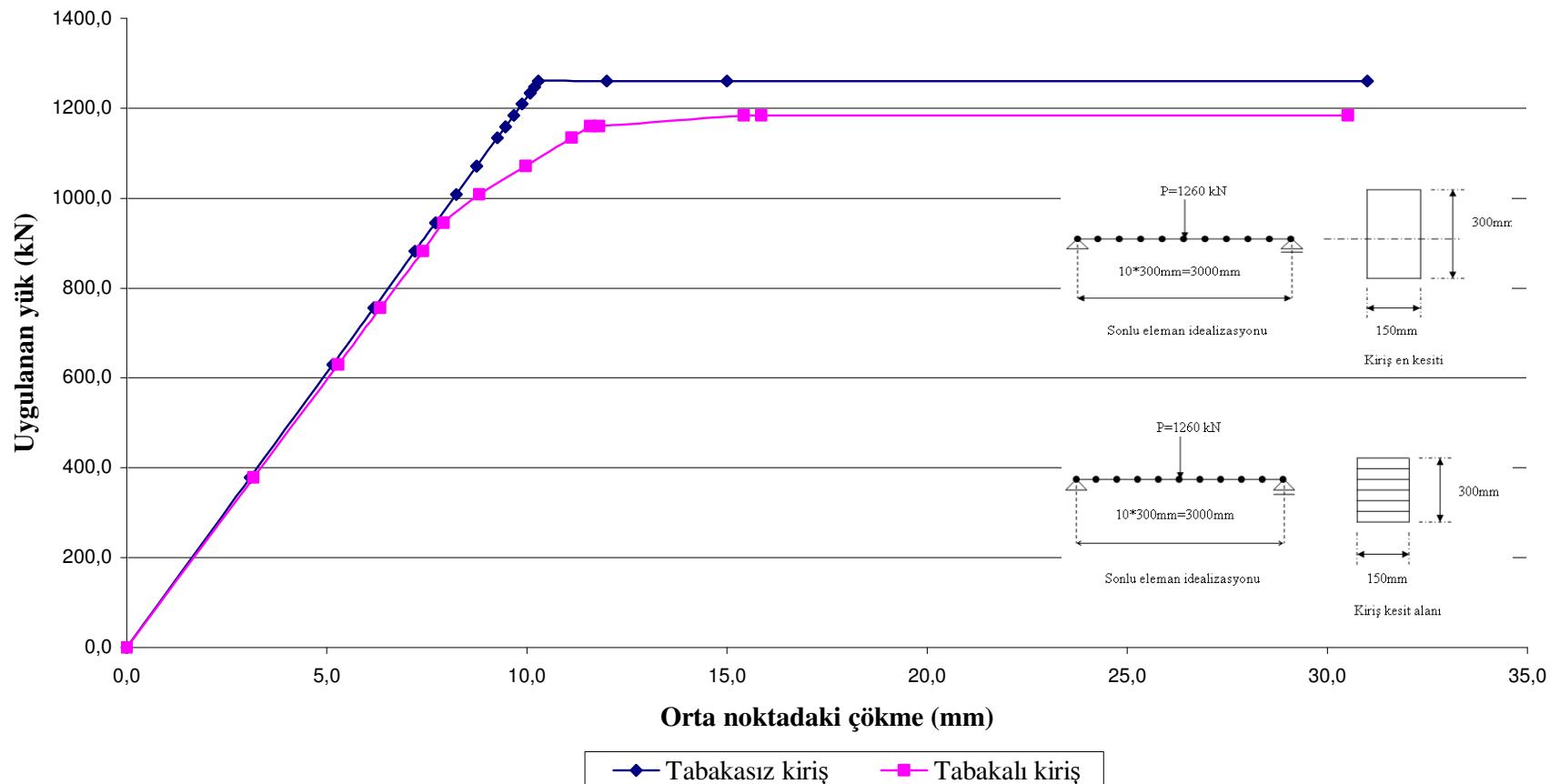
**Şekil 6.1:** Tabakasız Kırışte Tekil Yük Hali İçin Referans Kaynak Çözümü ile Kayma Şekil Değiştirmesini Dikkate Alan Çözümün Karşılaştırılması



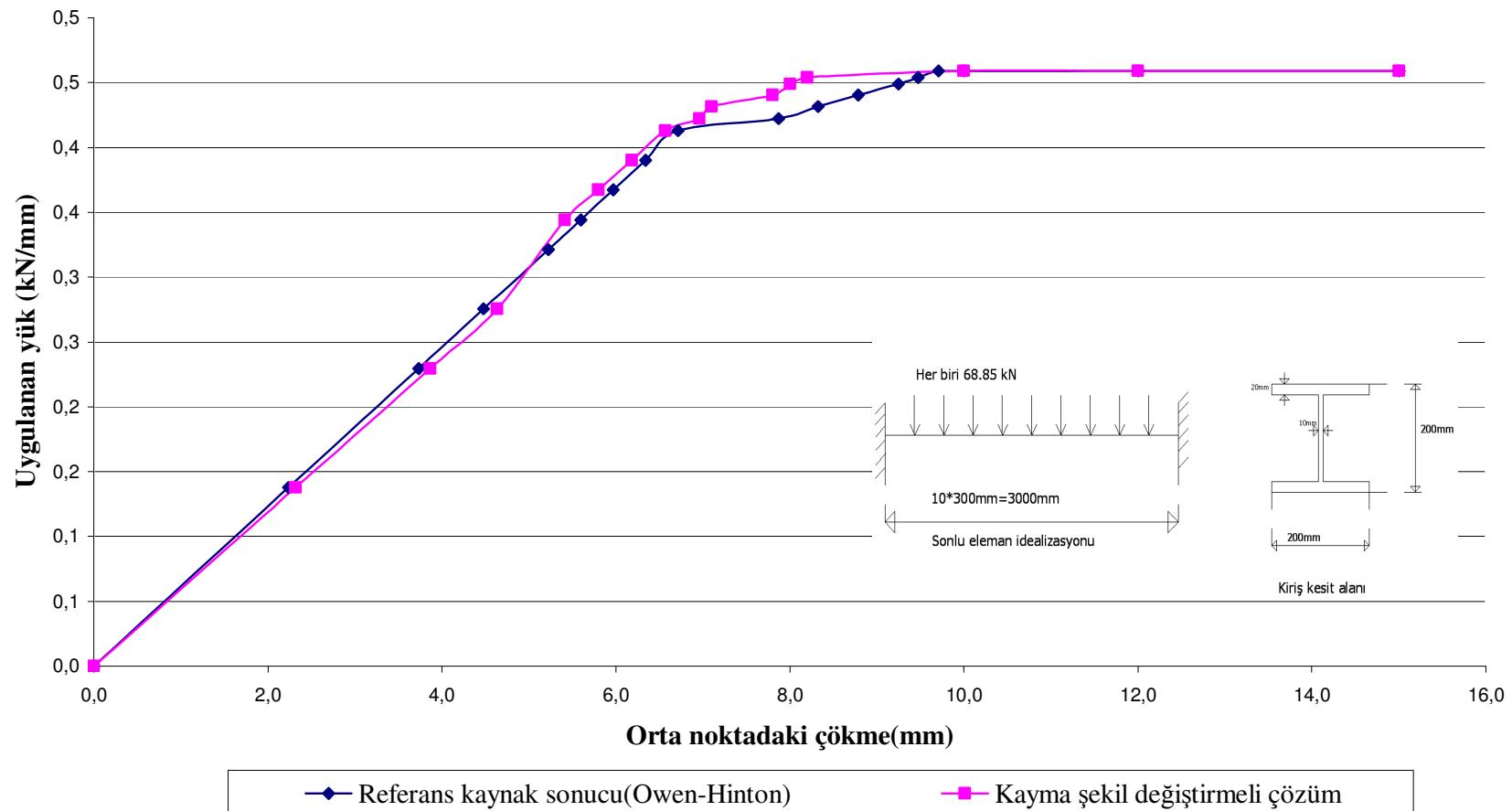
Şekil 6.2: Tabakasız kirişte tekil yük halinde 3 farklı zemin durumu için karşılaştırma



**Şekil 6.3:** Tabakasız kirişte yayılı yük halinde 3 farklı zemin durumunda karşılaştırma



Şekil 6.4: Tekil Yük Hali İçin Tabakasız Kirişle Tabakalı Kirişin Karşılaştırılması



**Şekil 6.5:**Tabakasız Kirişe Yaylı Yük Etkimesi Hali İçin Karşılaştırma



## KAYNAKLAR

- Aydoğan,M.,and Omurtag,M.H.**,Finite Element Methods, Ders notları, 2008.
- Celep,Z.**,Betonarme taşıyıcı sistemlerde doğrusal olmayan davranış ve çözümleme,Beta Dağıtım, İstanbul 2008.
- Çakıroğlu,A.,Özden,E.,and Özmen,G.**, Yapı sistemlerinin hesabı için matris metotları ve elektronik hesap makinası programları,Cilt1-2,.İTÜ İnşaat Fakültesi matbaası, İstanbul 1992.
- Çakıroğlu,A.,Özer,E.**, Malzeme ve geometri değişimi bakımından lineer olmayan sistemler,Cilt 1, İTÜ, 1980.
- Hughes,T.J.R.,Taylor ,R.L.,and Kanoknukulchai,S.**,A simple and efficient finite element for bending,Int.J.Num.Meth.Engng.,1977.
- İnan,M.**, Cisimlerin mukavemeti,İstanbul,1981.
- Kumbasar,N.,Pala,S.,Aydoğan,M.,Altan,M.,Yardımcı,N.,andYıldırım,H.**, Bilgisayar programları ile sayısal hesap, İMO İstanbul Şb. Yayıncı, İstanbul 1992.
- Owen,D.R.J.,and Hinton,E.**,Finite elements in plasticity:theory and practice. Department of Civil Engineering, University of Swansea, Pineridge Press, U.K.,1980.
- Özer,E.**, Yapı sistemlerinin lineer olmayan analizi ders notları, 2008.
- Saygun, A., Trupia, A., Özden,K.**, Temeller (Baskıda),2009.
- Yücel,N.**, Fortran IV,Nilüfer matbaası, İstanbul 1974.
- Zienkiewicz,O.C.**, The finite element method,McGraw-Hill,1977.



## **ÖZGEÇMİŞ**

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